



POLITECNICO
MILANO 1863

From vehicle dynamics control to autonomous driving in urban environments

Vertical Dynamics Control: semi active damping and stiffness control

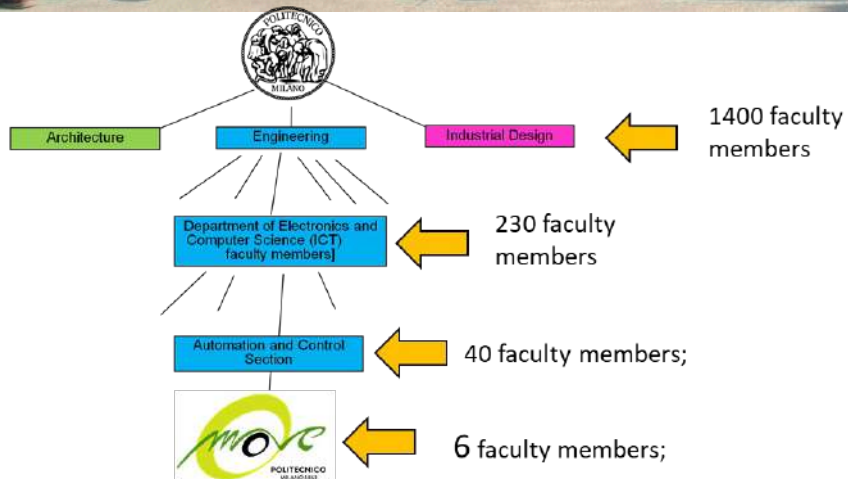
4/7/2023, Bertinoro



Matteo Corno



- Founded in 1863
- Polytechnic: Engineering, Architecture and Design
- 40.000 students; 1400 Faculty members



Faculty: 6
PhD: 15-20
MSc: 40-50

Prof. **Matteo Corno**



- Master of Science in Computer Science and Engineering, Politecnico di Milano
- Master of Science in Electronic Engineering, University of Illinois at Chicago, USA
- PhD in Systems and Control, Politecnico di Milano, Italia
- Post-Doc, Linz, University Austria
- Assistant professor at TU Delft, The Netherlands
- Associate professor, Politecnico di Milano.

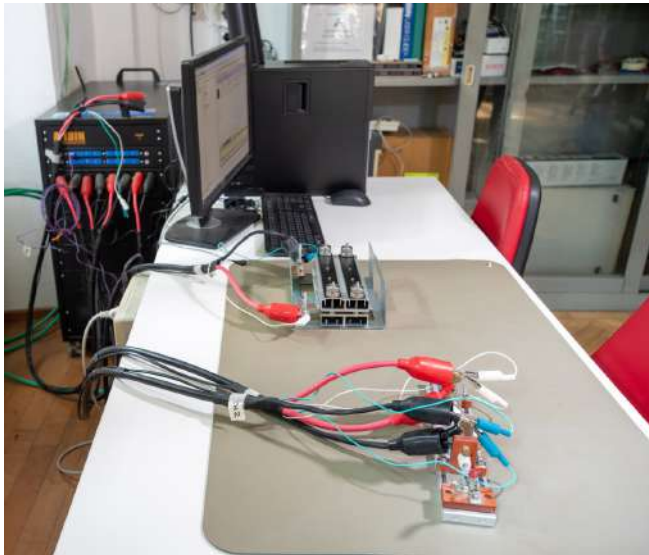
Research Interests: ***Automation and Control in Land Vehicles***

<https://www.move.deib.polimi.it/>

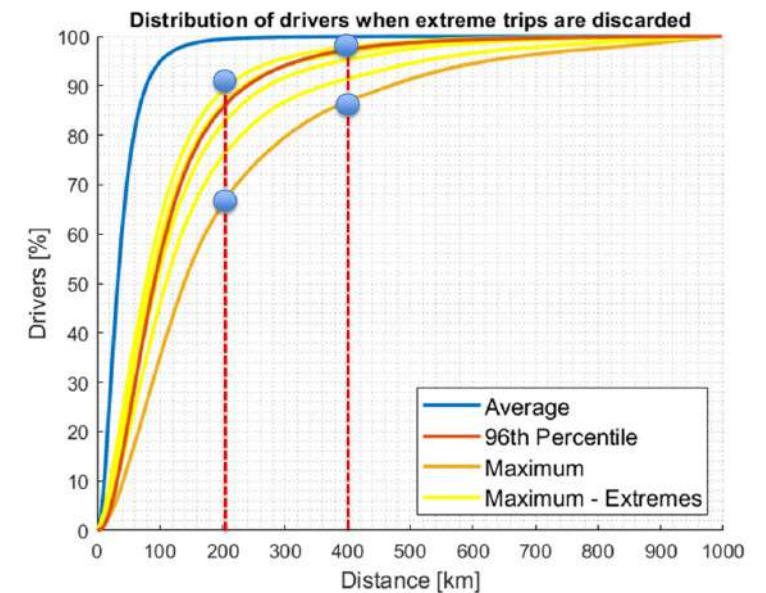


mOve carries out research, innovation and technology transfer activities in the areas of automotive controls, intelligent vehicles and smart mobility.

From component level



To fleet management





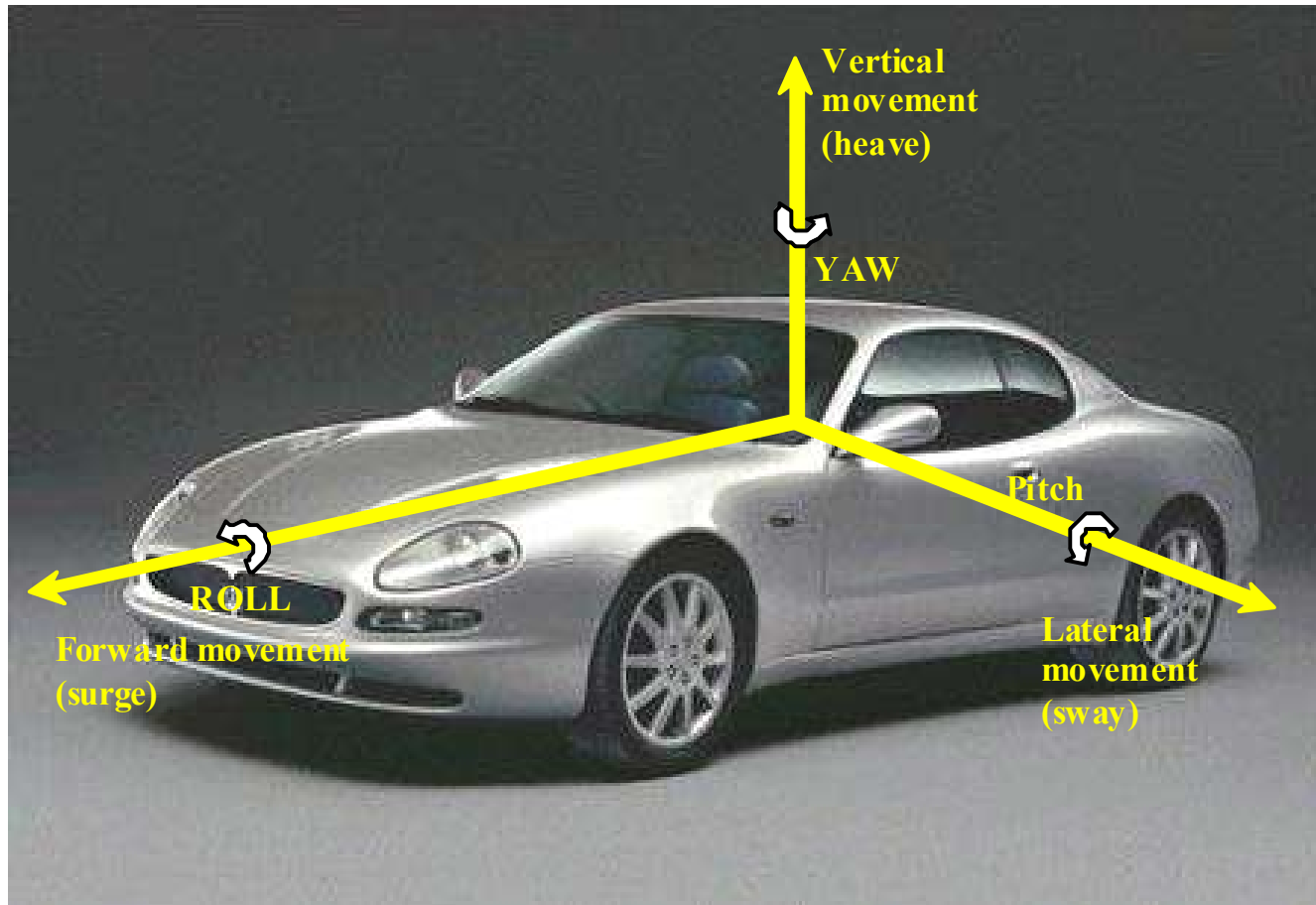
- Winners of the Indy Autonomous Challenge (Las Vegas, 2022-2023, Texas, 2023, Monza 2023)
- Record holders for the fastest autonomous car (@ Kennedy Space Center) 310 km/h (May 2022)

- Introduction
- Semi-Active Damping Control
 - Actuators
 - Models
 - Benchmark
 - Causal Control
- Semi-Active Stiffness Control
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- Sensing Preliminaries
- A look at the future
- Conclusions

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Introduction to Vertical Dynamics

Vertical Dynamics and its Influence



General goal: filter the road-to-vehicle interaction

Related movements (main):

- Heave
- Roll
- Pitch

Can influence (indirectly) also yaw/sway/surge.

Introduction to Vertical Dynamics

Why suspensions in 2023?



Introduction to Vertical Dynamics

Suspension System Goals

Goals of Suspension System:

- 1) Comfort → chassis vertical acceleration, pitch and roll movements



Introduction to Vertical Dynamics

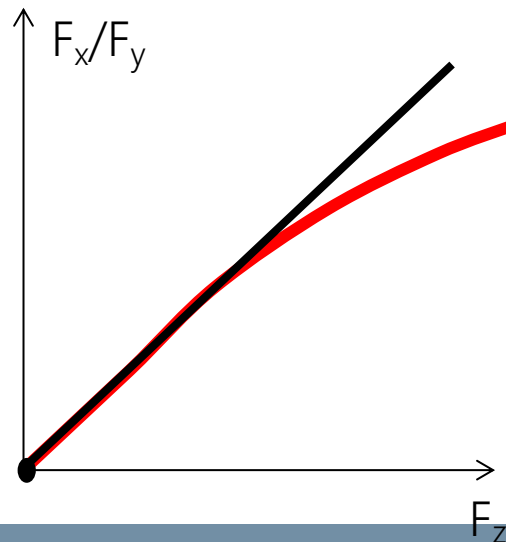
Suspension System Goals

Goals of Suspension System:

- 1) Comfort → chassis vertical acceleration, pitch and roll movements
- 2) Road Holding → keep vertical load as constant as possible

$$F_x = \mu_x(F_z)$$
$$F_y = \mu_y(F_z)$$

$$F_z = (M + m)g + \text{DynamicLoad} + [\text{AerodynamicLoad}]$$

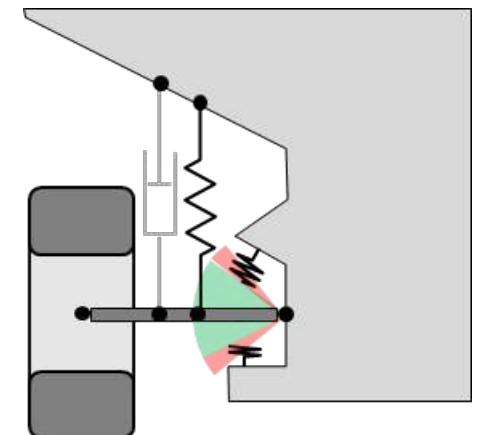


Introduction to Vertical Dynamics

Suspension System Goals

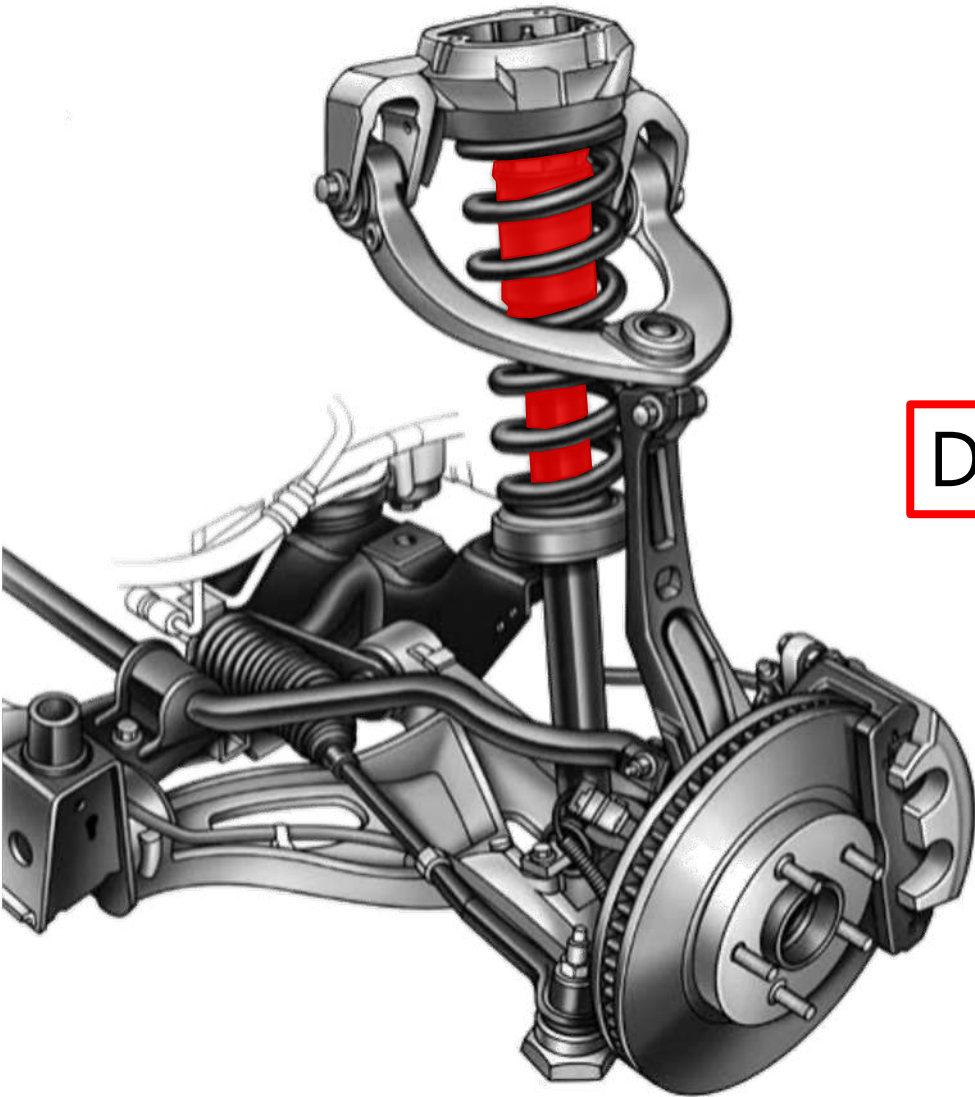
Goals of Suspension System:

- 1) Comfort → chassis vertical acceleration, pitch and roll movements
- 2) Road Holding → keep vertical load as constant as possible
- 3) Avoid hitting bump stops → keep the stroke of the suspension limited

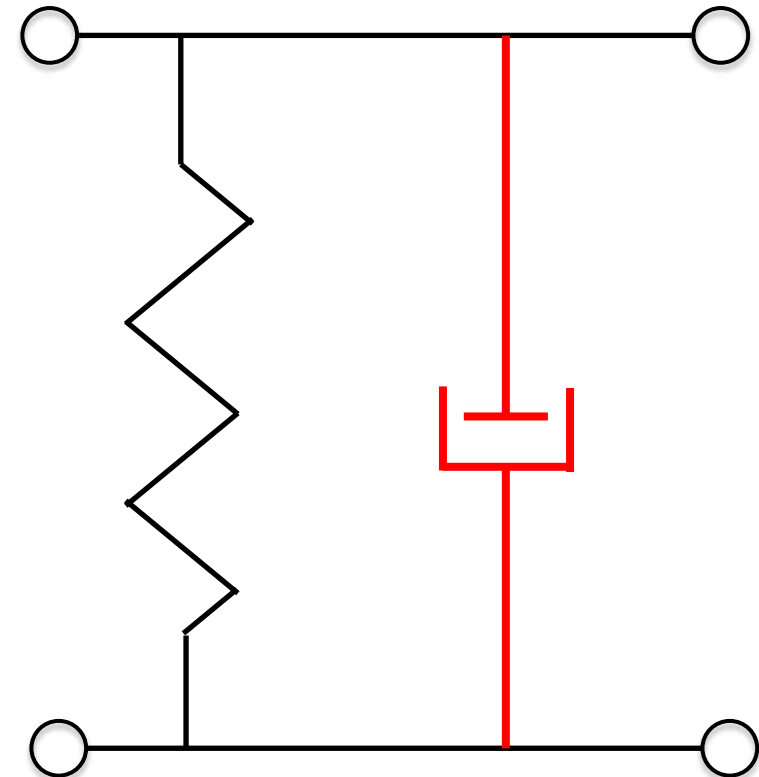


Introduction to Vertical Dynamics

Main Components of a Suspension



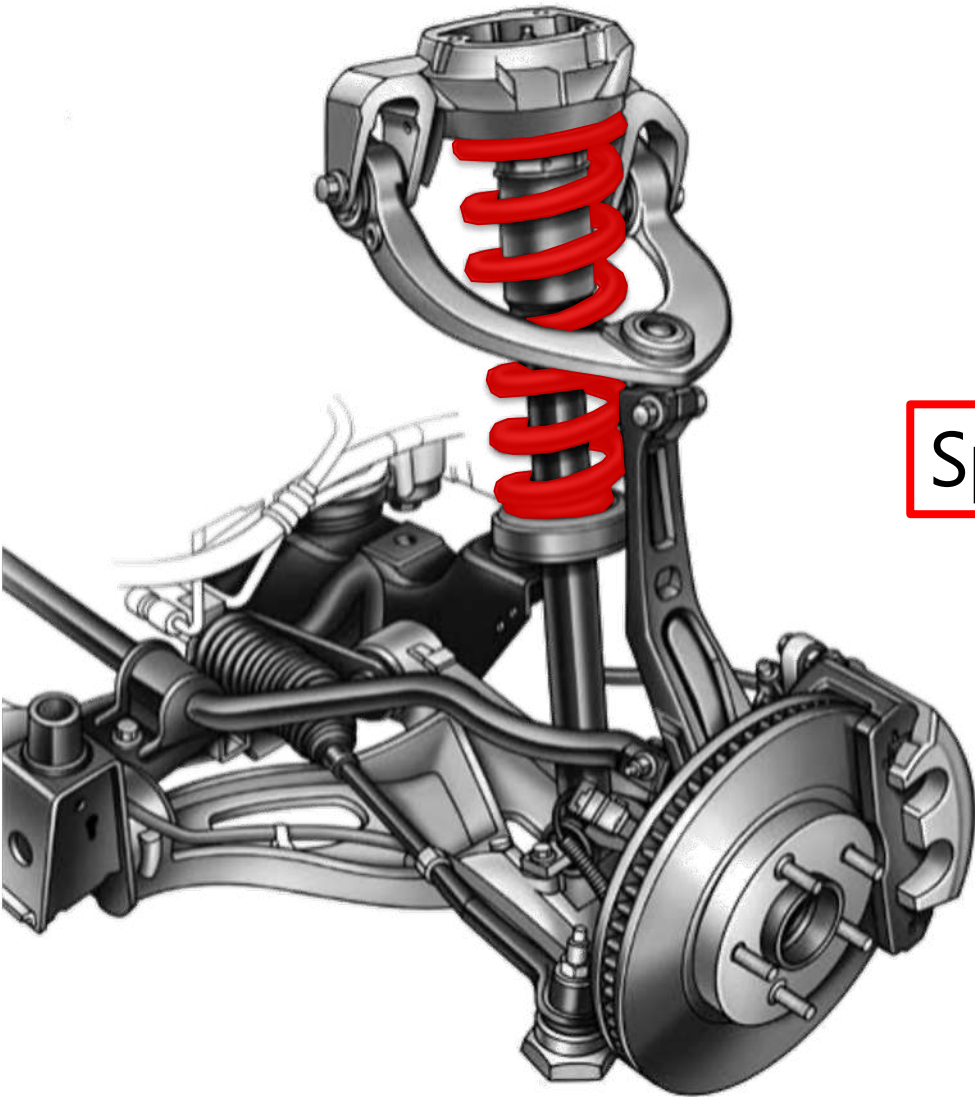
Damper (c)



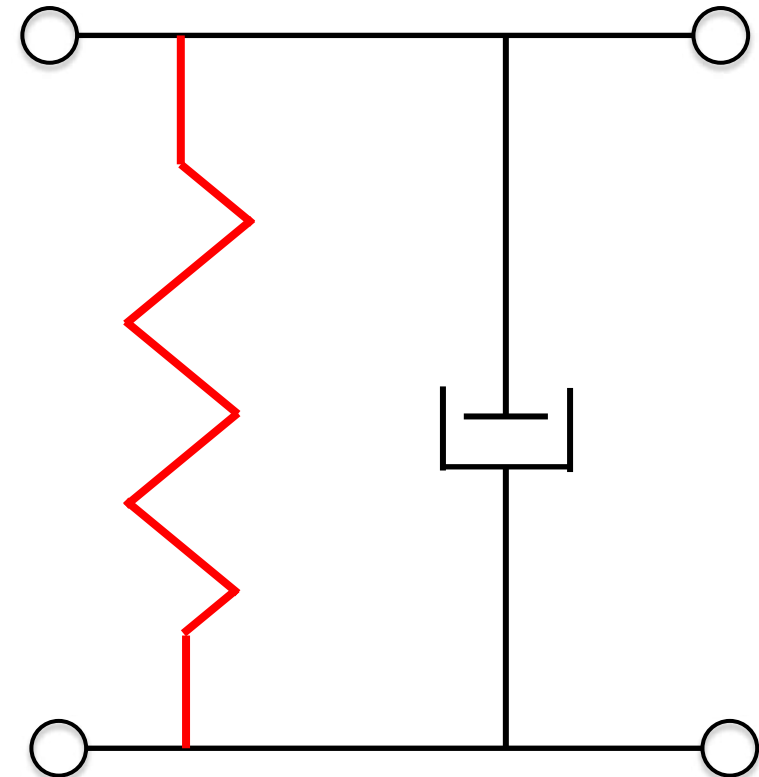
Damper: force function of stroke speed

Introduction to Vertical Dynamics

Main Components of a Suspension



Spring (k)



Spring: force function of stroke

How do we introduce control?

Actuators

Classification of suspension systems. Natural frequencies: f_B body and f_W wheel

System	System representation	Force range	Operation range	Max. energy demand
Passive			—	—
Slowly variable/adaptive			Quasi static	ca. 50 W
Semi-active			High frequency	ca. 50 W
Load-leveling (height adjuster)			Quasi static	ca. 50 W
Active partially loaded («slow-active»)			Mid frequency	1–2 kW
Active fully loaded («full-active»)			High frequency	1.5–7 kW

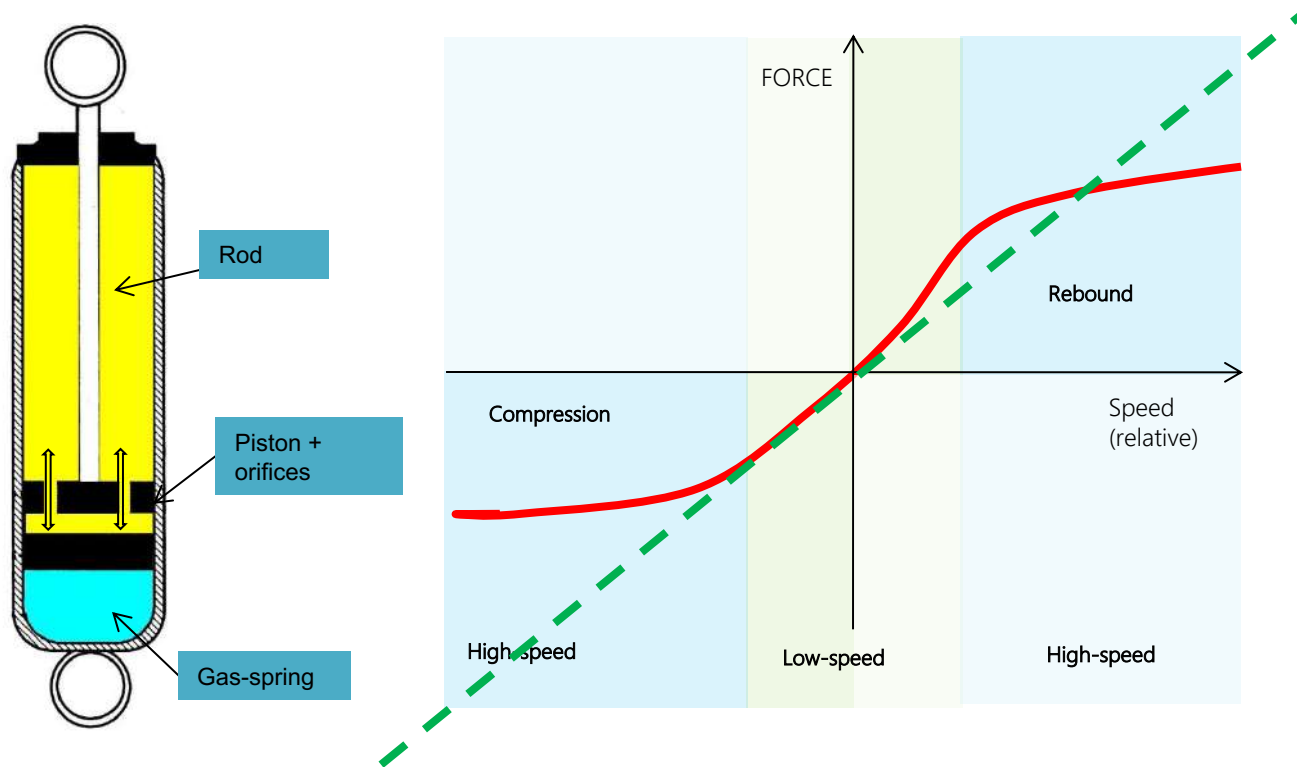
Industrially viable, but control is challenging

They change the characteristics without injecting mechanical energy

- Introduction
- **Semi-Active Damping Control**
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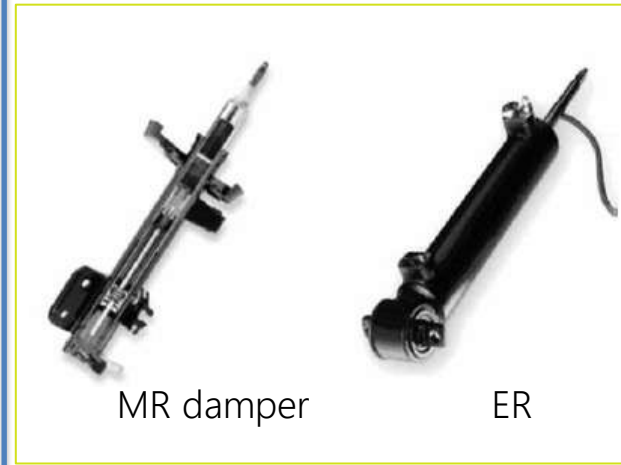
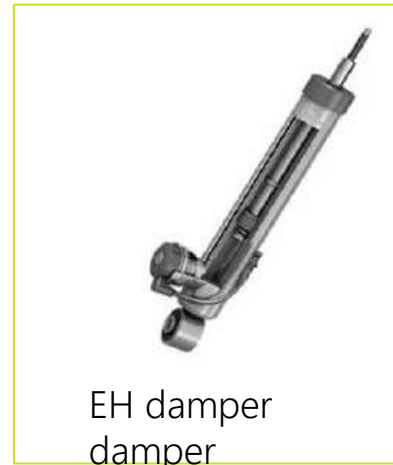
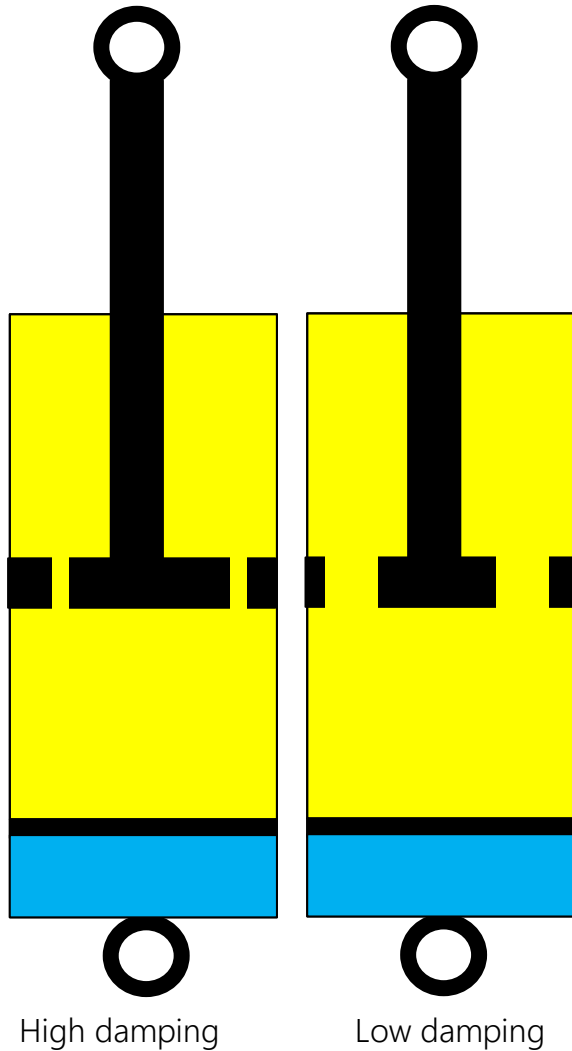
Semi-Active Damping Control

Actuator Technology



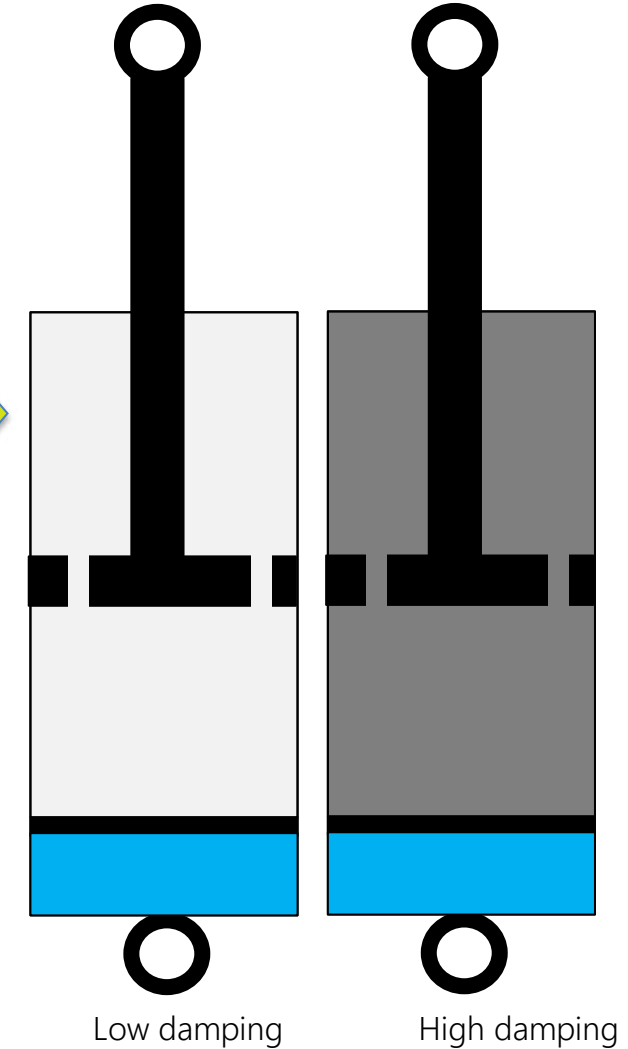
Semi-Active Damping Control

Actuator Technology



Electro-Hydraulic valve opens and closes (mechanical variation of orifices size)

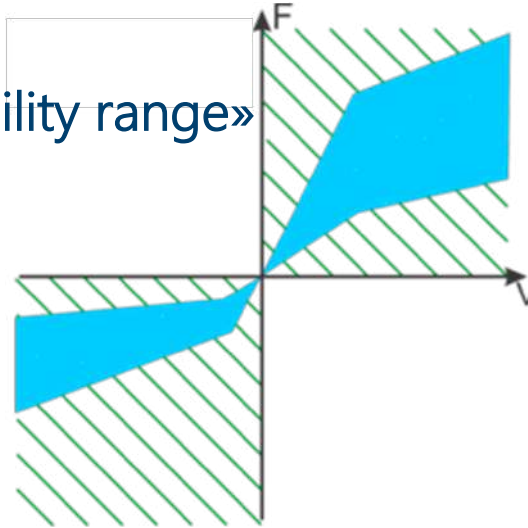
Magnetic or Electric field changes viscosity of the (Magneto-Rheologic or Electro-



Semi-Active Damping Control

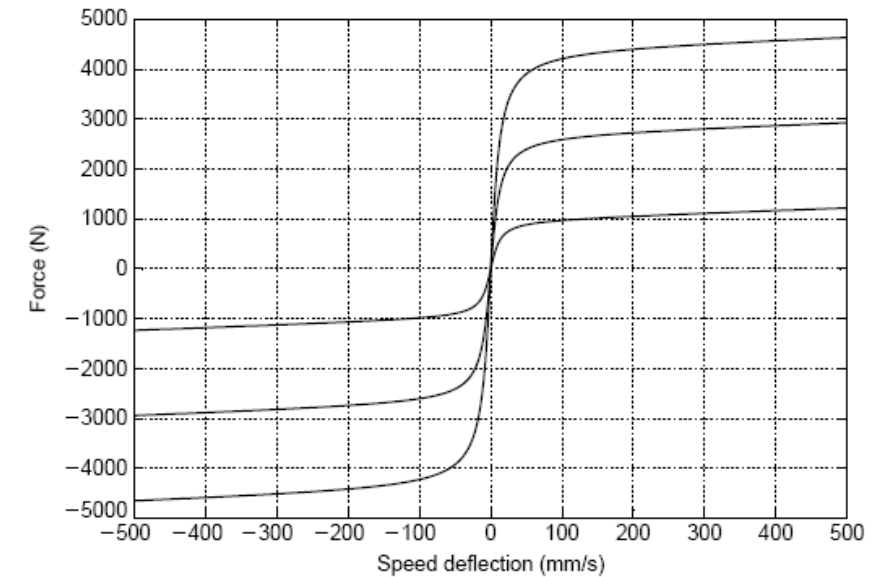
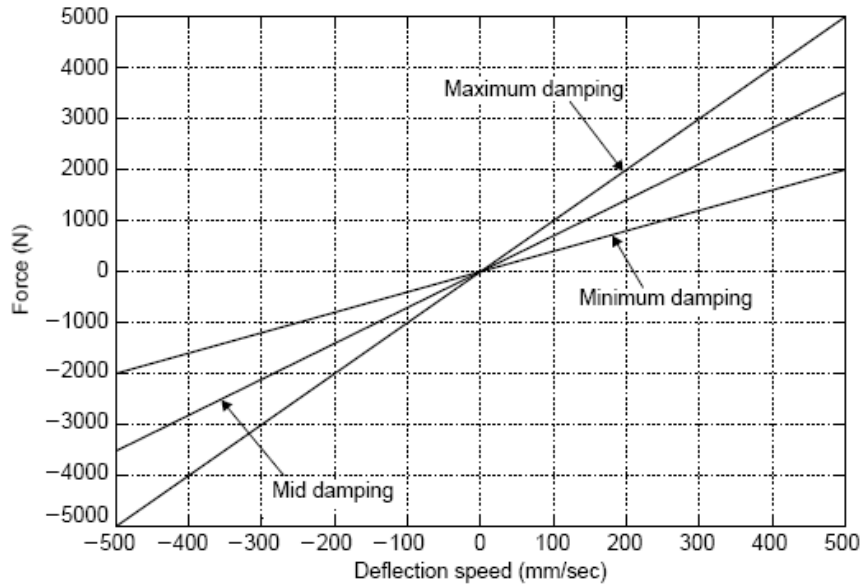
Actuator Technology – Static Characteristics

«Controllability range»



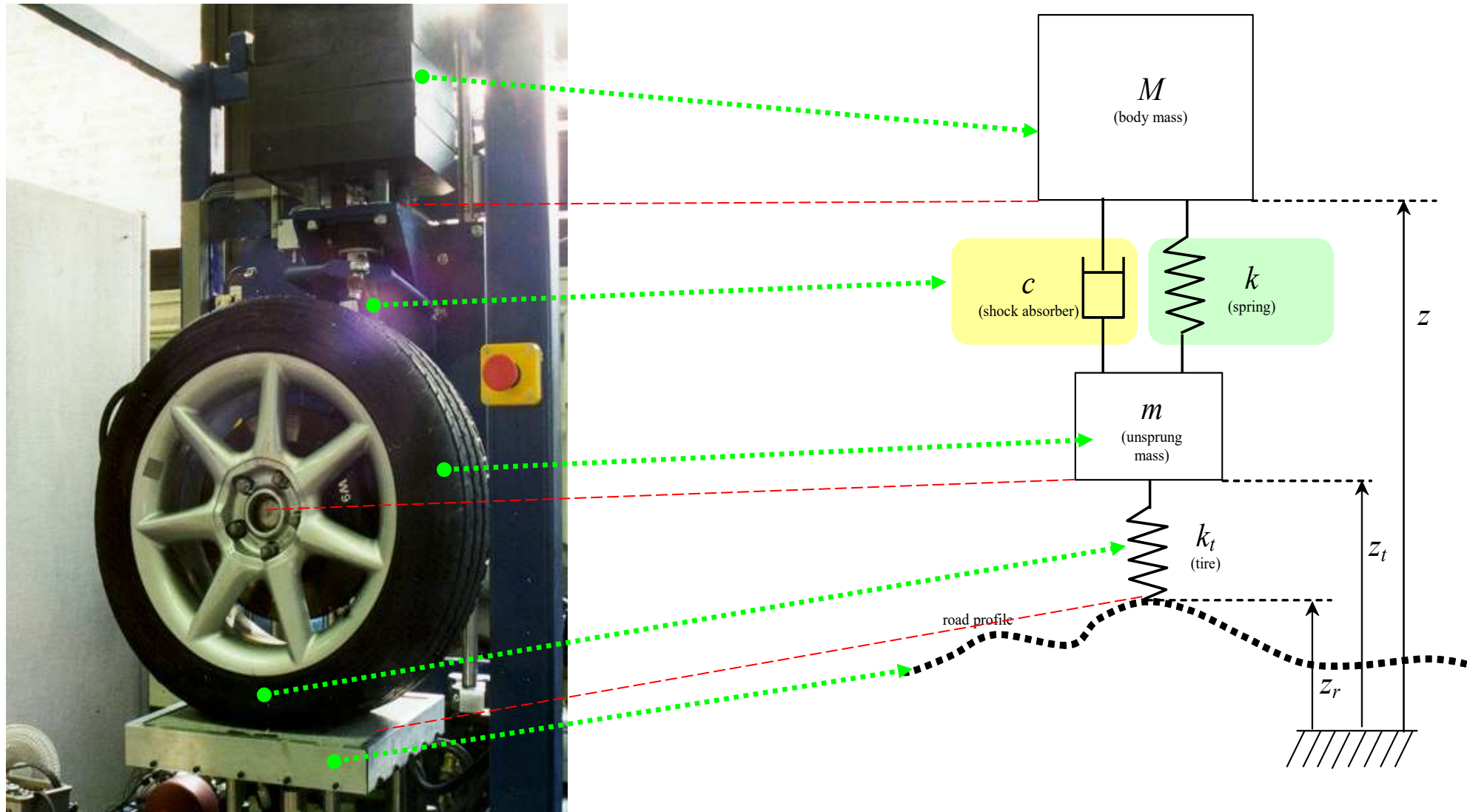
EH damper

MR damper



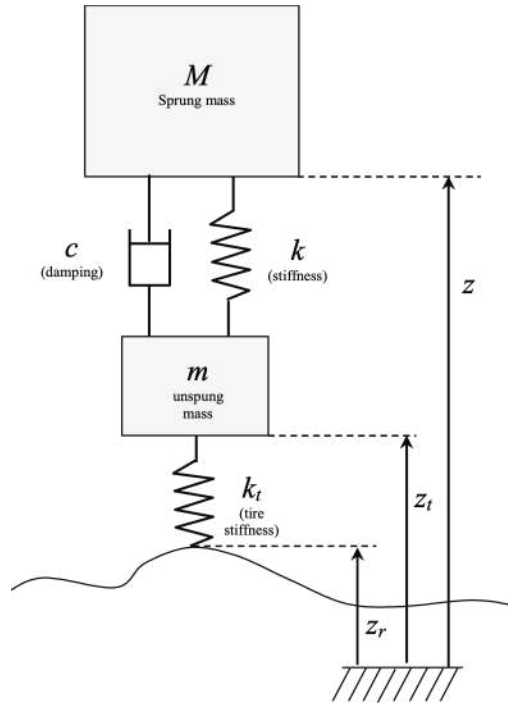
Semi-Active Damping Control

The quarter-car model and its features



Semi-Active Damping Control

The quarter-car model and its features



$$\mathbf{x} = \begin{bmatrix} z \\ \dot{z} \\ z_t \\ \dot{z}_t \end{bmatrix}$$

$$\mathbf{u} = z_r$$

$$\mathbf{y} = \begin{bmatrix} z \\ z_t \end{bmatrix}$$

Example of parameters

$$M = 400 \text{ Kg}$$

$$m = 50 \text{ Kg}$$

$$k = 20 \text{ KN / m}$$

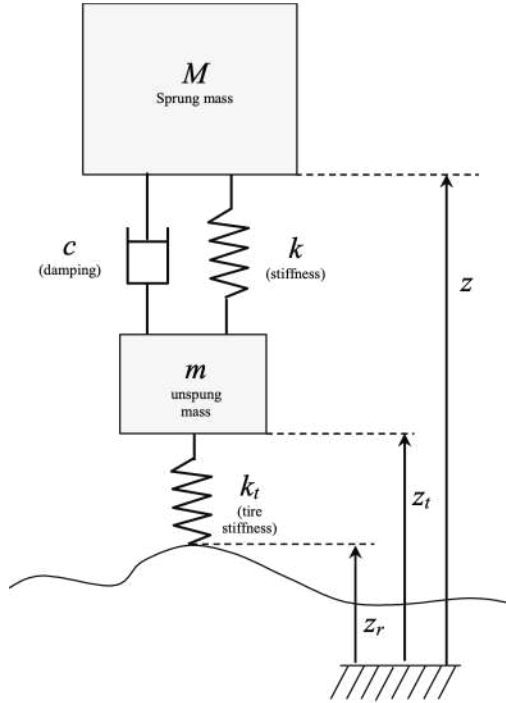
$$k_t = 250 \text{ KN / m}$$

$$c = 1,3 \text{ KN} \cdot \text{s / m}$$

$$\begin{cases} M\ddot{z}(t) = -c(\dot{z}(t) - \dot{z}_t(t)) - k(z(t) - z_t(t) - \Delta_s) - Mg \\ m\ddot{z}_t(t) = +c(\dot{z}(t) - \dot{z}_t(t)) + k(z(t) - z_t(t) - \Delta_s) - k_t(z_t(t) - z_r(t) - \Delta_t) - mg \end{cases}$$

Semi-Active Damping Control

The quarter-car model and its features



Linearizing Around an equilibrium point

$$\begin{cases} \dot{x}_1 = x_2 \\ \dot{x}_2 = -\frac{k}{M}x_1 - \frac{c}{M}x_2 + \frac{k}{M}x_3 + \frac{c}{M}x_4 \\ \dot{x}_3 = x_4 \\ \dot{x}_4 = \frac{k}{m}x_1 + \frac{c}{m}x_2 - \frac{k+k_t}{m}x_3 - \frac{c}{m}x_4 + \frac{k_t}{m}u \\ y_1 = x_1 \\ y_2 = x_3 \end{cases}$$

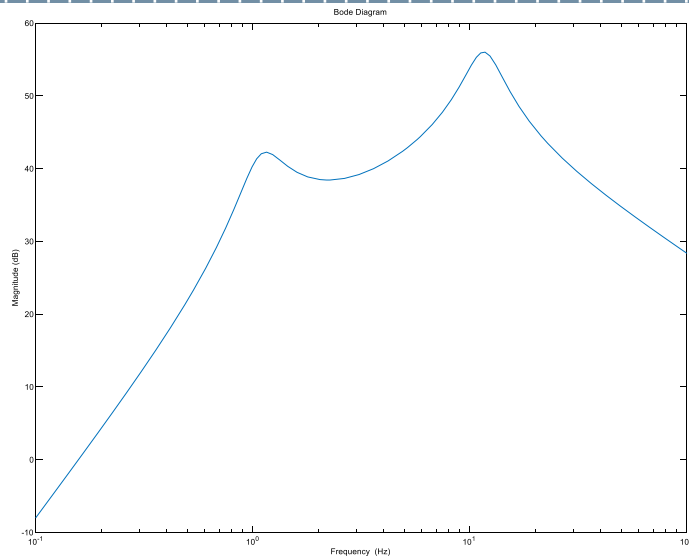
$$x = \begin{bmatrix} \delta z \\ \delta \dot{z} \\ \delta z_t \\ \delta \dot{z}_t \end{bmatrix}, \quad u = [\delta z_r], \quad y = \begin{bmatrix} \delta z \\ \delta z_t \end{bmatrix}$$

From which the transfer functions

$$\begin{cases} \delta Z(s) = F_z(s)U(s) \\ \delta Z_t(s) = F_{z_t}(s)U(s) \end{cases}$$

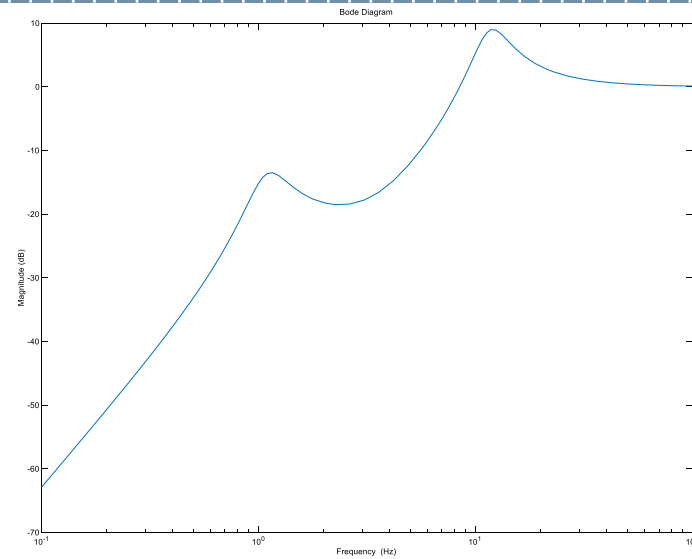
Semi-Active Damping Control

The quarter-car model and its features



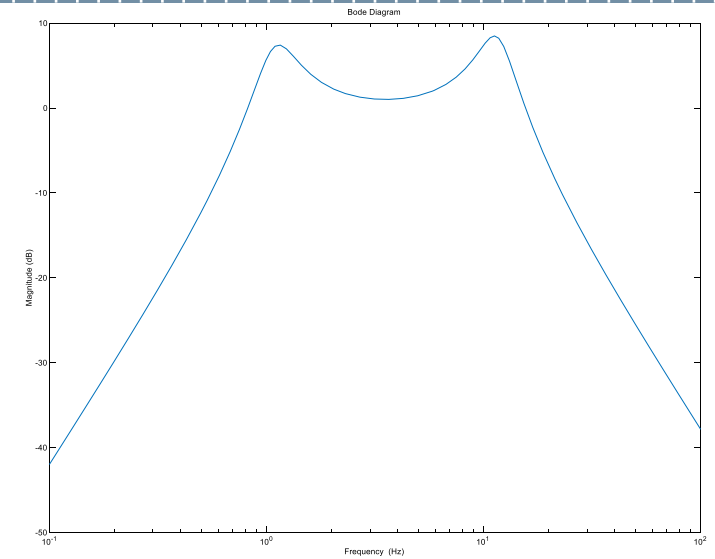
$$\delta z_r \rightarrow \ddot{\delta z} = s^2 F_z(s)$$

«Comfort» or
«acceleration» transfer
function



$$\delta z_r \rightarrow \delta z_t - \delta z_r = F_{zt}(s) - 1$$

«Road-contact» transfer
function



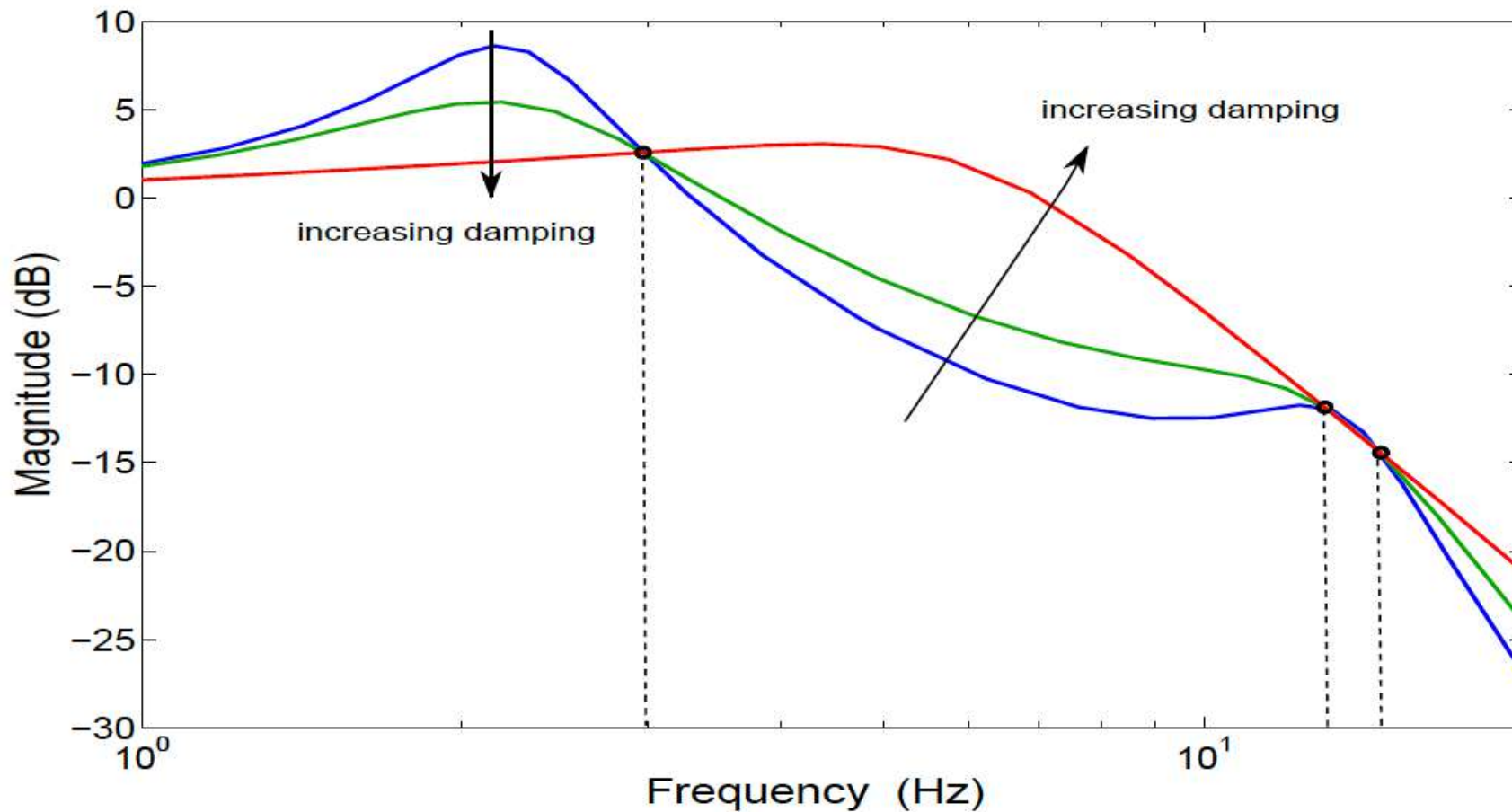
$$\delta z_r \rightarrow \delta z - \delta z_t = F_z(s) - F_{zt}(s)$$

«Elongation» transfer
function

Semi-Active Damping Control

The quarter-car model and its features

Frequency response of $F_z(s)$

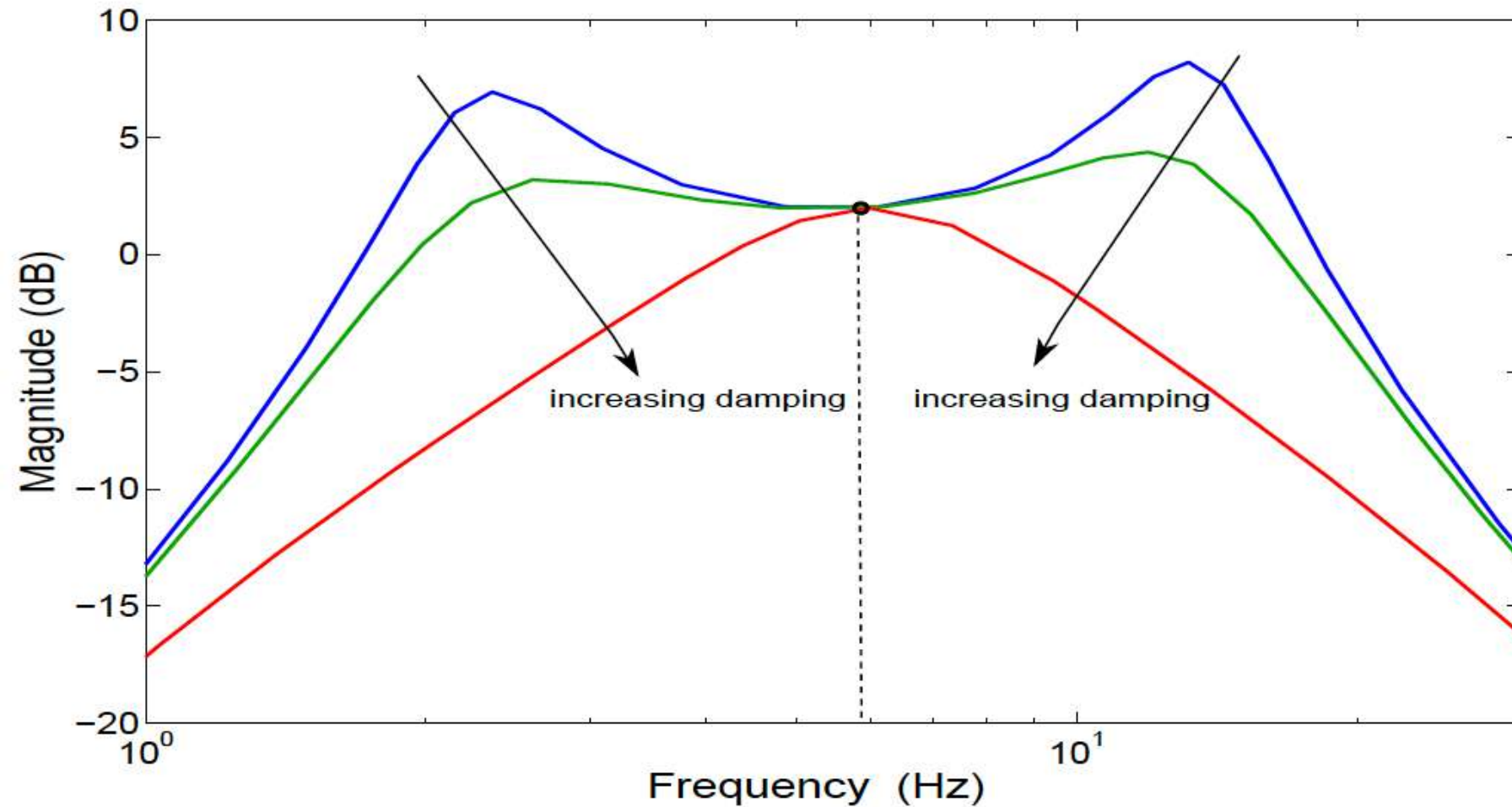


green: $c=2600$ Ns/m
blue : $c=1300$ Ns/m
red: $c=750$ Ns/m

Semi-Active Damping Control

The quarter-car model and its features

Frequency response of $Fz_{\text{def}}(s)$

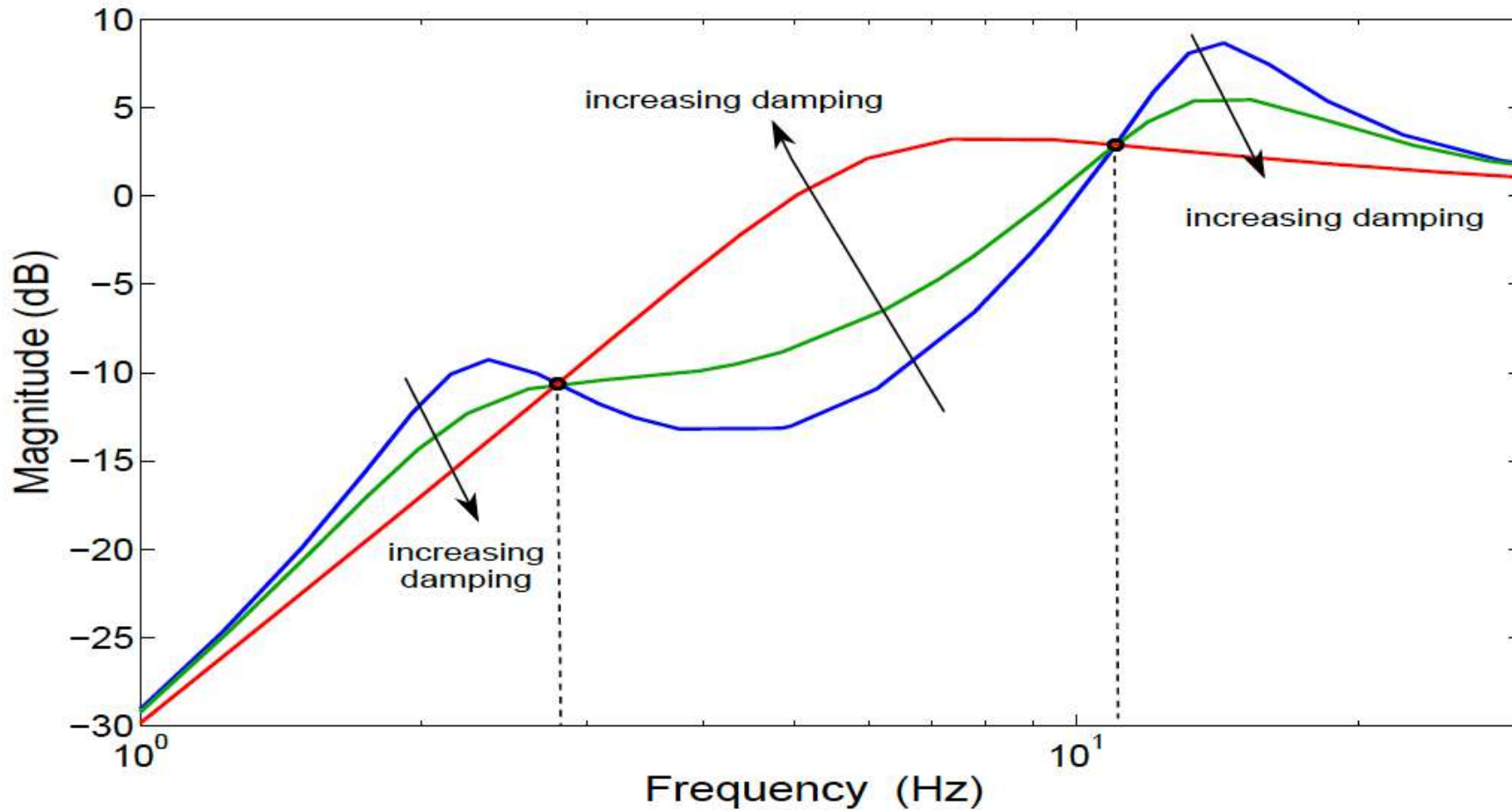


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Semi-Active Damping Control

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Frequency response of $Fz_{\text{deft}}(s)$

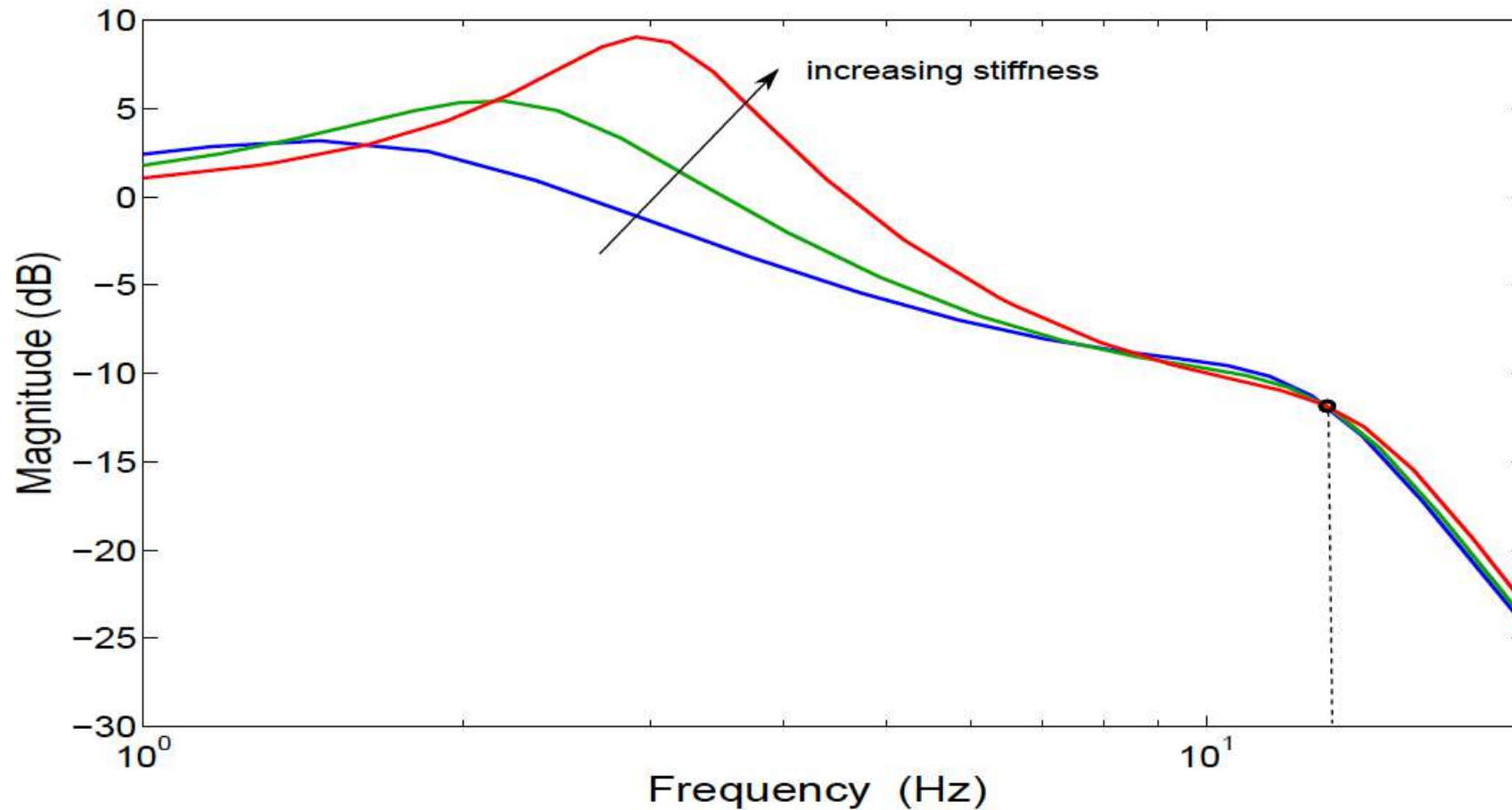


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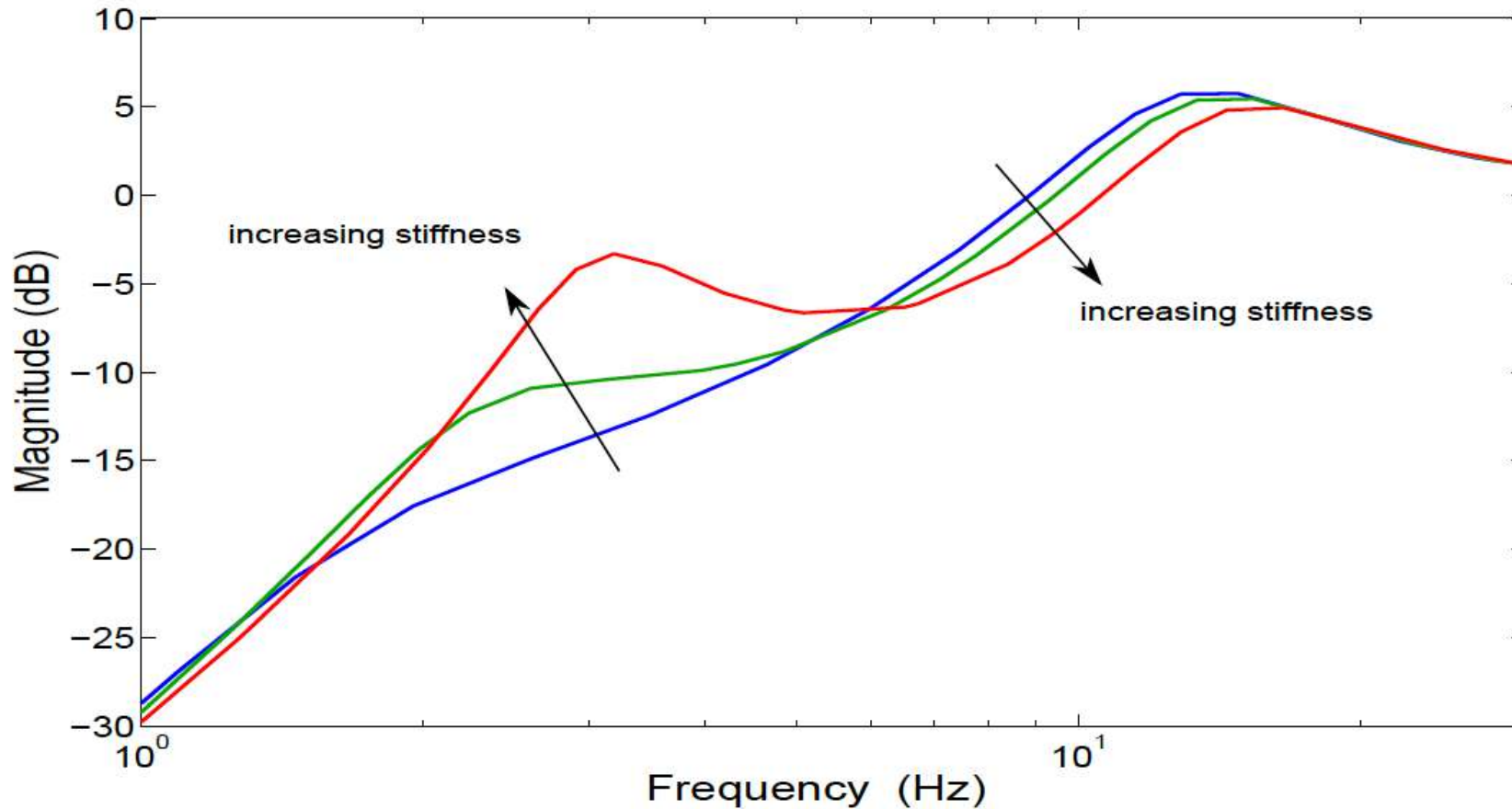


blue : $k=20000$ N/m
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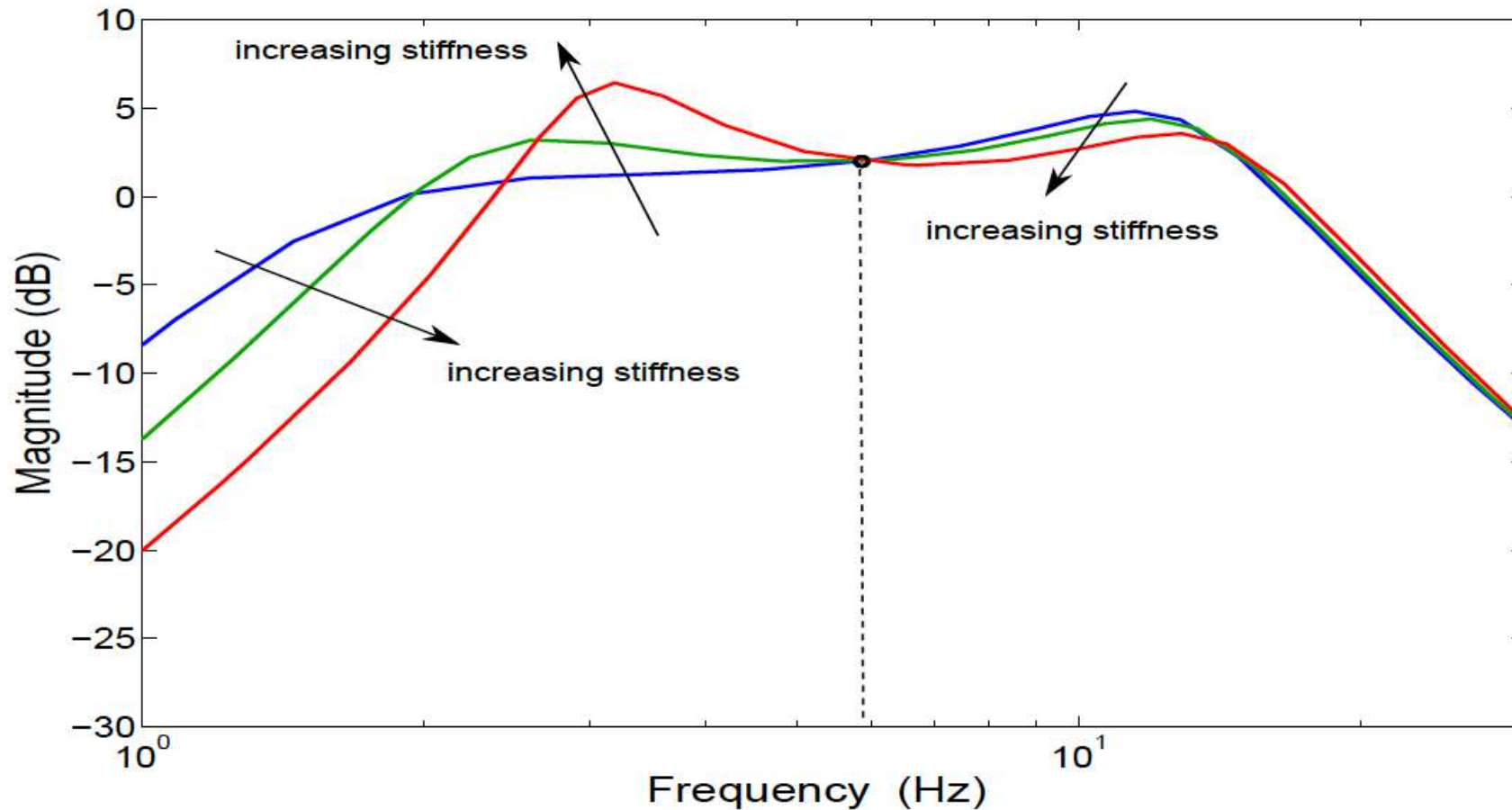


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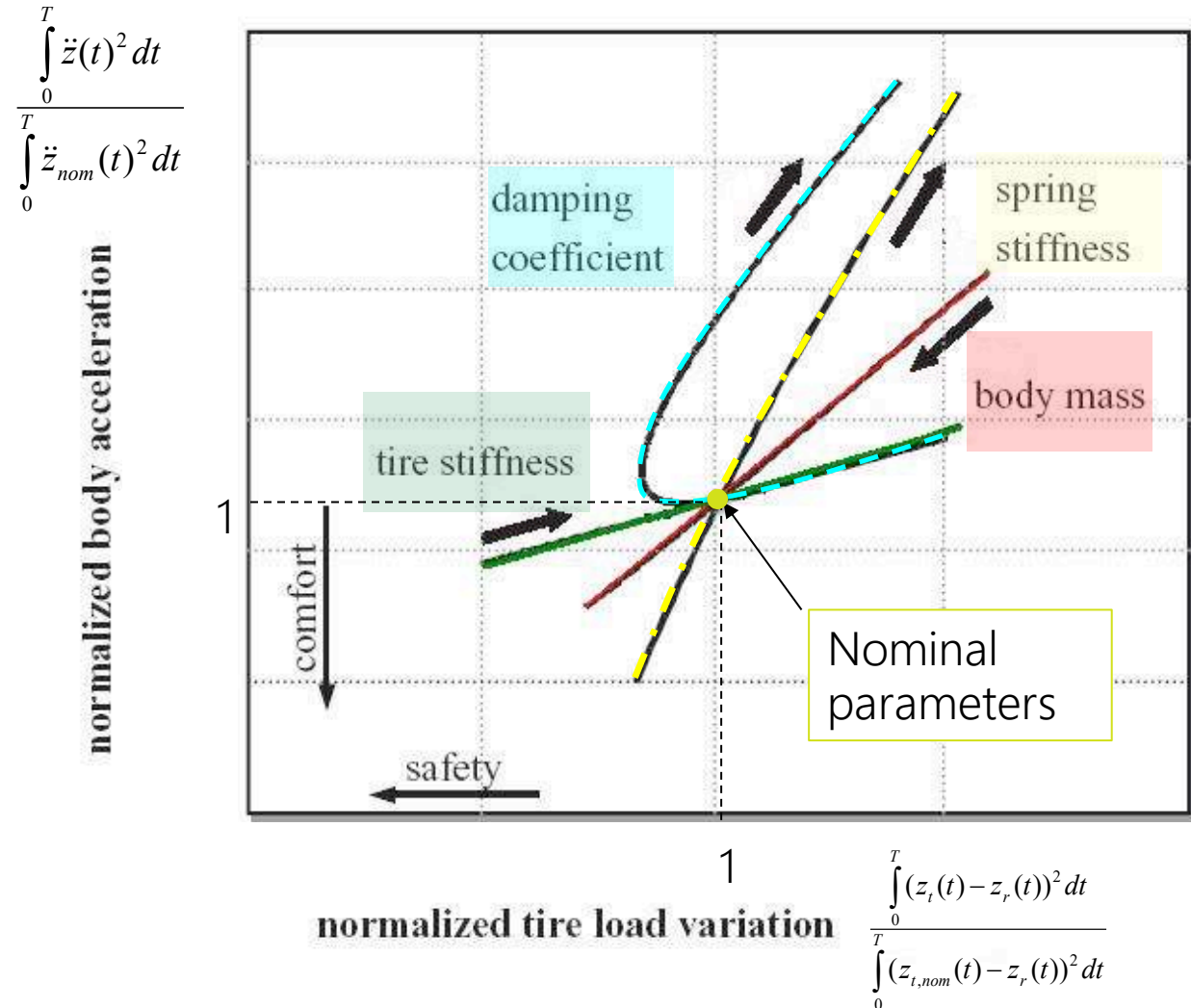
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Semi-Active Damping Control

The quarter-car model and its features



Consider a specific road profile $z_r(t)$ over a time-window 0-T as «standard» input for the comparison

The experiment is made with all the parameters at their «nominal» value is the (1,1) position

Each point on the trade-off map is obtained by changing a parameter (one only)

Comment on:

- Body mass
- Spring stiffness
- Tire stiffness

Semi-Active Damping Control

The quarter-car model and its features

Recall that the three objectives are:

$$F_{acceleration}(s)Z_r(s) = s^2Z(s)$$

$$F_{stroke}(s)Z_r(s) = Z(s) - Z_t(s)$$

$$F_{load}(s)Z_r(s) = (K_t/m)(Z_t(s) - Z_r(s))$$

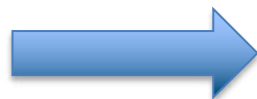
three objectives with apparently only 2 variables ($Z(s)$ and $Z_t(s)$).

→ cannot achieve all three objectives

Given:

Z_r

comfort
handling



it seems possible to design a control law for the suspension force to achieve those objectives

(2 unknowns 2 equations)

Semi-Active Damping Control

The quarter-car model and its features

... not quite true. Assume the ideal case where F can be freely controlled

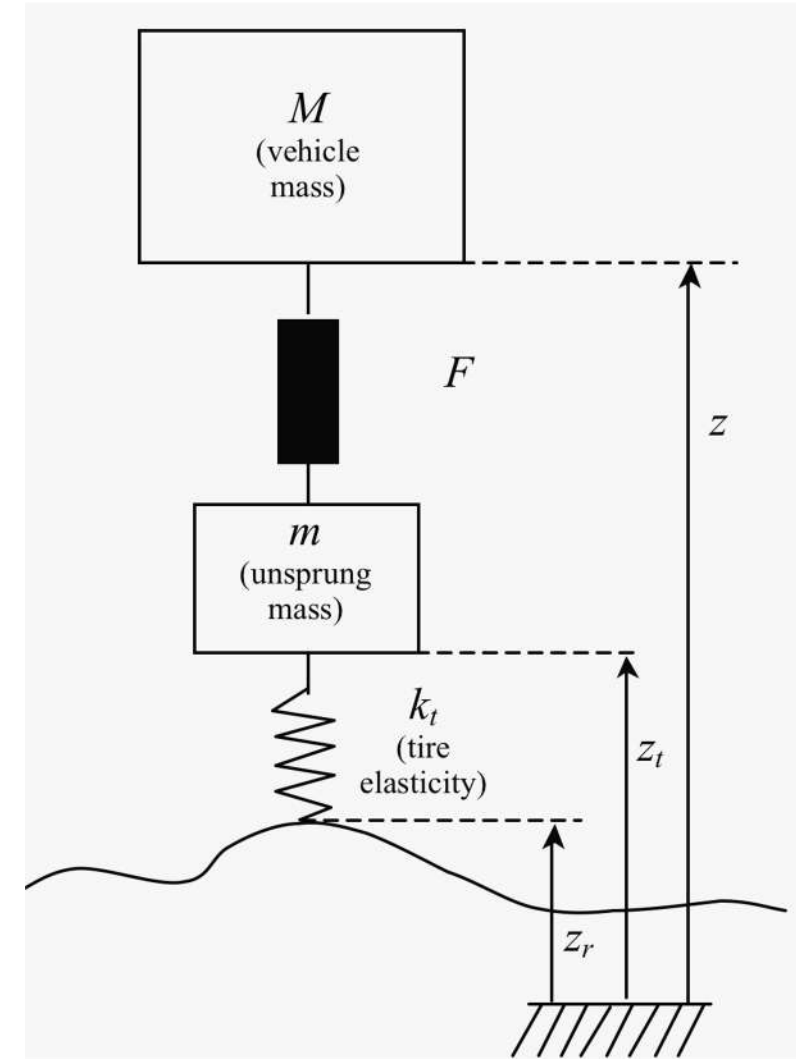
$$\begin{cases} M \delta \ddot{z} = \delta F \\ m \delta \ddot{z}_t = -k_t (\delta z_t - \delta z_r) - \delta F \end{cases}$$

by eliminating δF :

$$Ms^2 Z(s) + ms^2 Z_t(s) + k_t (Z_t(s) - Z_r(s)) = 0$$

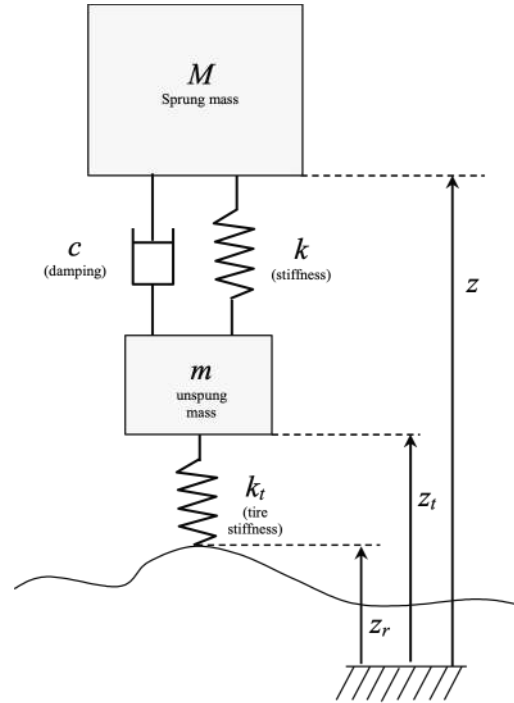
there is an additional dynamic constraint:

The two objectives cannot be independently set



Semi-Active Damping Control

The quarter-car model and its features

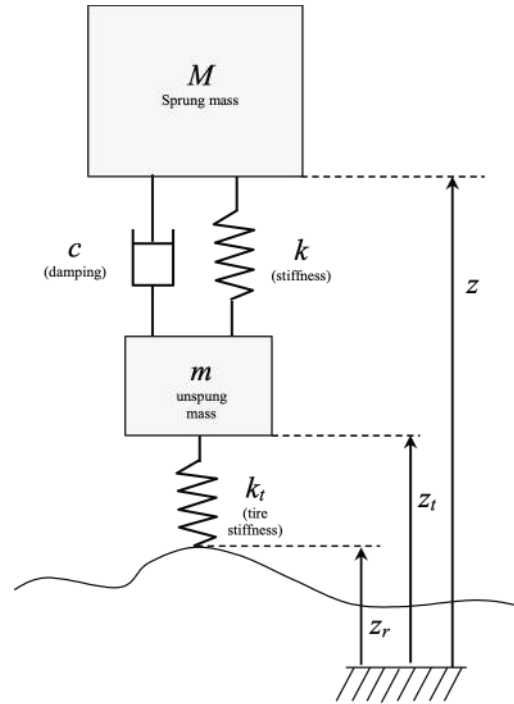


$$x = \begin{bmatrix} z \\ \dot{z} \\ z_t \\ \dot{z}_t \end{bmatrix} \quad u = \begin{bmatrix} z_r \\ c \end{bmatrix} \quad y = \begin{bmatrix} z \\ z_t \end{bmatrix}$$

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Semi-Active Damping Control

The quarter-car model and its features



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If we linearize around an equilibrium point we lose the effect of the damping variation



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$$\begin{cases} M\ddot{z}(t) = -c(\dot{z}(t) - \dot{z}_t(t)) - k(z(t) - z_t(t) - \Delta_s) - Mg \\ m\ddot{z}_t(t) = +c(\dot{z}(t) - \dot{z}_t(t)) + k(z(t) - z_t(t) - \Delta_s) - k_t(z_t(t) - z_r(t) - \Delta_t) - mg \end{cases}$$

Semi-Active Damping Control

Actuator Technology – Dynamic Properties

Furthermore, the suspension response is more complex:

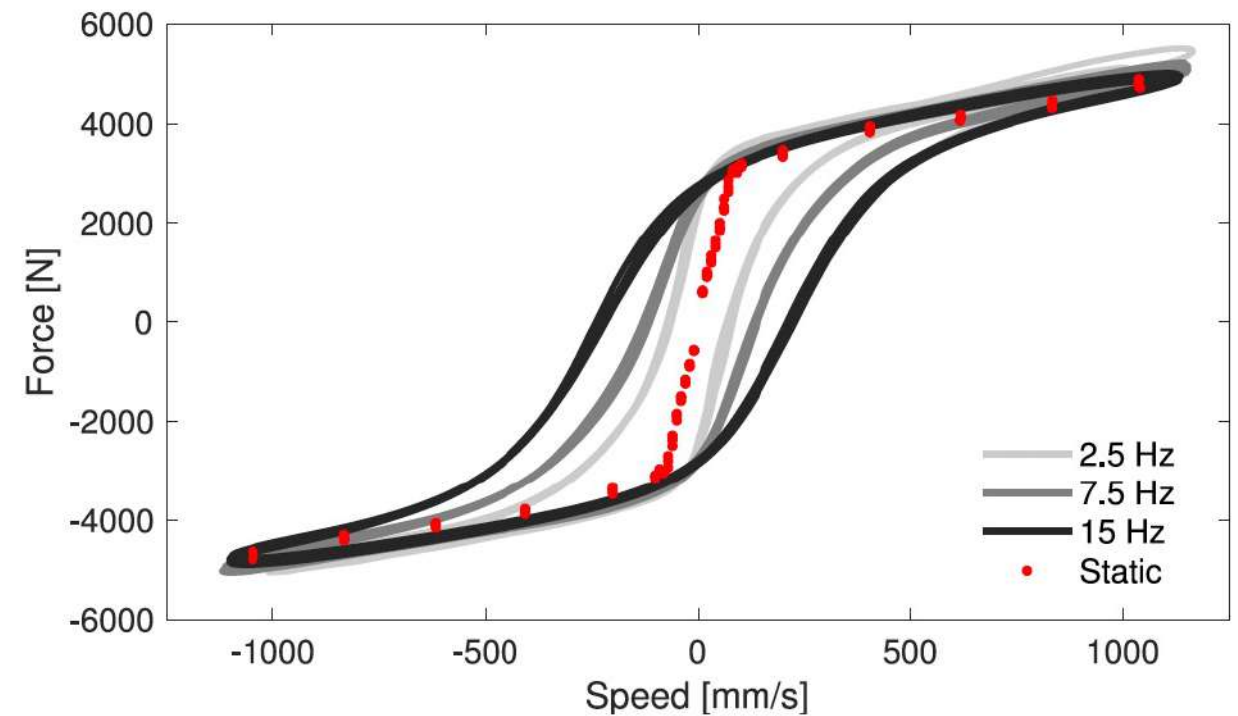
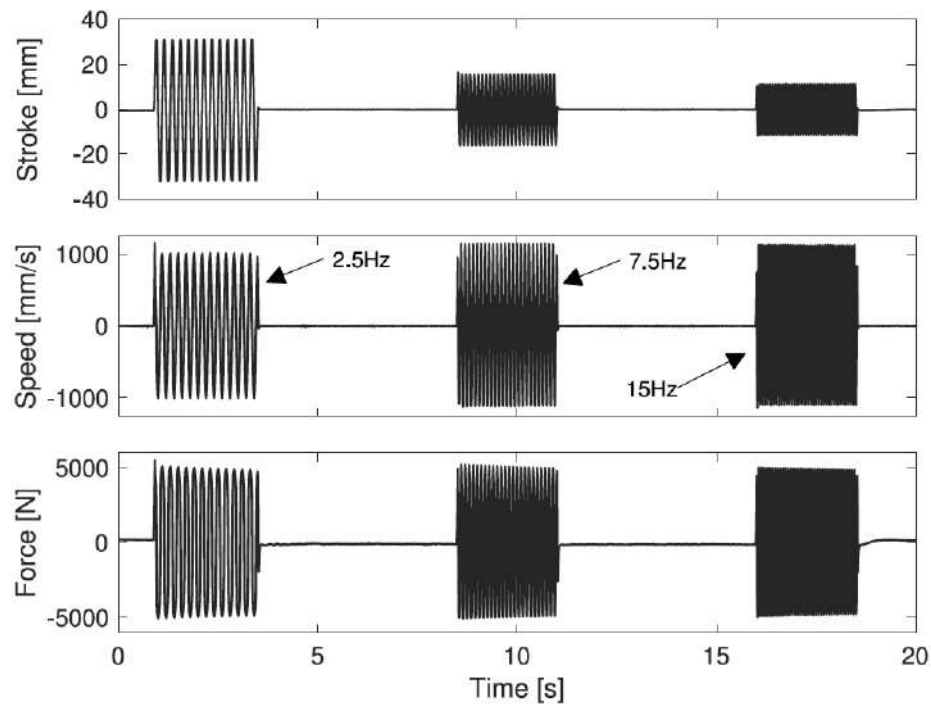
- Hysteresis
- Dynamic response

Semi-Active Damping Control

Actuator Technology – Dynamic Properties

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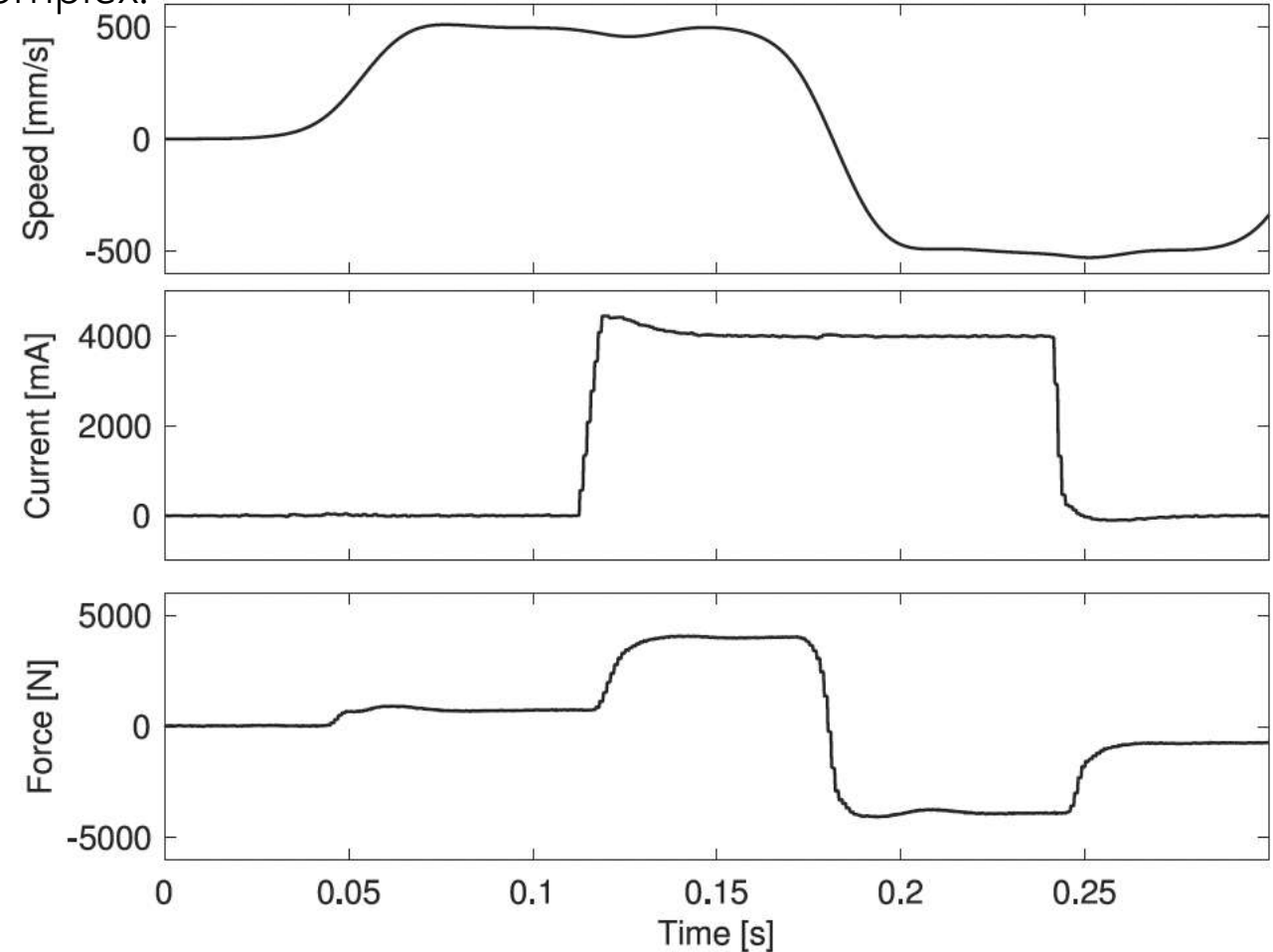


Semi-Active Damping Control

Actuator Technology – Dynamic Properties

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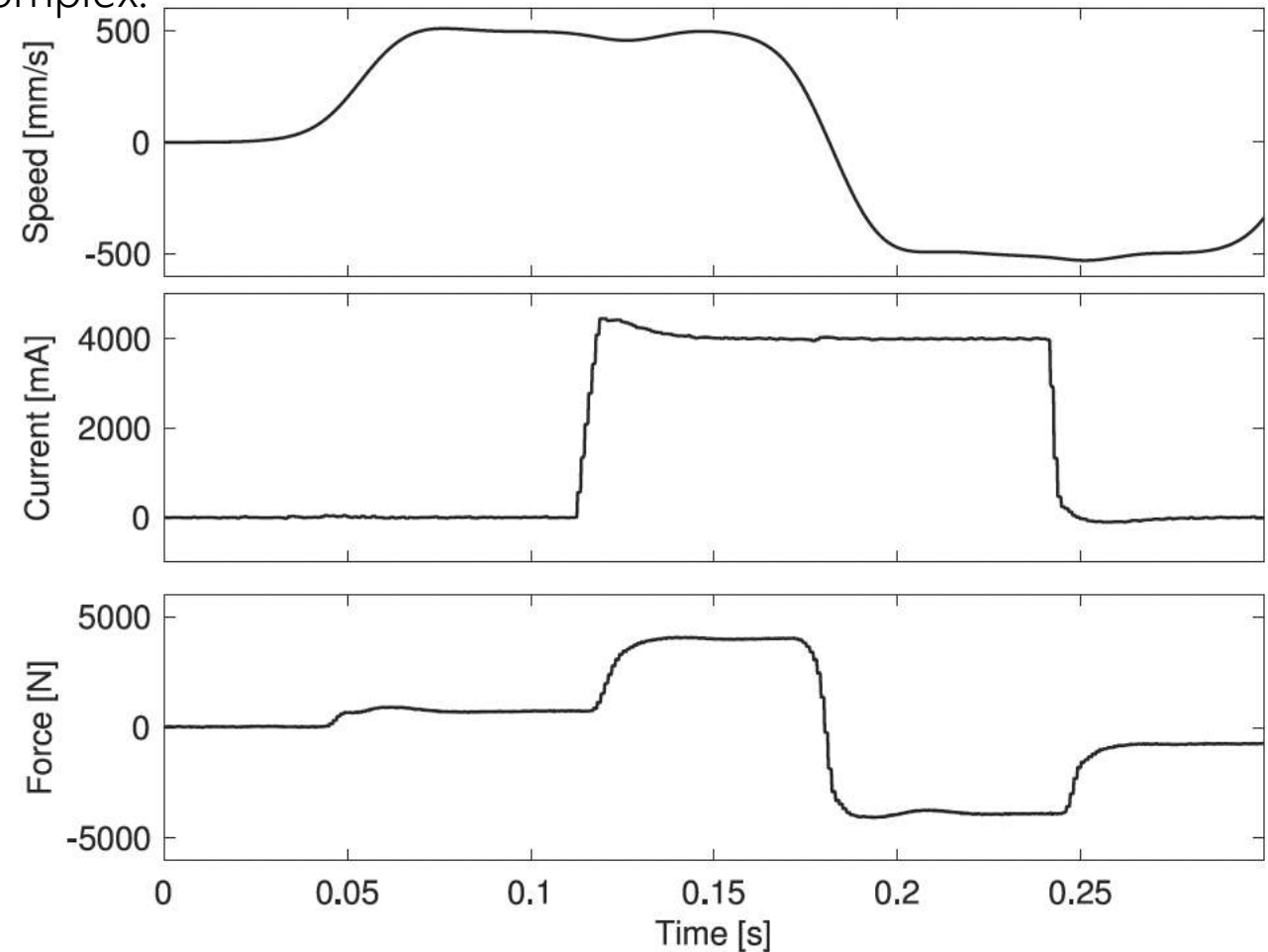


Semi-Active Damping Control

Actuator Technology – Dynamic Properties

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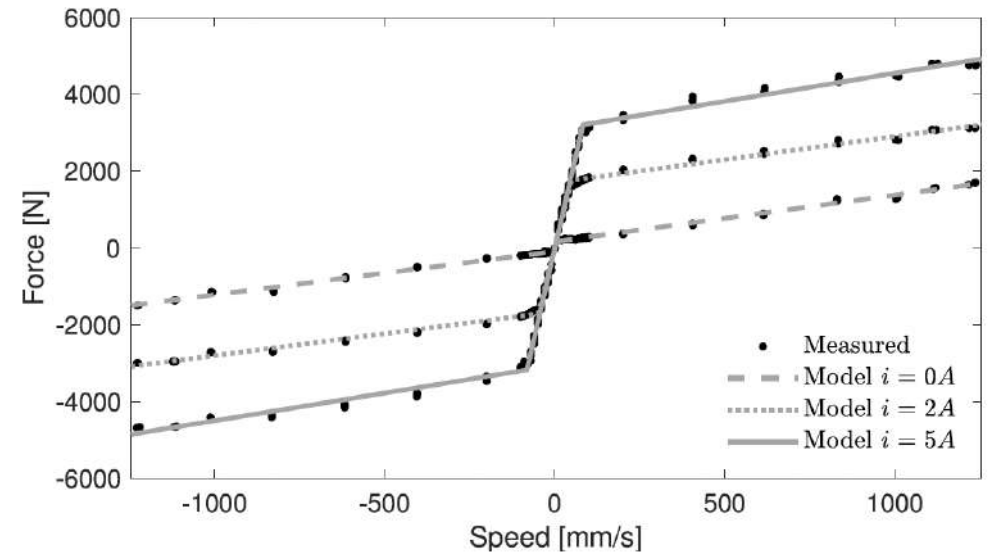
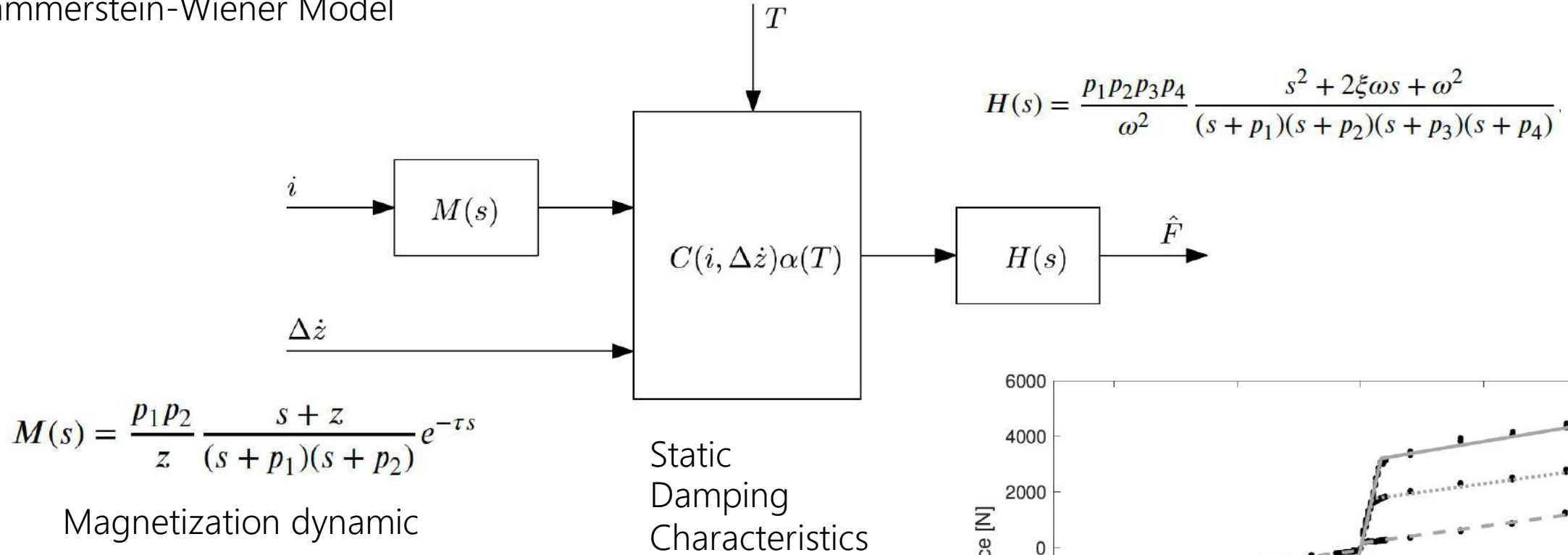
- Hysteresis
- Dynamic response



Semi-Active Damping Control

Actuator Technology – Dynamic Properties

Hammerstein-Wiener Model



Semi-Active Damping Control

Control Oriented Semi-Active Damping Model

$$\Sigma_c(c^0) := \begin{cases} M\ddot{z} &= -k(z - z_t) - c^0(\dot{z} - \dot{z}_t) - F_d \\ m\ddot{z}_t &= k(z - z_t) + c^0(\dot{z} - \dot{z}_t) + F_d - k_t(z_t - z_r) \\ \dot{F}_d &= \beta(u - F_d) \end{cases}$$

Considers a nominal damping

Models the actuator bandwidth

Is the control variable.
We need to add a dissipative constrain

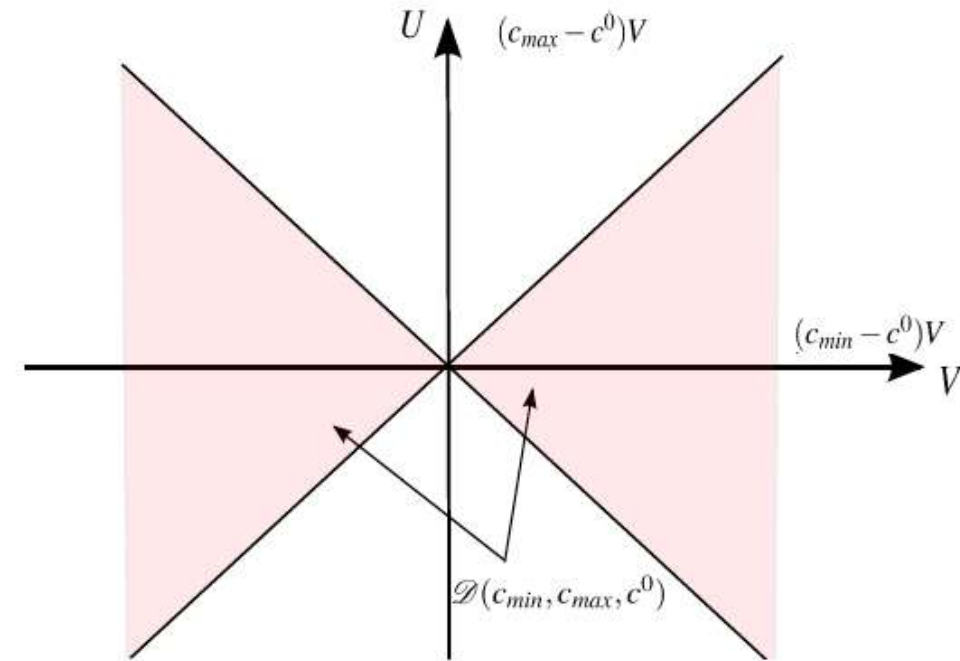
Semi-Active Damping Control

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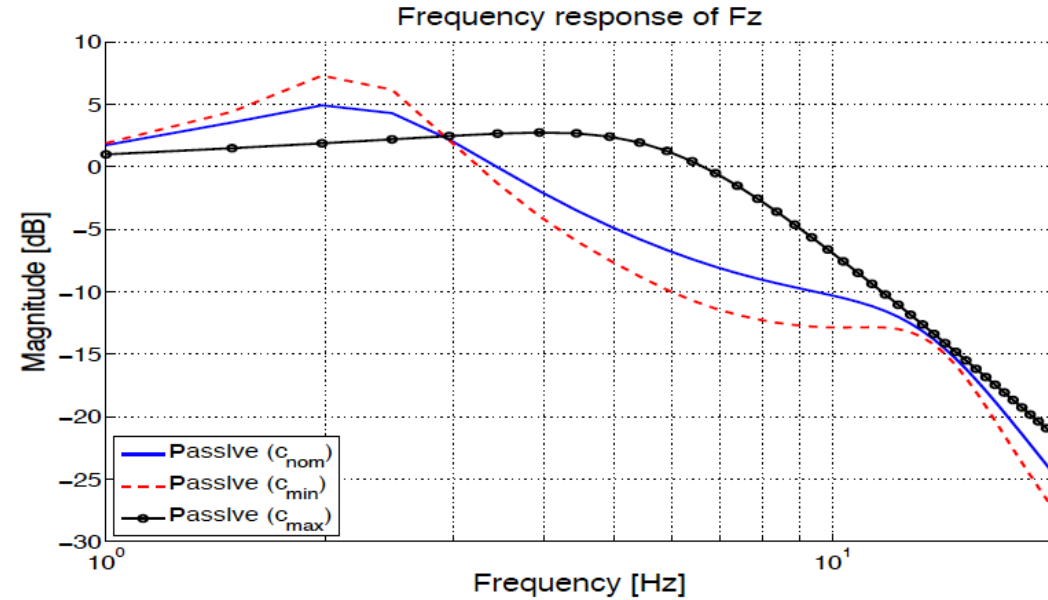
$$u \in \mathcal{D}(c_{min}, c_{max}, c^0) \subseteq \mathbb{R}$$

$$\mathcal{D}(c_{min}, c_{max}, c^0) := \{ \forall (U, V) \in \mathbb{R} \times \mathbb{R} \mid (U - (c_{max} - c^0)V)((c_{min} - c^0)V - U) \geq 0 \}$$



Several ways to assess performance:

- Frequency Response.
 - It requires the knowledge of the input.
 - Work well in simulation.
 - Not applicable in many experimental scenarios
- Integral Performance Index
 - it works experimentally
 - it is a “lumped” approach



$$J = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} |x(t)|^2 dt$$

Semi-Active Damping Control

Road Profile Generation

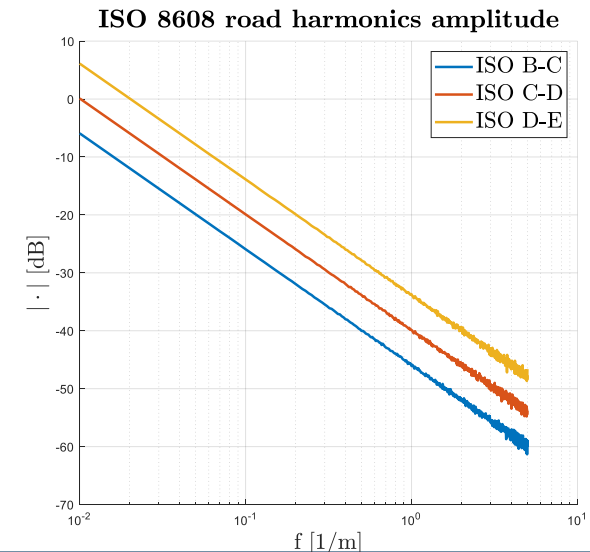
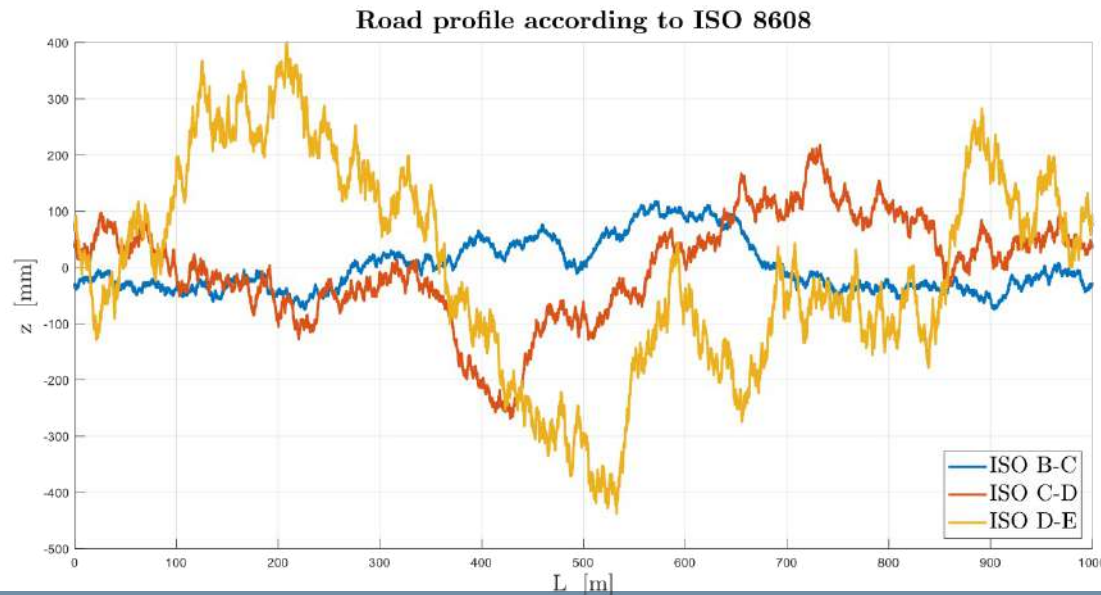
Road classification is made according to **ISO 8608 standard**

Standard road profile can be mathematically modeled **as a sum of sinusoids with decreasing amplitude**

Road profile can be approximated with a **white noise filtered with a very low-frequency 1st order low-pass filter**

$$h(x) = \sum_{i=1}^N \sqrt{\Delta_n} 2^k \cdot 10^{-3} \frac{n_0}{i \Delta_n} \cos(2\pi i \Delta_n x + \phi_i)$$

- k , that allows to build road profiles with different levels of roughness;
- x , that is the longitudinal displacement;
- ϕ_i , that is the phase of each sinusoidal component, randomly chosen to obtain an irregular profile.



Semi-Active Damping Control

Road Profile Generation



Pebble Road A



Cement Road



Belgian Road C1



Pebble Road B



Dislocated Washboard Road C



Belgian Road C2



Long wave road
(Short wavelength)



Long wave road
(Long wavelength)

Semi-Active Damping Control

Road Profile Generation



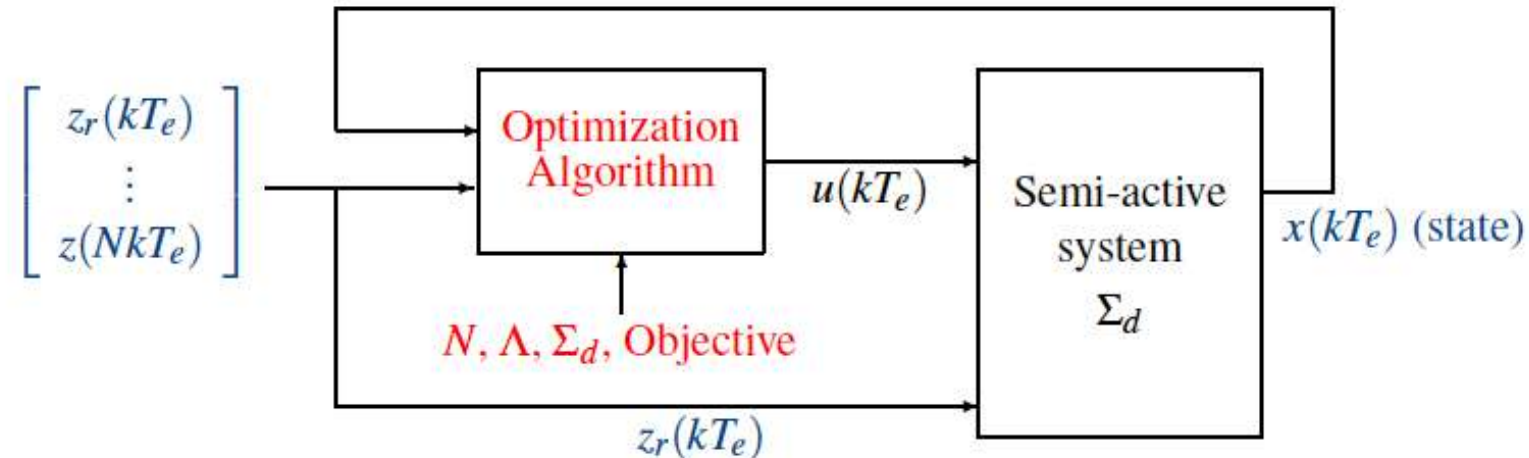
Semi-Active Damping Control

Optimal Control and Benchmarking

It is useful to evaluate the best performance a given system, subject to actuator and inner nested limitations, can achieve

Assumptions:

1. The road disturbance profile is known
2. The state variables of the system are perfectly measured (i.e. no measurement noise).
3. The semi-active quarter car model is known (no system uncertainty).



Semi-Active Damping Control

Optimal Control and Benchmarking

$$J_i^*(N, u, x, z_r) = \min J_\alpha = \alpha J_c(N, u, x, z_r) + (1 - \alpha) J_{rh}(N, u, x, z_r)$$

Subject to

$$\Sigma_d(c^0) : x(k+1) = \left(I_n + A(c^0) \right) T_e x(k) + B T_e \begin{bmatrix} z_r(k) & u(k) \end{bmatrix}^T$$

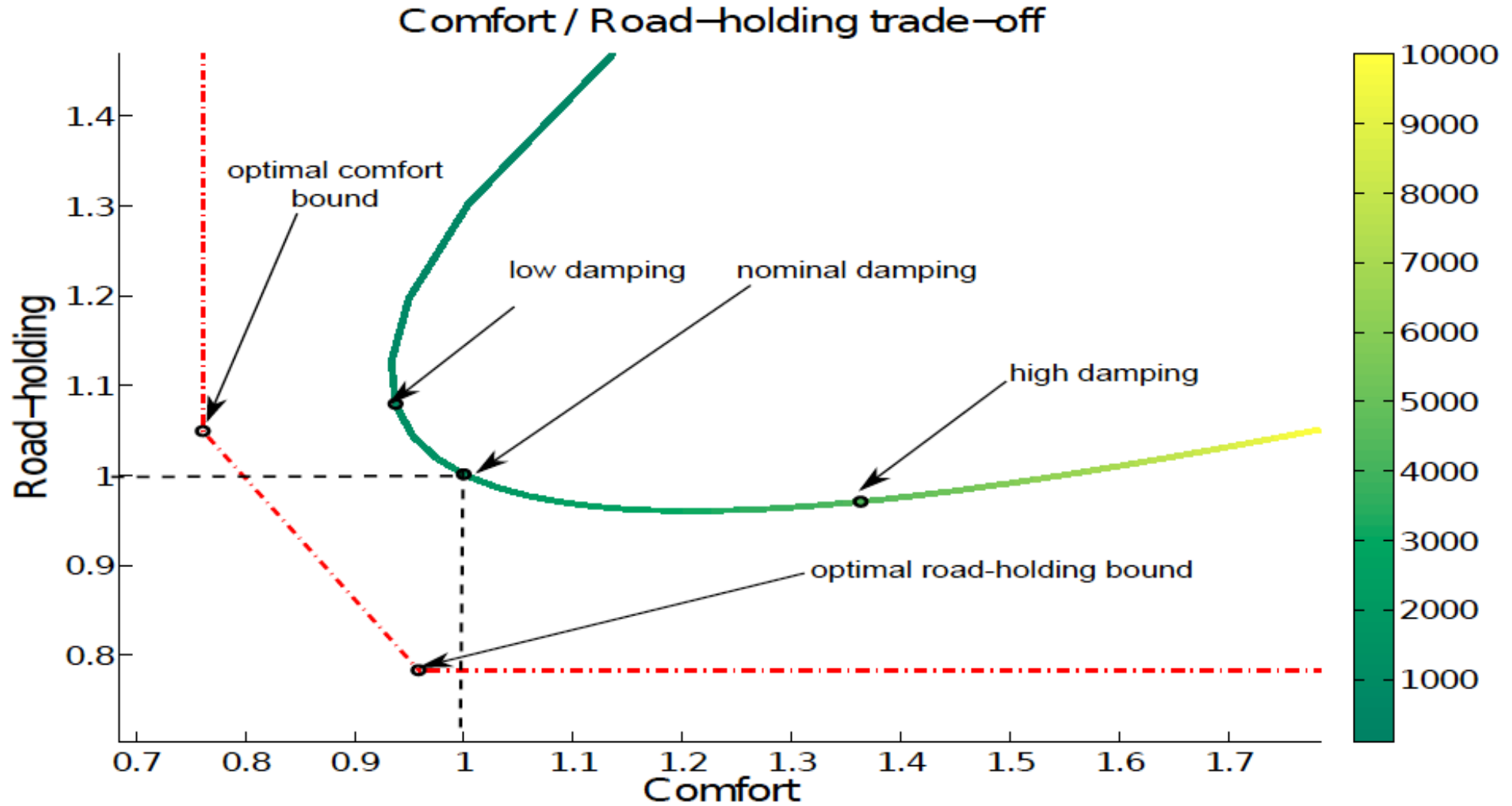
$$\text{if } \dot{z} - \dot{z}_t \geq 0, \Lambda: \begin{cases} u \geq (c_{min} - c^0)(\dot{z} - \dot{z}_t) \\ u \leq (c_{max} - c^0)(\dot{z} - \dot{z}_t) \end{cases}$$

$$\text{if } \dot{z} - \dot{z}_t < 0, \Lambda: \begin{cases} u \leq (c_{min} - c^0)(\dot{z} - \dot{z}_t) \\ u \geq (c_{max} - c^0)(\dot{z} - \dot{z}_t) \end{cases}$$

- It is framed as a nonlinear optimization problem with logical constraints and solved using YALMIP
- α balances the two objective: comfort and road holding
- N is the optimization horizon

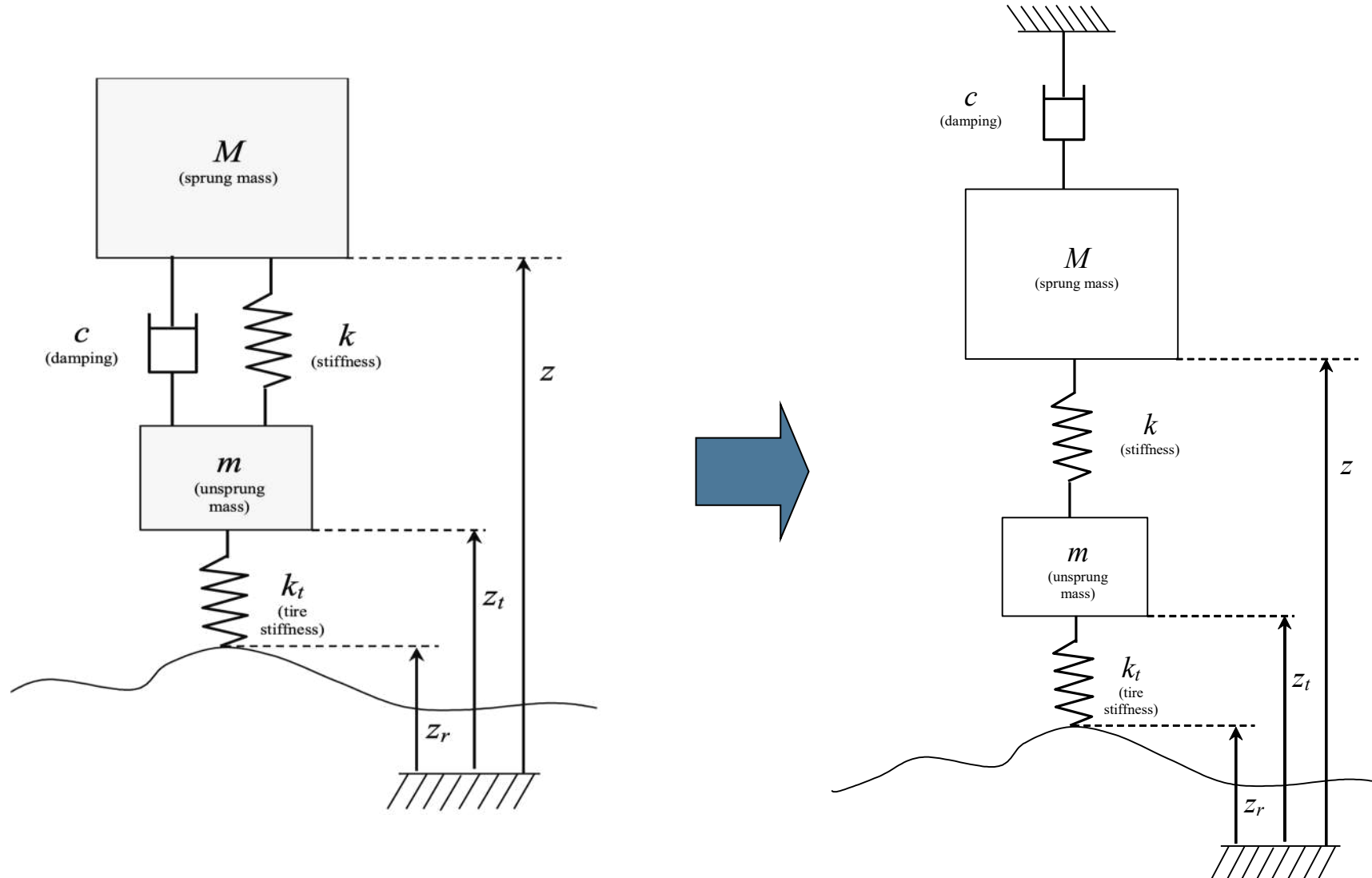
Semi-Active Damping Control

Optimal Control and Benchmarking



Semi-Active Damping Control

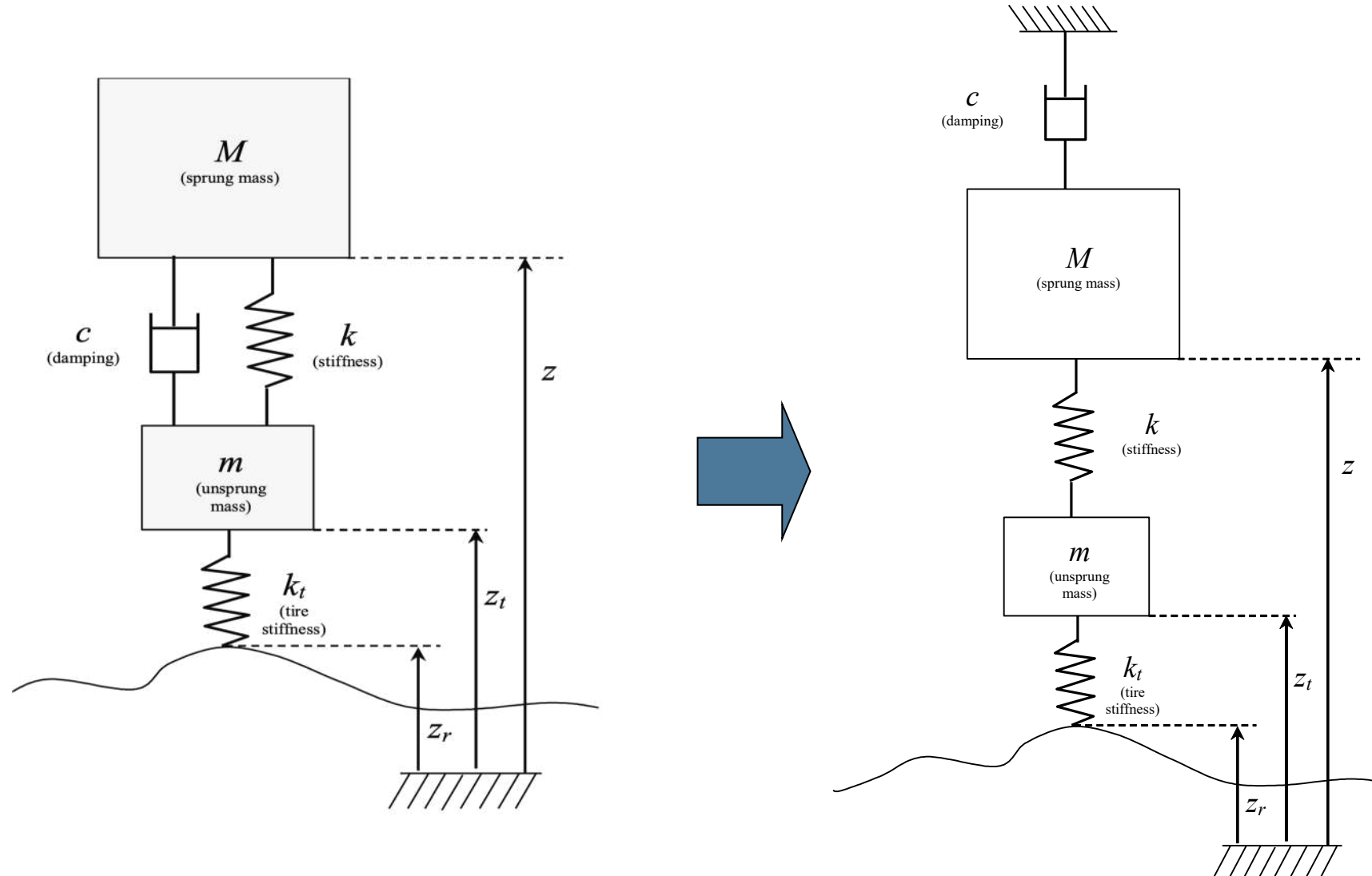
Sky-Hook Concept (Ideal Sky-Hook)



Damping force:
proportional to
body-speed only

Semi-Active Damping Control

Sky-Hook Concept (Ideal Sky-Hook)



Damping force:
proportional to
body-speed only

Semi-Active Damping Control

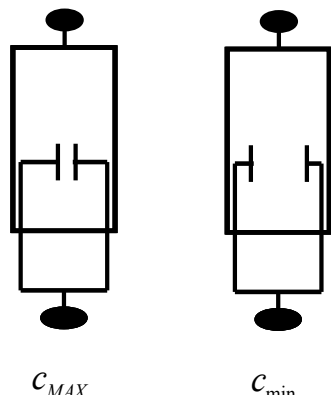
Sky-Hook Concept (Two-State Sky-Hook Control)

$$\begin{cases} c(t) = c_{MAX} & \text{if } \dot{z}(\dot{z} - \dot{z}_t) \geq 0 \\ c(t) = c_{min} & \text{if } \dot{z}(\dot{z} - \dot{z}_t) < 0 \end{cases}$$

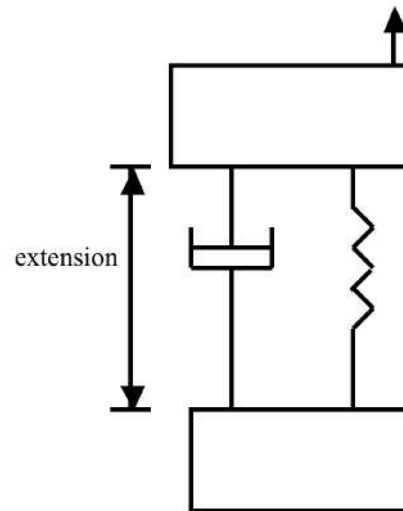
Sensors requirement:

- Body speed
- Stroke speed

Actuator requirement: two-states only, C_{min} and C_{max}



Remark on its intuitive interpretation



if the sprung mass is raising and suspension extending \rightarrow the damper does what we want \rightarrow C_{max}

Semi-Active Damping Control

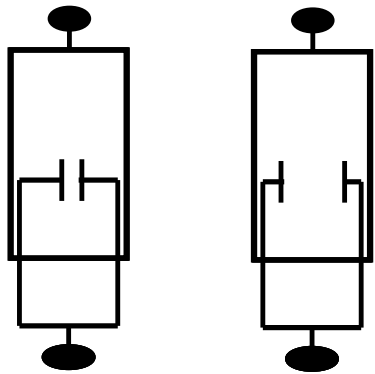
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Sensors requirement:

- Body speed
- Stroke speed

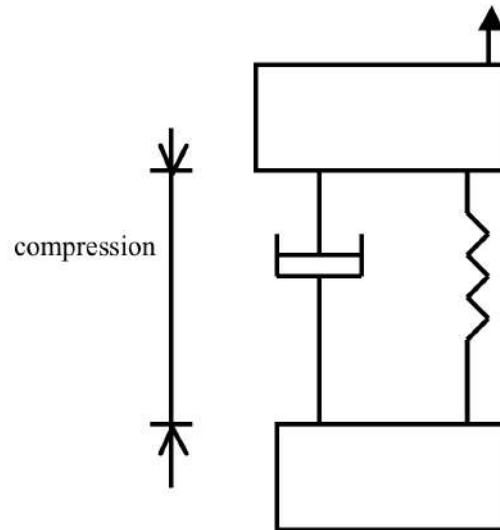
Actuator requirement: two-states only, C_{min} and C_{max}



c_{MAX}

c_{min}

Remark on its intuitive interpretation

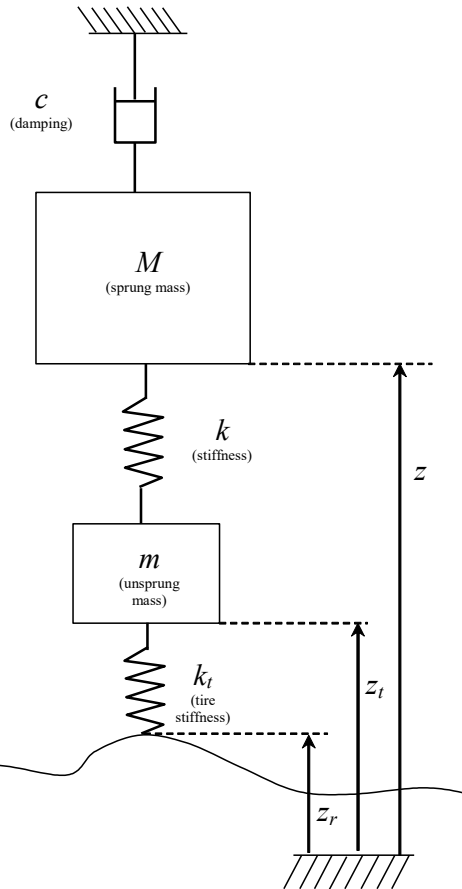


if the sprung mass is raising and suspension compressing \rightarrow the damper is amplifying the sprung mass movement $\rightarrow c_{min}$

Semi-Active Damping Control

Sky-Hook Concept (Classical Linear Sky-Hook Control)

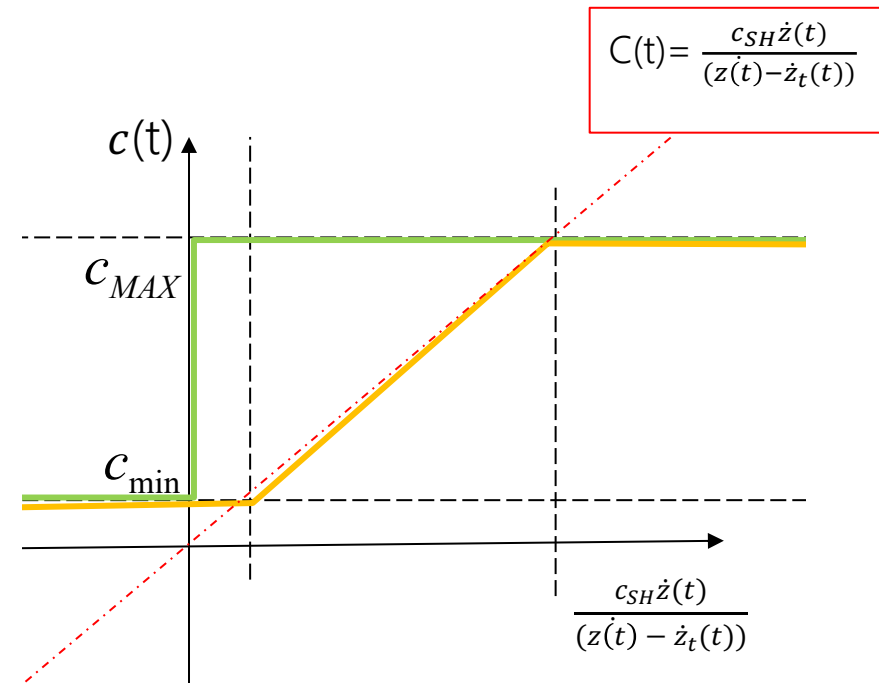
$$-c(t)(\dot{z} - \dot{z}_t) = -c_{SH}\dot{z} \quad \longrightarrow \quad c(t) = \text{sat}_{[c_{min}, c_{max}]} \left\{ \frac{c_{SH}\dot{z}}{(\dot{z} - \dot{z}_t)} \right\}$$



Red: ideal

Green: on-off (simple) approximation

Yellow: linear approximation



Semi-Active Damping Control

Acceleration Driven Damper Control

The two-state SH control law can be applied based on the acceleration:
Acceleration Driven Damper Control

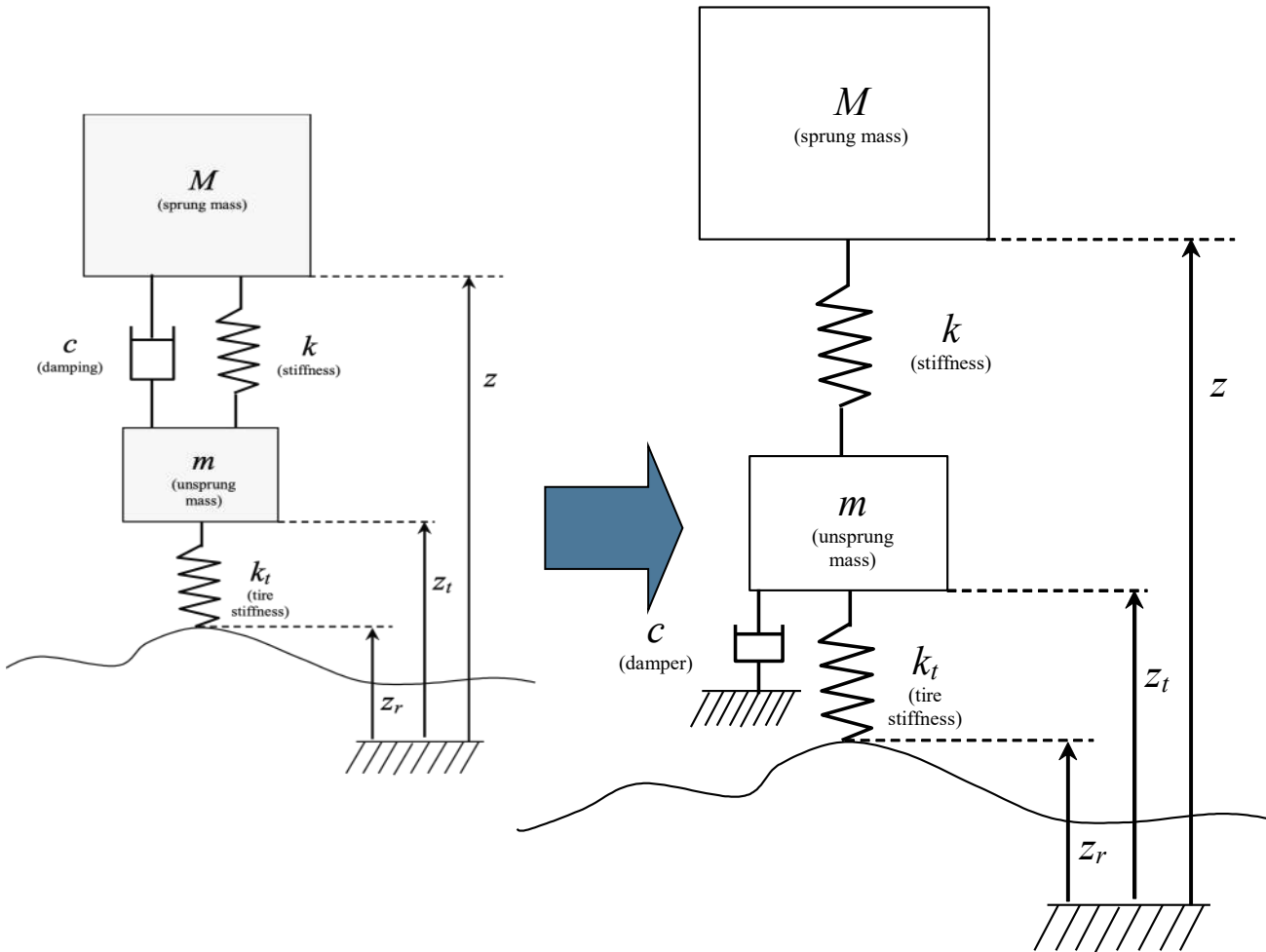
$$\begin{cases} c(t) = c_{MAX} & \text{if } \ddot{z}(\dot{z} - \dot{z}_t) \geq 0 \\ c(t) = c_{min} & \text{if } \ddot{z}(\dot{z} - \dot{z}_t) < 0 \end{cases}$$

It is optimal if the road profile is a white noise.

The switching behavior causes high frequency discomfort.

Semi-Active Damping Control

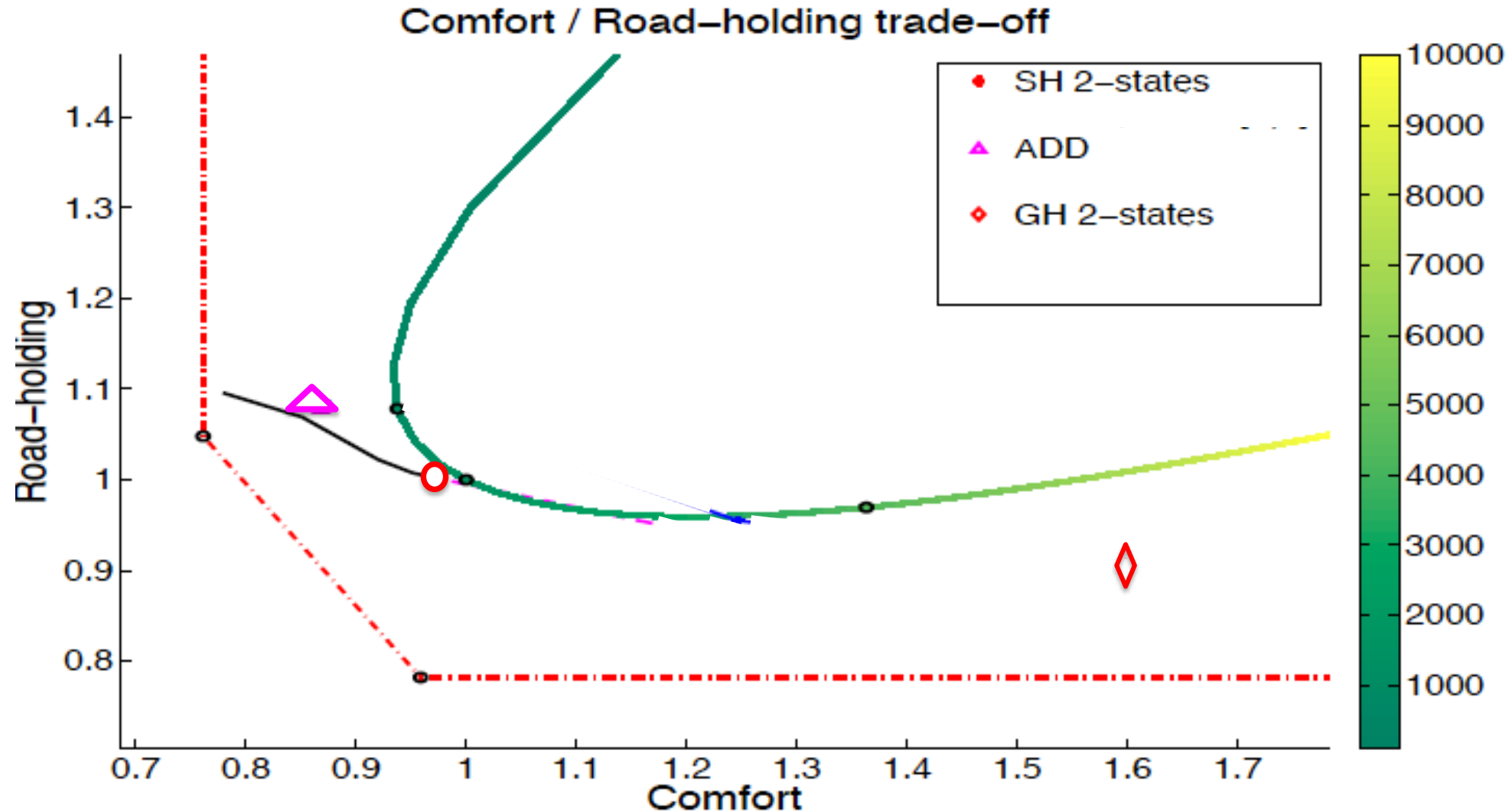
Ground-Hook Concept



$$\begin{cases} c(t) = c_{MAX} & \text{if } -\dot{z}_t(\dot{z} - \dot{z}_t) \geq 0 \\ c(t) = c_{min} & \text{if } -\dot{z}_t(\dot{z} - \dot{z}_t) < 0 \end{cases}$$

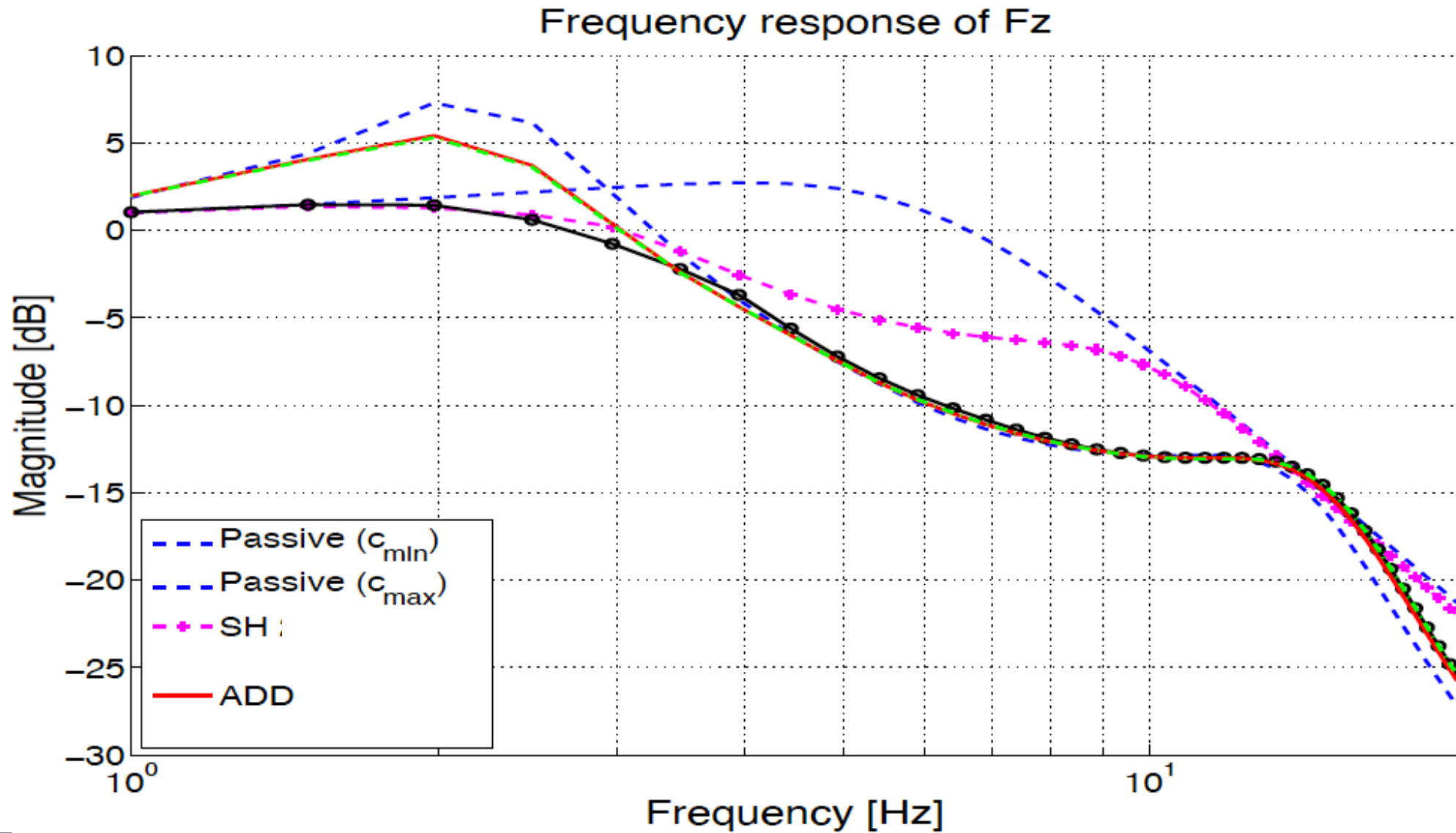
Semi-Active Damping Control

Acceleration Driven Damper Control



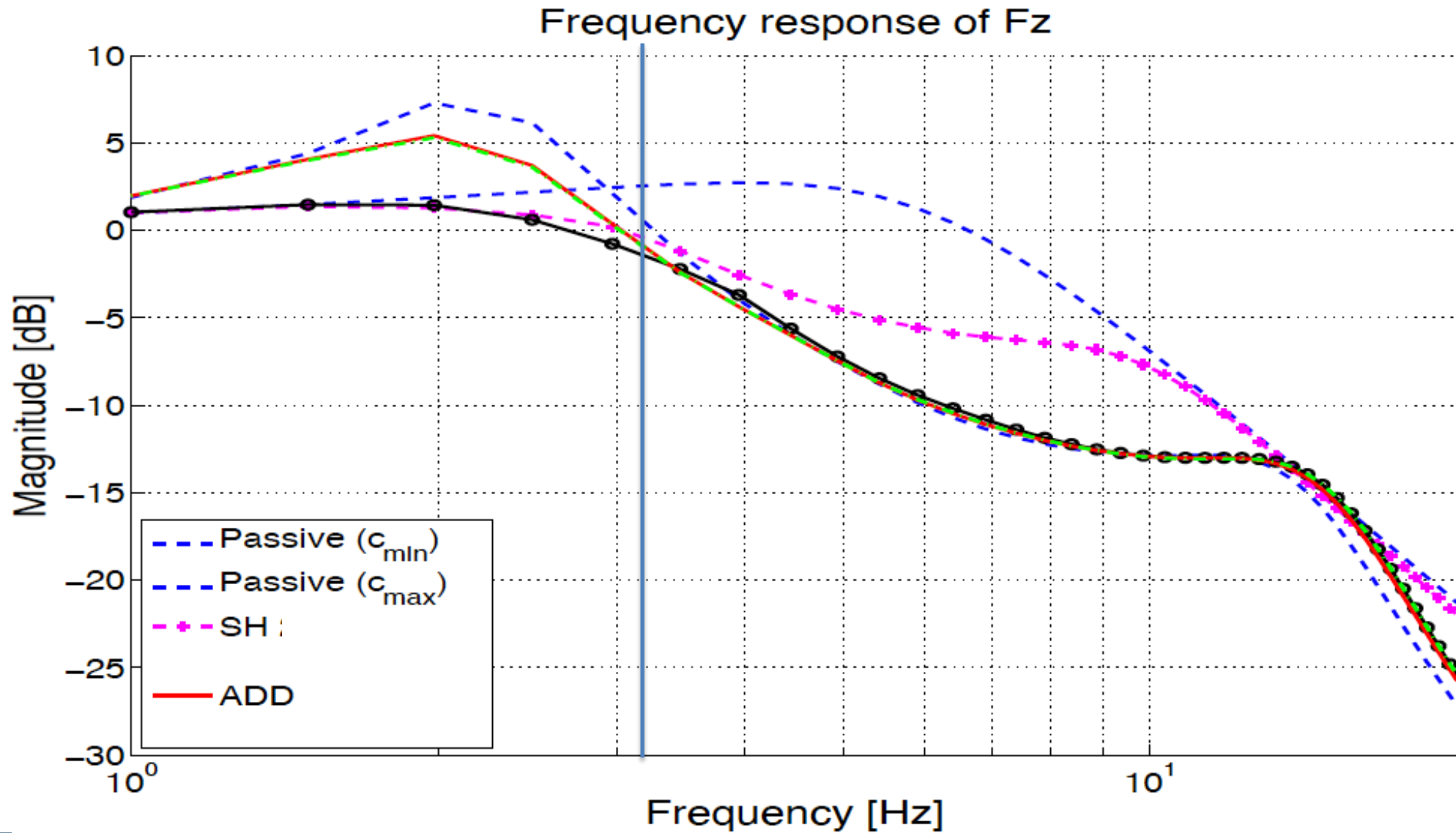
Semi-Active Damping Control

Acceleration Driven Damper Control



Semi-Active Damping Control

Acceleration Driven Damper Control




Semi-Active Damping Control

Mixed SH-ADD Semi-Active Control

Idea: distinguish the instantaneous dynamical behavior of the suspension: in case of low frequency dynamic the SH is selected while the ADD is selected otherwise

$$\begin{cases} c_{in}(t) = c_{\max} & \text{if } \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \quad \wedge \quad \dot{z}(\dot{z} - \dot{z}_t) > 0 \right] \vee \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \quad \wedge \quad \ddot{z}(\dot{z} - \dot{z}_t) > 0 \right] \\ c_{in}(t) = c_{\min} & \text{if } \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \quad \wedge \quad \dot{z}(\dot{z} - \dot{z}_t) \leq 0 \right] \vee \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \quad \wedge \quad \ddot{z}(\dot{z} - \dot{z}_t) \leq 0 \right] \end{cases}$$



Frequency Selector SH ADD

Semi-Active Damping Control

Frequency Range Selector

Consider the single tone $\dot{z}(t) = A \sin(\omega t)$

And the frequency selector $f(t) = \ddot{z}(t)^2 - \alpha^2 \dot{z}(t)^2$

$$f(t) = A^2 \omega^2 - A^2 \sin^2(\omega t) (\alpha^2 \omega^2)$$

We can see that $f(t) > 0 \Rightarrow \sin^2(\omega t) < \frac{\omega^2}{\omega^2 + \alpha^2}$

If we call $D_+(\omega) = \{t : f(t) > 0, 0 \leq t \leq T\}$

$$|D_+(\omega)| = \frac{2T}{\pi} \arcsin \left(\sqrt{\frac{\omega^2}{\omega^2 + \alpha^2}} \right)$$

Semi-Active Damping Control

Frequency Range Selector

$$\frac{|D_+(\omega)|}{T} \rightarrow 0 \text{ if } \omega \ll \alpha$$

$$\frac{|D_+(\omega)|}{T} \rightarrow 1 \text{ if } \omega \gg \alpha$$

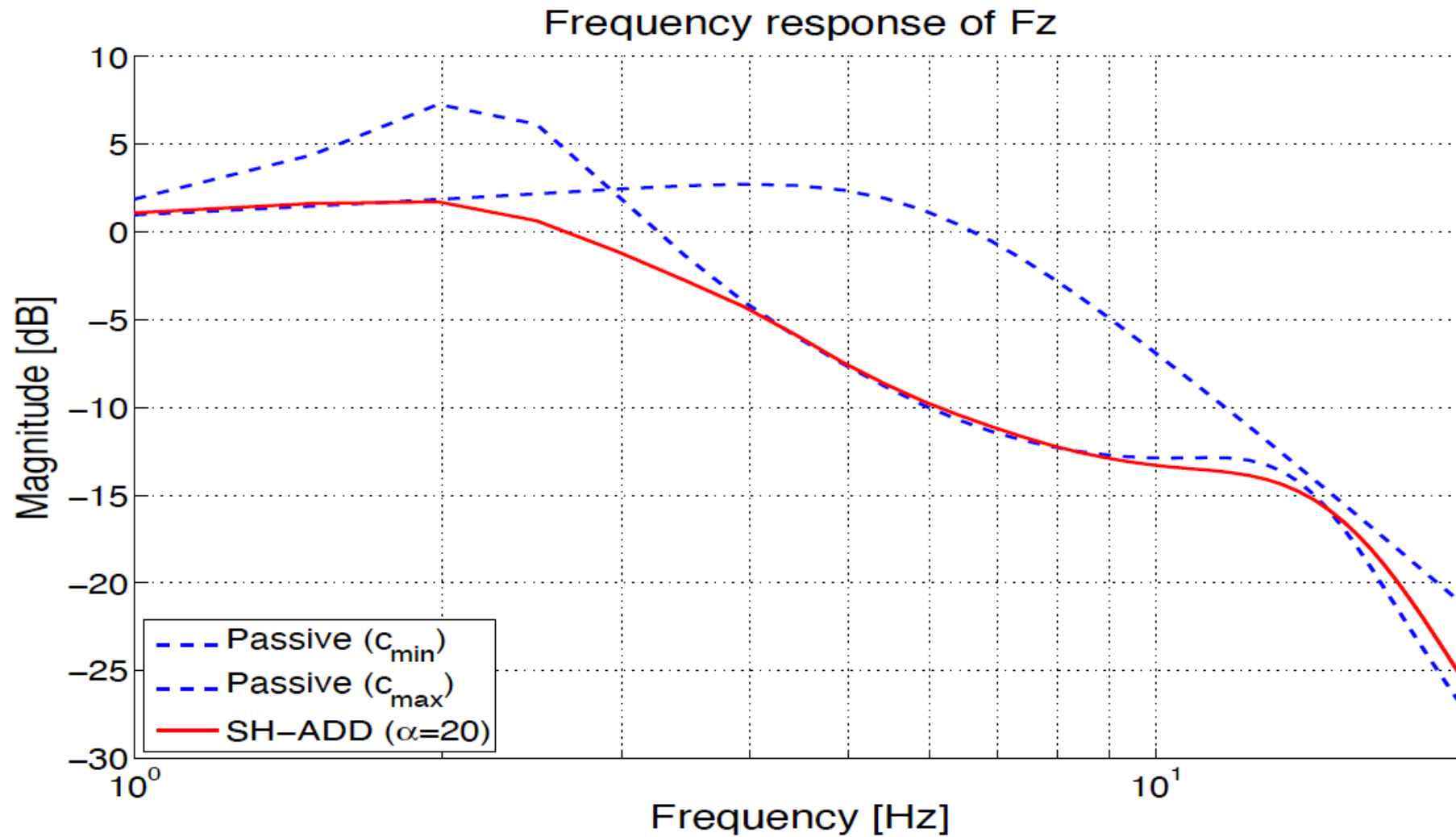
$$\frac{|D_+(\omega)|}{T} = \frac{1}{2} \text{ if } \omega = \alpha$$

Over a period T:

- $f(t) > 0$ for more than $T/2$ if $\omega > \alpha$.
- $f(t) < 0$ for more than $T/2$ if $\omega < \alpha$.

Semi-Active Damping Control

Frequency Range Selector



Semi-Active Damping Control

Single Sensor Mix Algorithm

$$\begin{cases} c_{in}(t) = c_{\max} & \text{if } \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \quad \wedge \quad \dot{z}(\dot{z} - \dot{z}_t) > 0 \right] \vee \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \quad \wedge \quad \ddot{z}(\dot{z} - \dot{z}_t) > 0 \right] \\ c_{in}(t) = c_{\min} & \text{if } \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \quad \wedge \quad \dot{z}(\dot{z} - \dot{z}_t) \leq 0 \right] \vee \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \quad \wedge \quad \ddot{z}(\dot{z} - \dot{z}_t) \leq 0 \right] \end{cases}$$

The mixed SH-ADD control logic requires:

- Stroke velocity
- Corner acceleration and velocity



Two sensors for each corner

- Potentiometer
- Accelerometer



Semi-Active Damping Control

Single Sensor Mix Algorithm

$$\begin{cases} c_{in}(t) = c_{\max} & \text{if } \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \quad \wedge \quad \dot{z}(\dot{z} - \dot{z}_t) > 0 \right] \vee \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \quad \wedge \quad \ddot{z}(\dot{z} - \dot{z}_t) > 0 \right] \\ c_{in}(t) = c_{\min} & \text{if } \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \quad \wedge \quad \dot{z}(\dot{z} - \dot{z}_t) \leq 0 \right] \vee \left[(\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \quad \wedge \quad \ddot{z}(\dot{z} - \dot{z}_t) \leq 0 \right] \end{cases}$$

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Semi-Active Damping Control

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The mixed SH-ADD control logic requires:

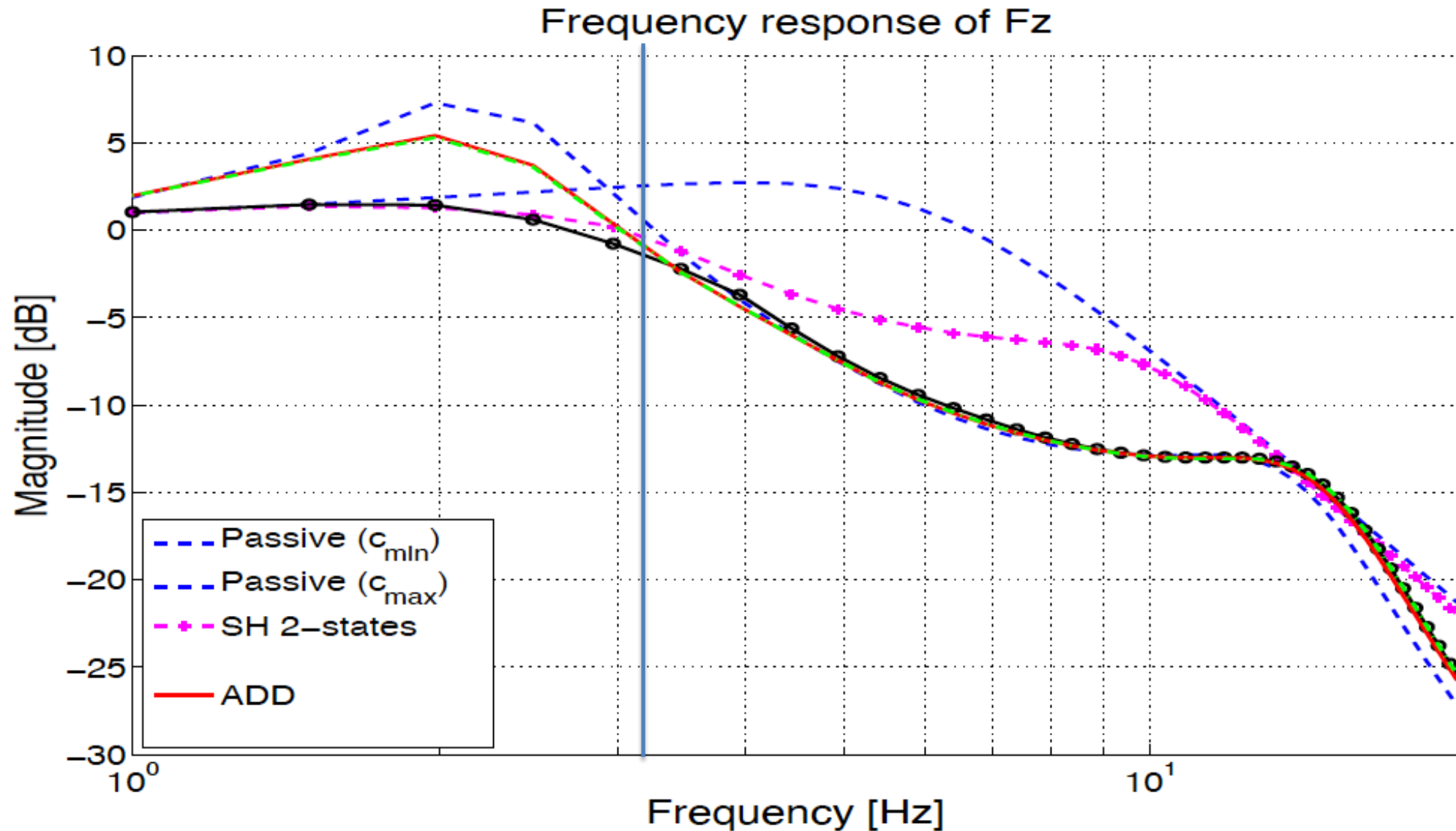
- Stroke velocity
- Corner acceleration and velocity

The frequency selector uses only the accelerometer

→ what happens if we use only the frequency selector?

Semi-Active Damping Control

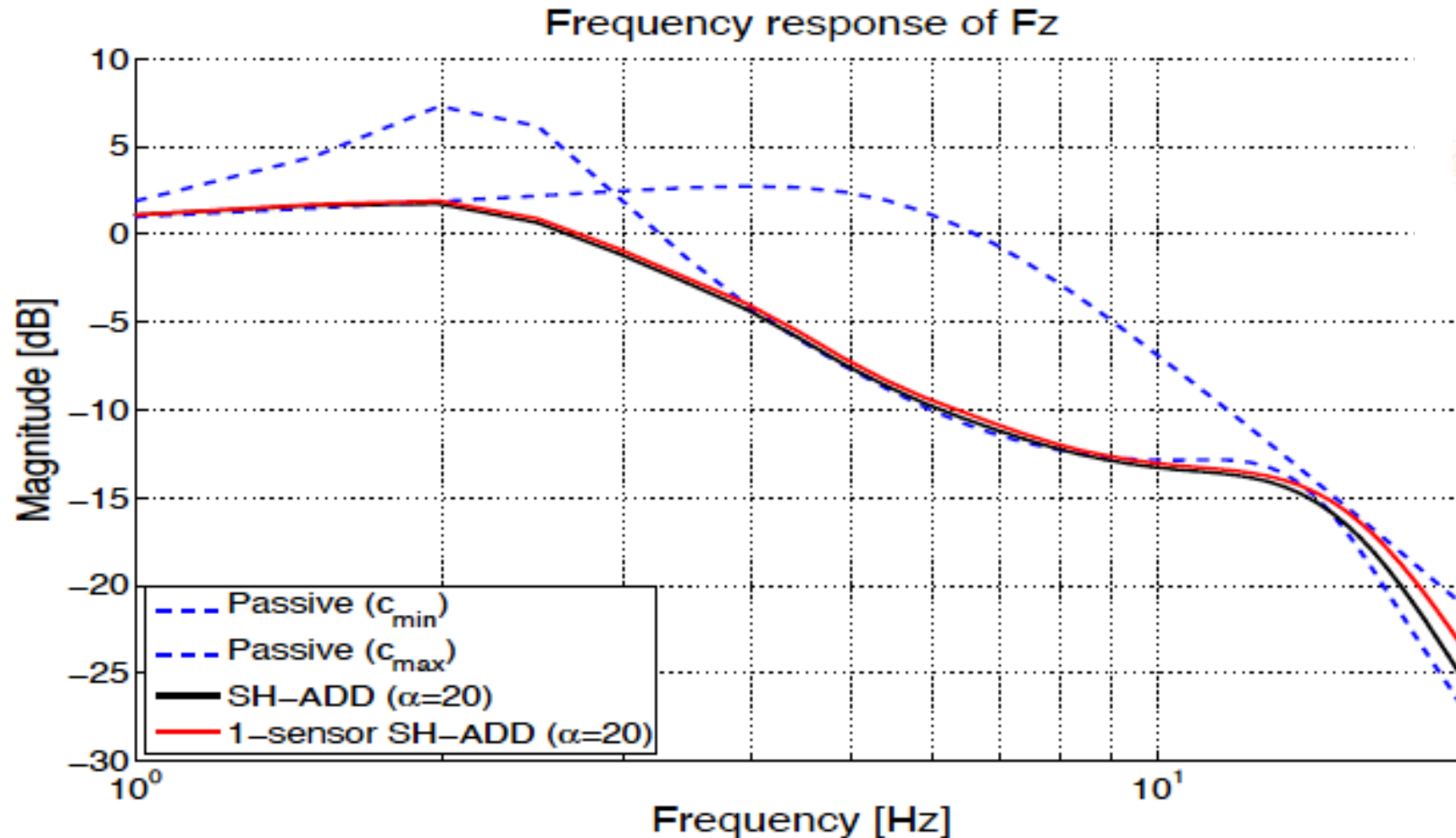
Single Sensor Mix Algorithm



Semi-Active Damping Control

Single Sensor Mix Algorithm

Single sensor Mix Algorithm

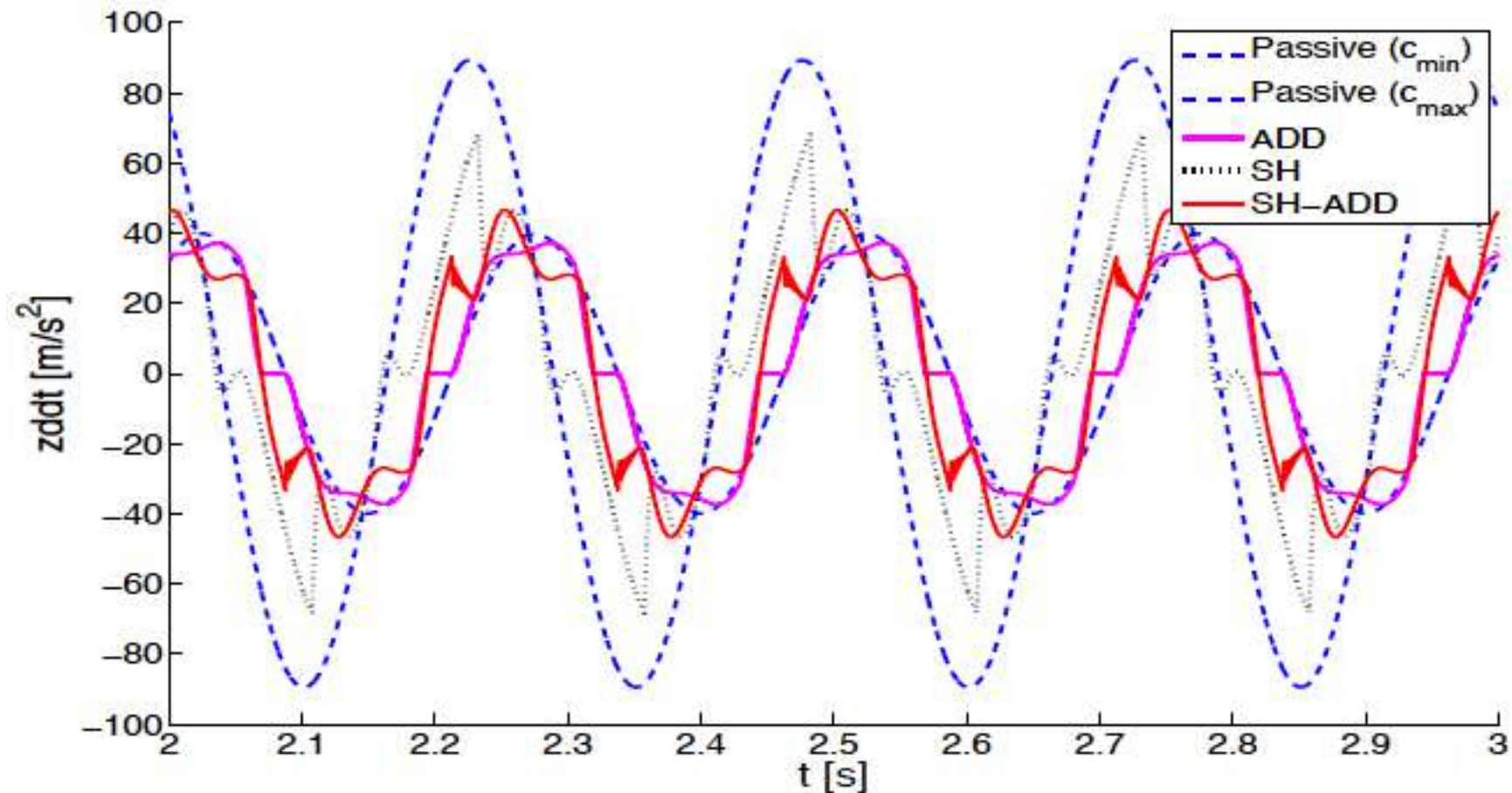


$$c_{in} = \begin{cases} c_{min} & \text{if } (\ddot{z}^2 - \alpha^2 \dot{z}^2) \leq 0 \\ c_{max} & \text{if } (\ddot{z}^2 - \alpha^2 \dot{z}^2) > 0 \end{cases}$$

Semi-Active Damping Control

SH-Mix Algorithm

Both versions of the algorithm are switching algorithms:



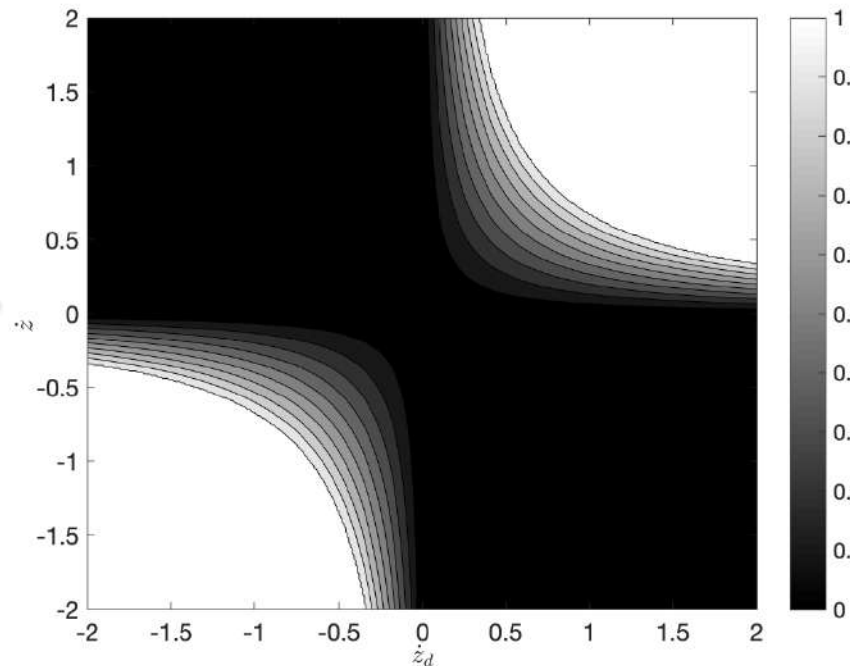
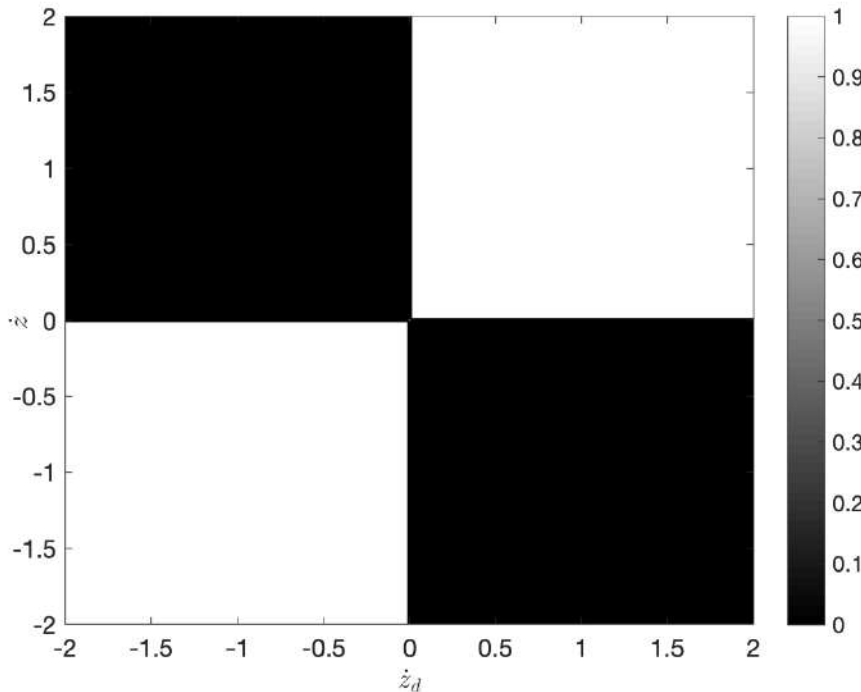
Semi-Active Damping Control

SH-Mix Algorithm

Idea: propose a continuously modulating version of the SH and ADD and combine the two.

Continuously modulating SH:

$$c_{ref} = \underset{c_{ref} \in [c_{min}; c_{max}]}{\text{sat}} (k_{sky} \dot{z} \dot{z}_d + c_{nom})$$



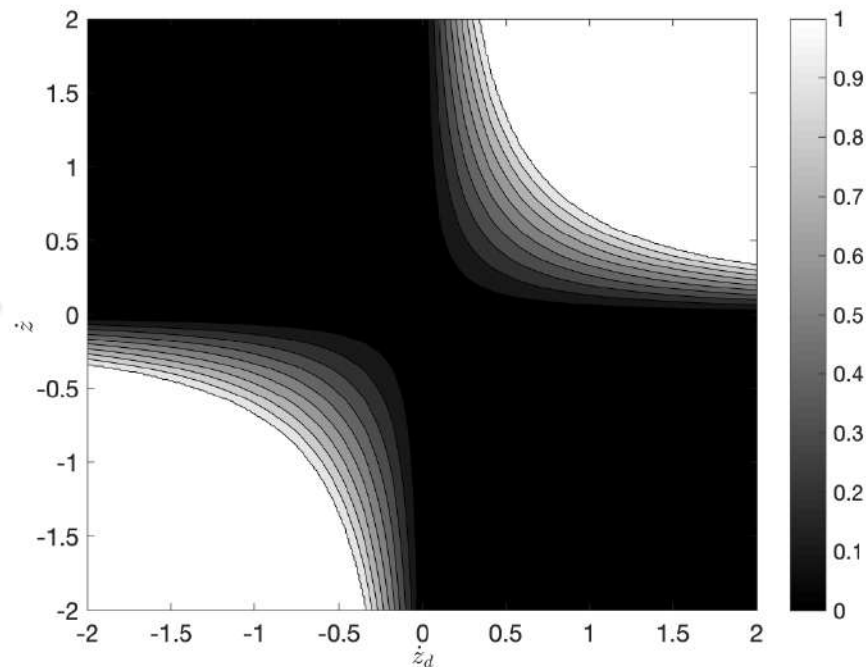
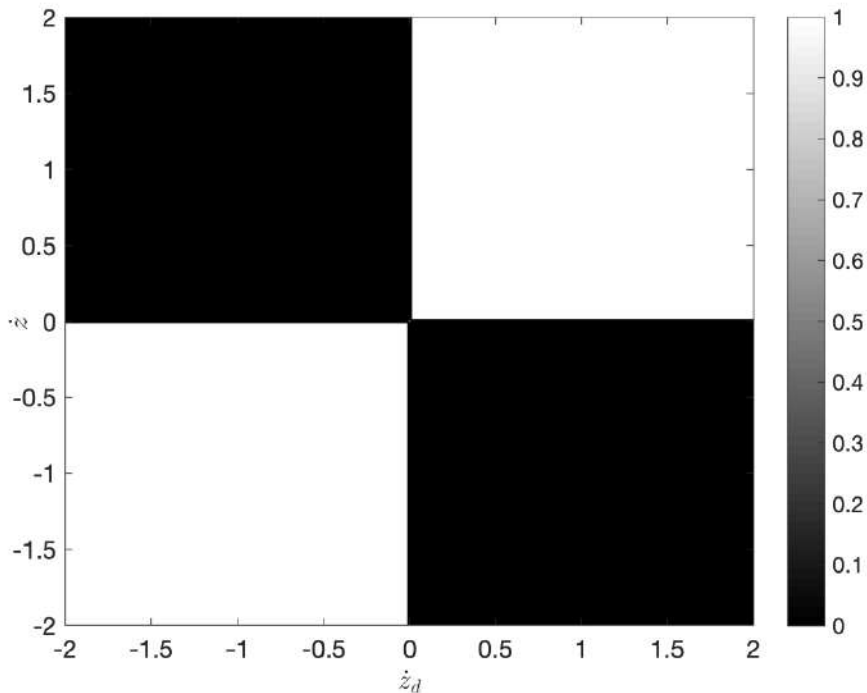
- Smooth
- Easily parametrizable
- It converges to the switching algorithm when k_{sky} increases

Semi-Active Damping Control

SH-Mix Algorithm

Idea: propose a continuously modulating version of the SH and ADD and combine the two.

Continuously modulating ADD: $c_{ref} = sat_{[c_{min}, c_{max}]}(k_{ADD}\ddot{z}_b\Delta\dot{z})$



Idea: propose a continuously modulating version of the SH and ADD and combine the two.

Continuously mixed SH- ADD: $c_{ref} = sat_{[c_{min}, c_{max}]}(c_{nom} + k_{SH}\dot{z}_b\Delta z + k_{ADD}\ddot{z}_b\Delta\dot{z})$

Semi-Active Damping Control

SH-Mix Algorithm

Idea: propose a continuously modulating version of the SH and ADD and combine the two.

Continuously mixed SH- ADD: $c_{ref} = sat_{[c_{min},c_{max}]}(c_{nom} + k_{SH}\dot{z}_b\Delta z + k_{ADD}\ddot{z}_b\Delta\dot{z})$

We can extend the approach to the single-sensor philosophy

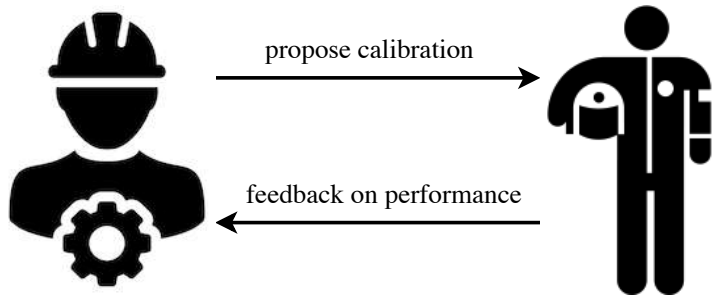
$$\begin{cases} c_{ref} = c_{min}, & \text{if } (\ddot{z}_b^2 - \alpha^2\dot{z}_b^2) \leq 0 \\ c_{ref} = c_{max}, & \text{if } (\ddot{z}_b^2 - \alpha^2\dot{z}_b^2) > 0 \end{cases} \quad \Rightarrow \quad c_{ref} = sat_{[c_{min},c_{max}]}(k_{M1S}|sat_{[-\infty,0]}(\ddot{z}_b^2 - \alpha^2\dot{z}_b^2)|)$$

- Continuously increase the damping at low frequency.
- Keep minimum damping at high frequency.

Semi-Active Damping Control

Calibration

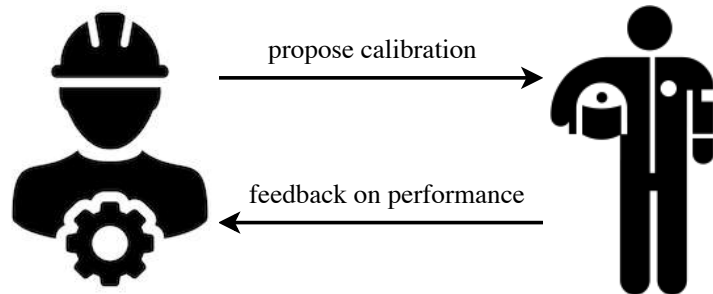
(A) traditional calibration



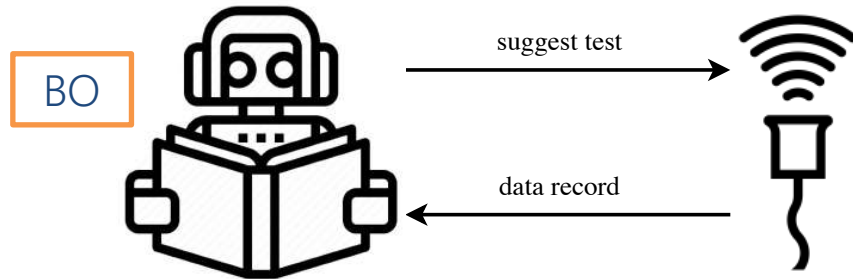
Semi-Active Damping Control

Calibration

(A) traditional calibration

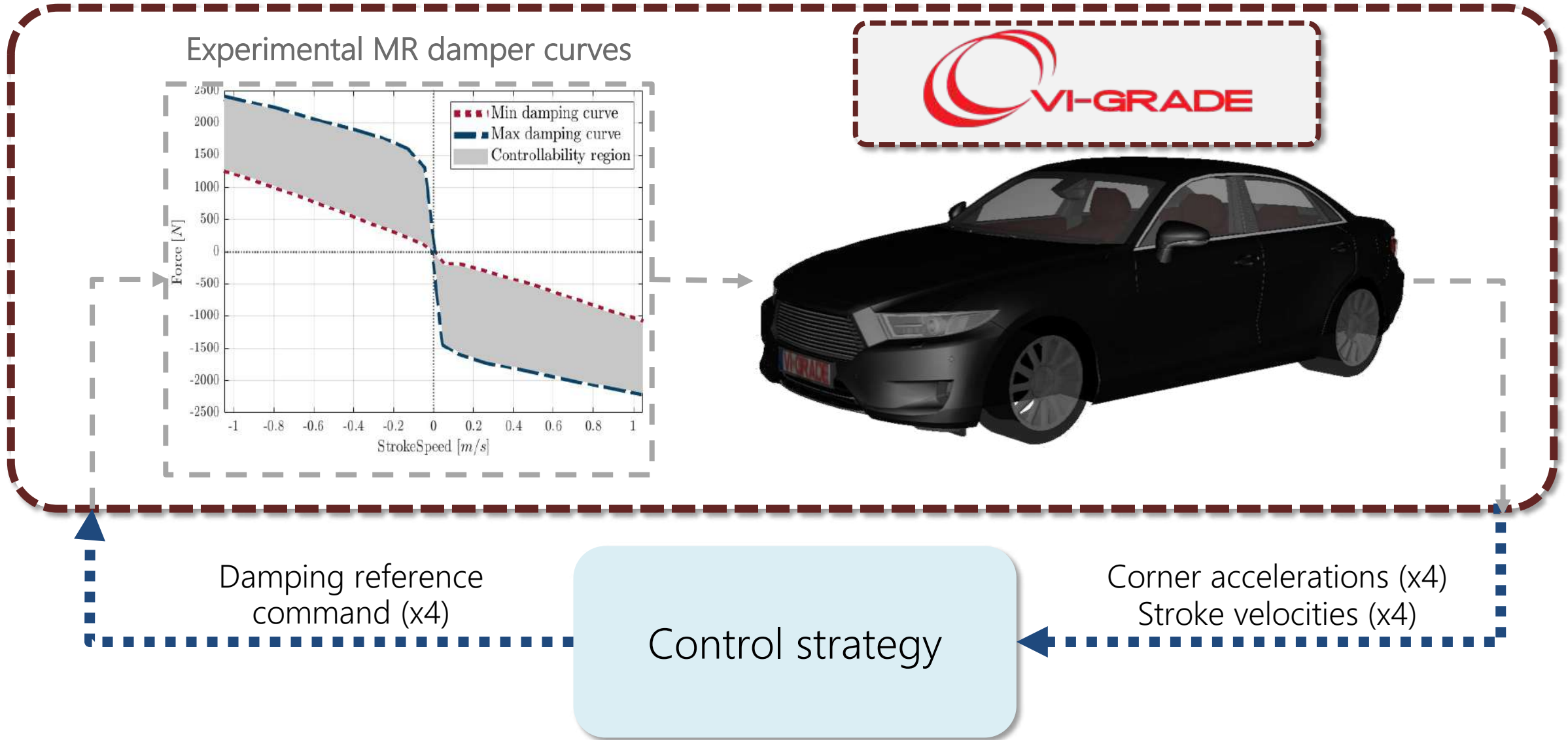


(B) automatic performance-based paradigm



Semi-Active Damping Control

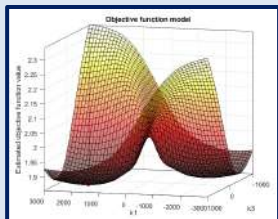
Calibration



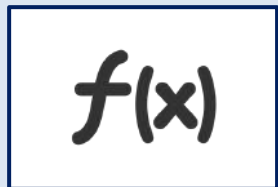
Bayesian Optimization

Data-driven optimization technique suitable for **cost-to-evaluate objective function**.

At each optimization step:



Objective function is modeled as a realization of a Gaussian Process

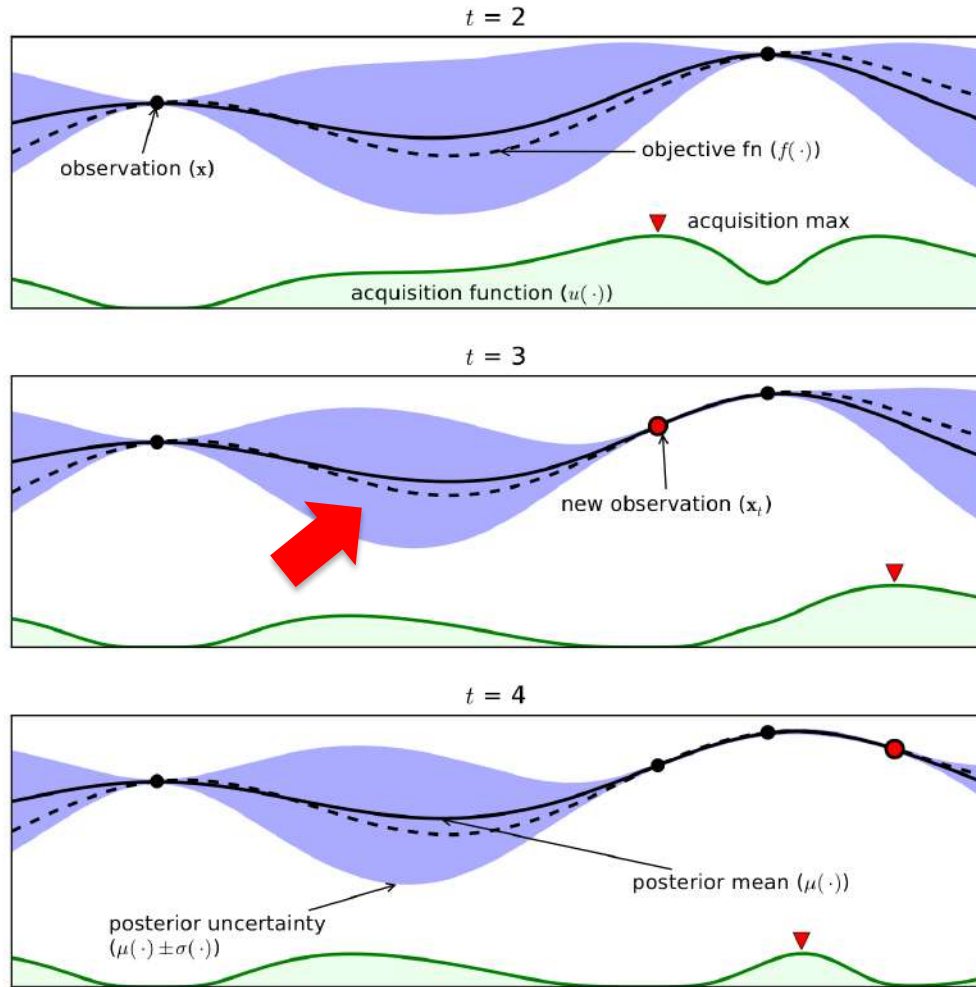


An **acquisition function** determines where to sample the parameters space next.

Frazier, P.I. (2018). A tutorial on bayesian optimization. arXiv preprint arXiv:1807.02811.

Semi-Active Damping Control

Calibration



The objective function is not explicitly known.

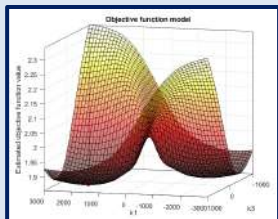
It can be considered a **stationary gaussian process**.

A known surrogate of the objective function (**Acquisition Function**) is optimized at each iteration.

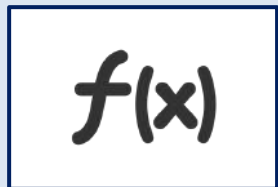
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Several acquisition functions:

Expected Improvement: The assumption is to return only explored values. We maximize the a posteriori expected improvement

$$EI_n(x) := E_n [[f(x) - f_n^*]^+]$$

EI is efficient to compute and to maximize

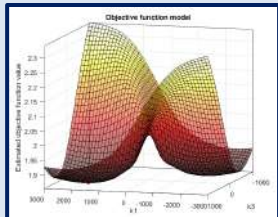
Knowledge Gradient: We allow the decision-maker to return any solution she likes,

Entropy Search: acquisition function values the information we have about the location of the global maximum according to its differential entropy

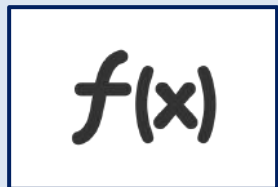
Bayesian Optimization

Data-driven optimization technique suitable for hard-to-evaluate objective function.

At each optimization step:



Objective function is modeled as a realization of a Gaussian Process



An acquisition function determines where to sample the parameters space next.

Frazier, P.I. (2018). A tutorial on bayesian optimization. arXiv preprint arXiv:1807.02811.

Objective function

Typical quantitative performance index for ride comfort:

$$\min_{\Theta} \left[\frac{1}{T} \int_0^T A_z(t, \Theta)^2 dt \right]$$

Where:

- $\Theta = \text{control algorithm parameters}$
- $A_z = \text{chassis CoG vertical acceleration}$

Optimization settings

Range of parameters: obtained by sensitivity analysis

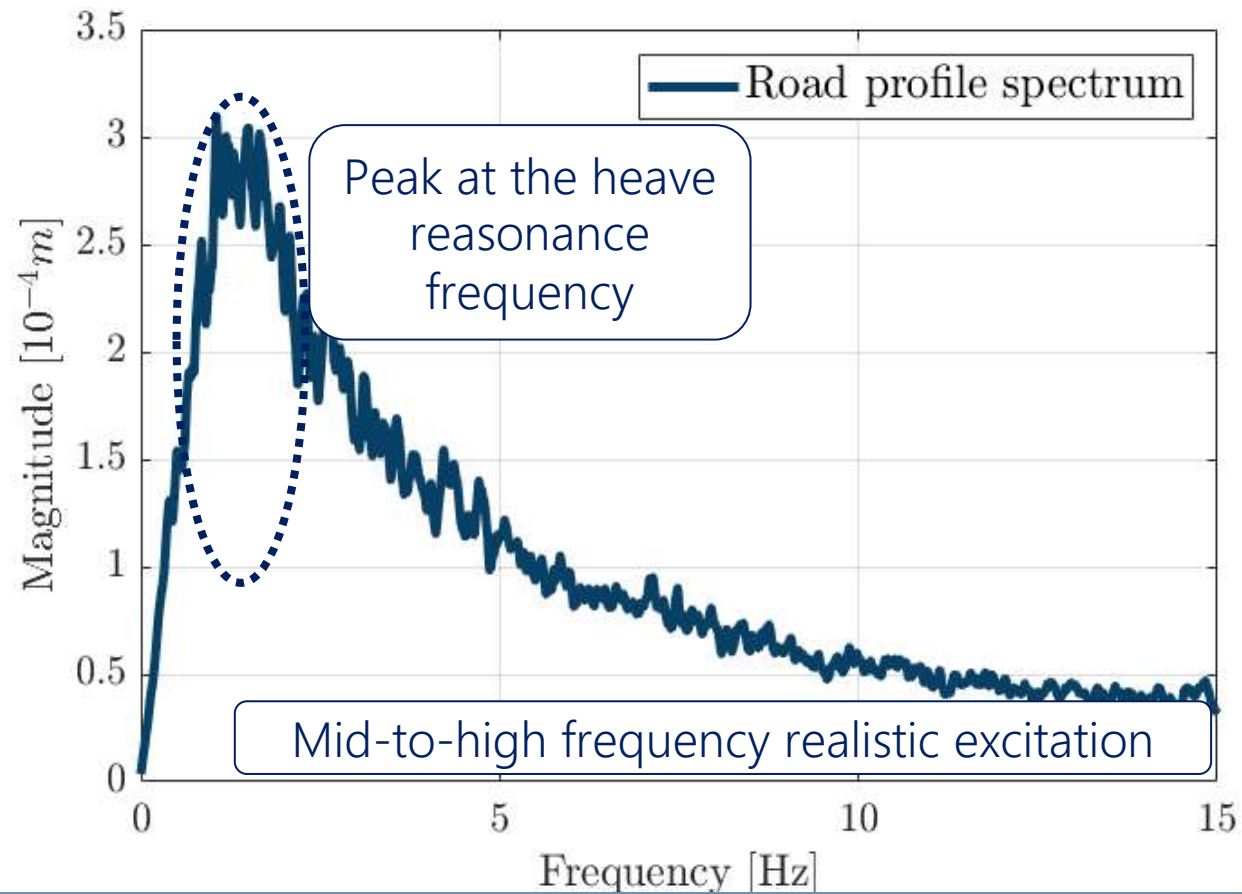
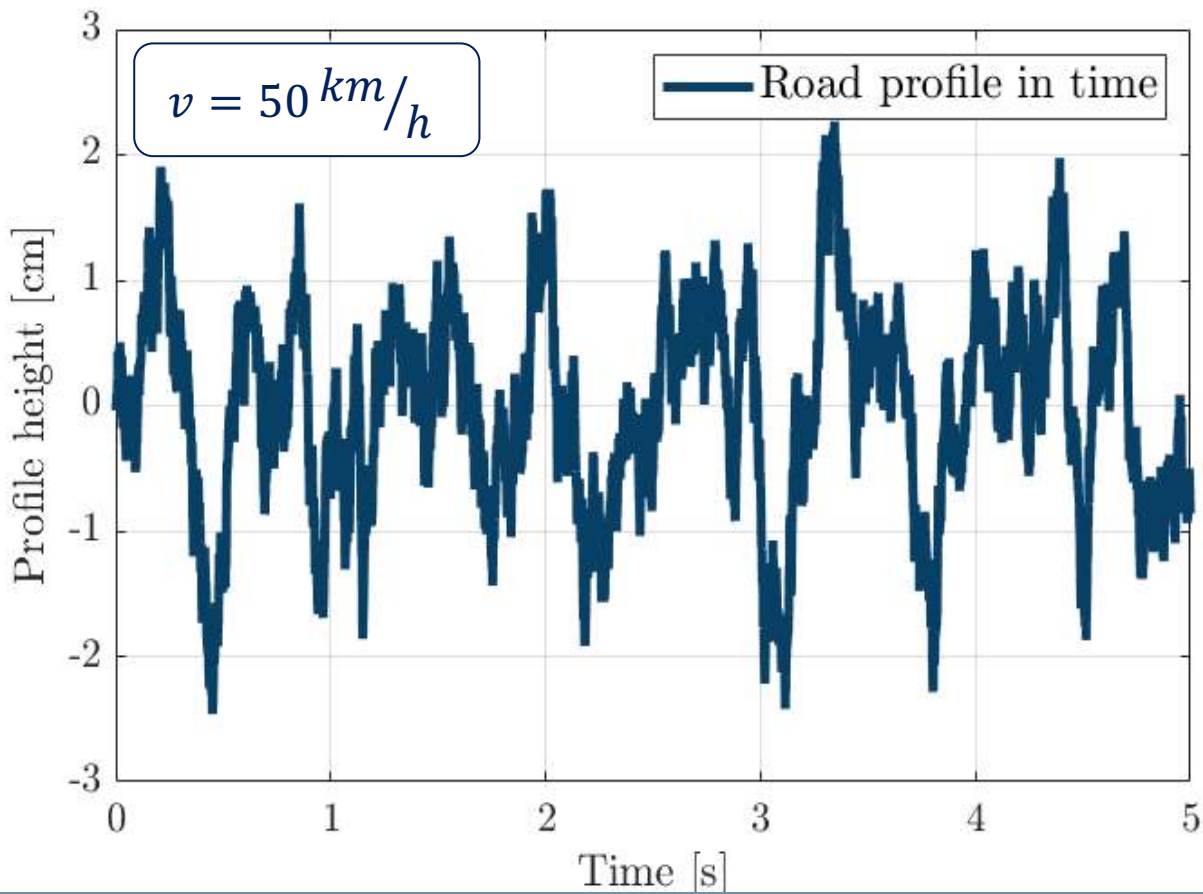
Number of iterations: 100 ~ 150

Semi-Active Damping Control

Calibration

Standard ISO – 8608 C-D road profile: regular-to-poor road scenario

$$h(x) = \sum_{i=0}^N \sqrt{\Delta n} 2^k 10^{-3} \left(\frac{n_0}{i \Delta n} \right) \cos(2\pi i \Delta n x + \phi_i)$$



Semi-Active Damping Control

Calibration

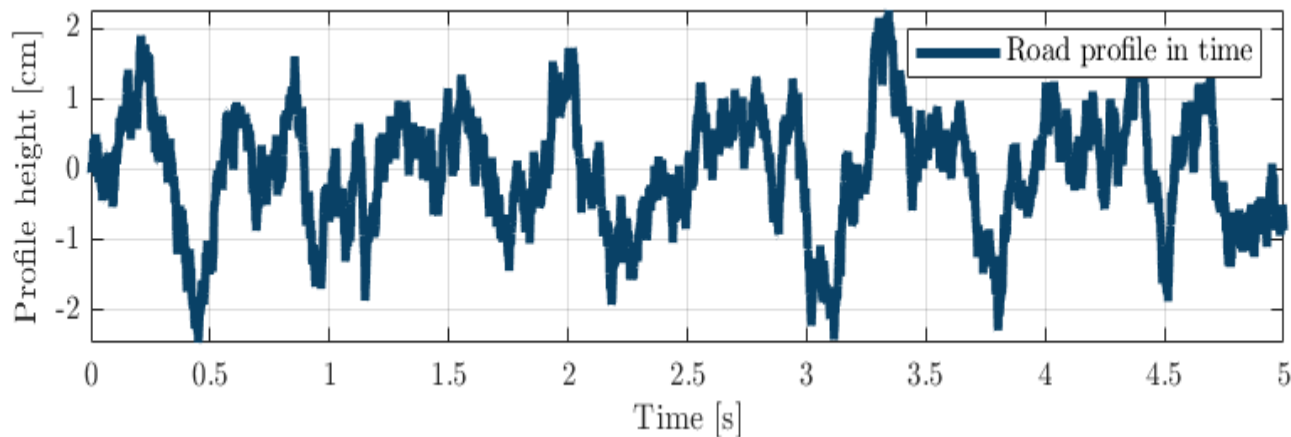
Road profile

20 realizations of the ISO road profile

$$h(x) = \sum_{i=0}^N \sqrt{\Delta n} 2^k 10^{-3} \left(\frac{n_0}{i \Delta n} \right) \cos(2\pi i \Delta n x + \phi_i)$$

Amplitude
fixed by the
standard

Phase lag
randomly
generated



Performance indexes

- Acceleration index:

$$J_{A_z} = \frac{1}{T} \int_0^T A_z(t)^2 dt$$

- Vertical jerk index

$$J_{J_z} = \frac{1}{T} \int_0^T J_z(t)^2 dt$$

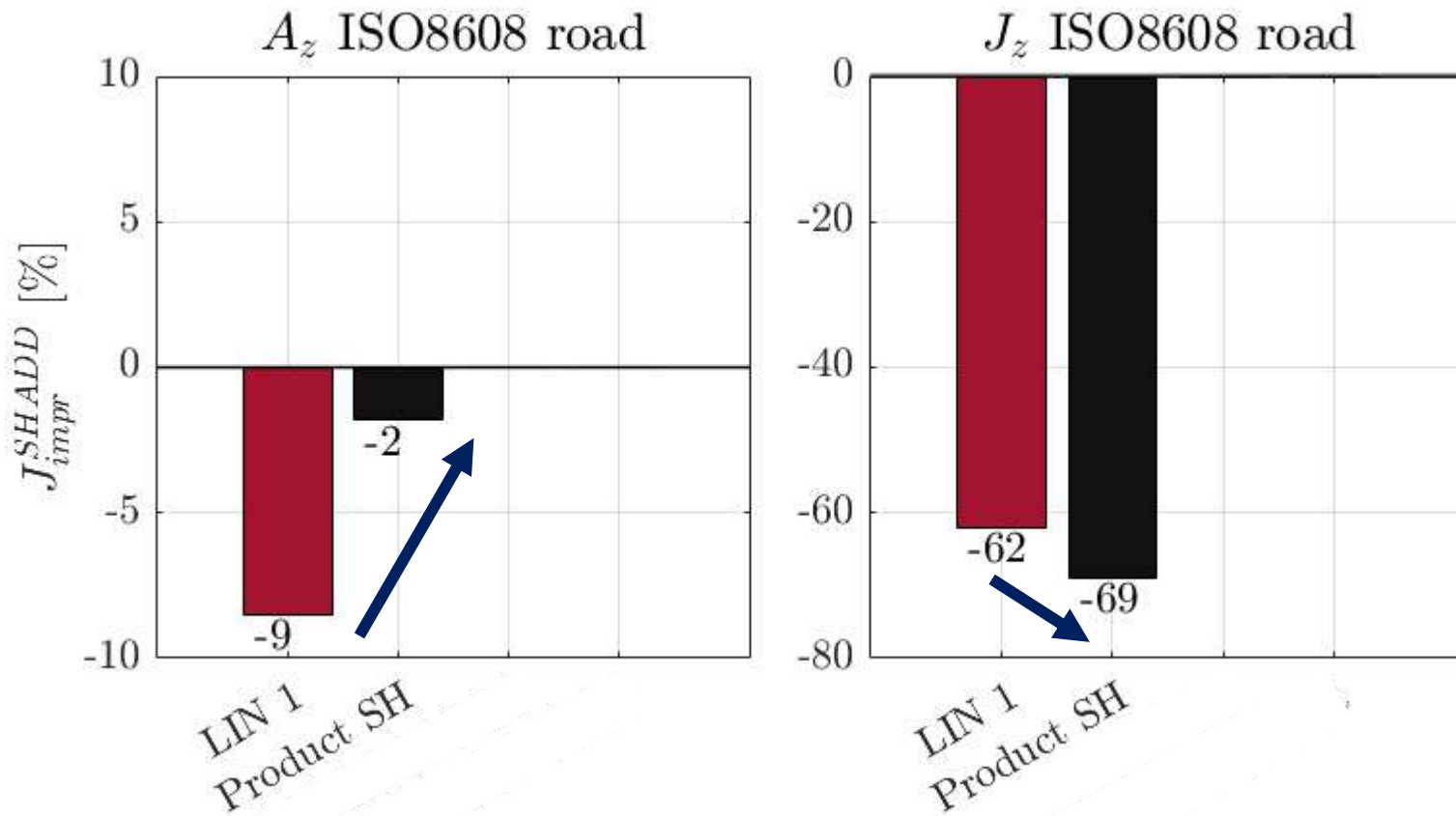
Indexes are reported as **percentage improvement** with respect to the original Mix SH-ADD:

$$J_{impr}^{A_z, J_z} = \frac{J_{A_z, J_z} - J_{A_z, J_z}^{SHADD}}{J_{A_z, J_z}^{SHADD}} \times 100$$

Semi-Active Damping Control

Calibration

The continuously modulating Mix SH-ADD is benchmarked against the Product SkyHook. Index values are the average over the 20 experiments.



Benchmark with switching Mix SH-ADD:

- $J_{impr}^{A_z} = 9\%$
- $J_{impr}^{J_z} = 62\%$

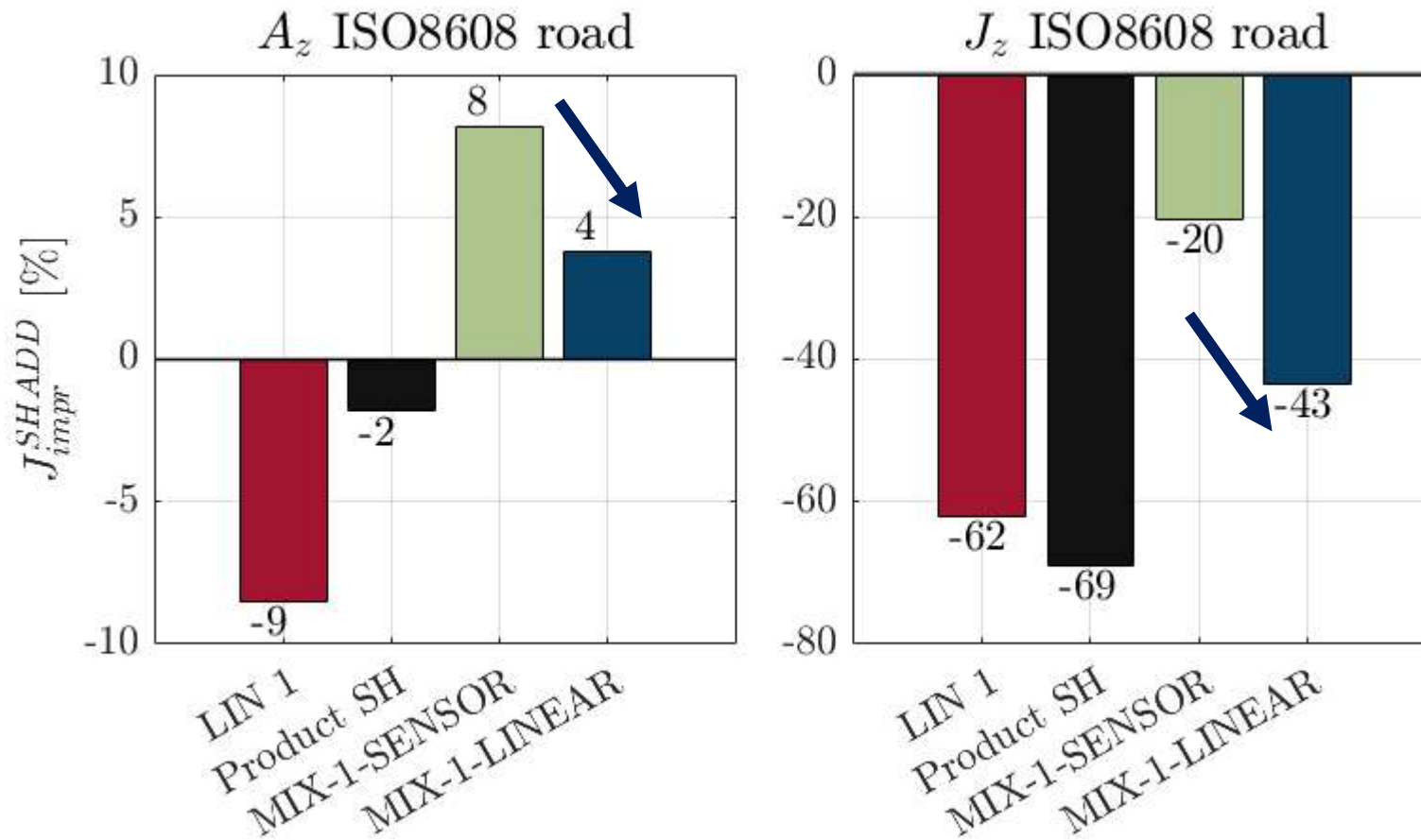
Benchmark with Product SH:

- Better filtering of road excitation
- Slightly higher vertical jerk.

Semi-Active Damping Control

Calibration

The **Mix-1-Linear** is benchmarked against the **Mix-1-Sensor** algorithm.
Index values are the average over the 20 experiments.



Benchmark with switching Mix SH-ADD:

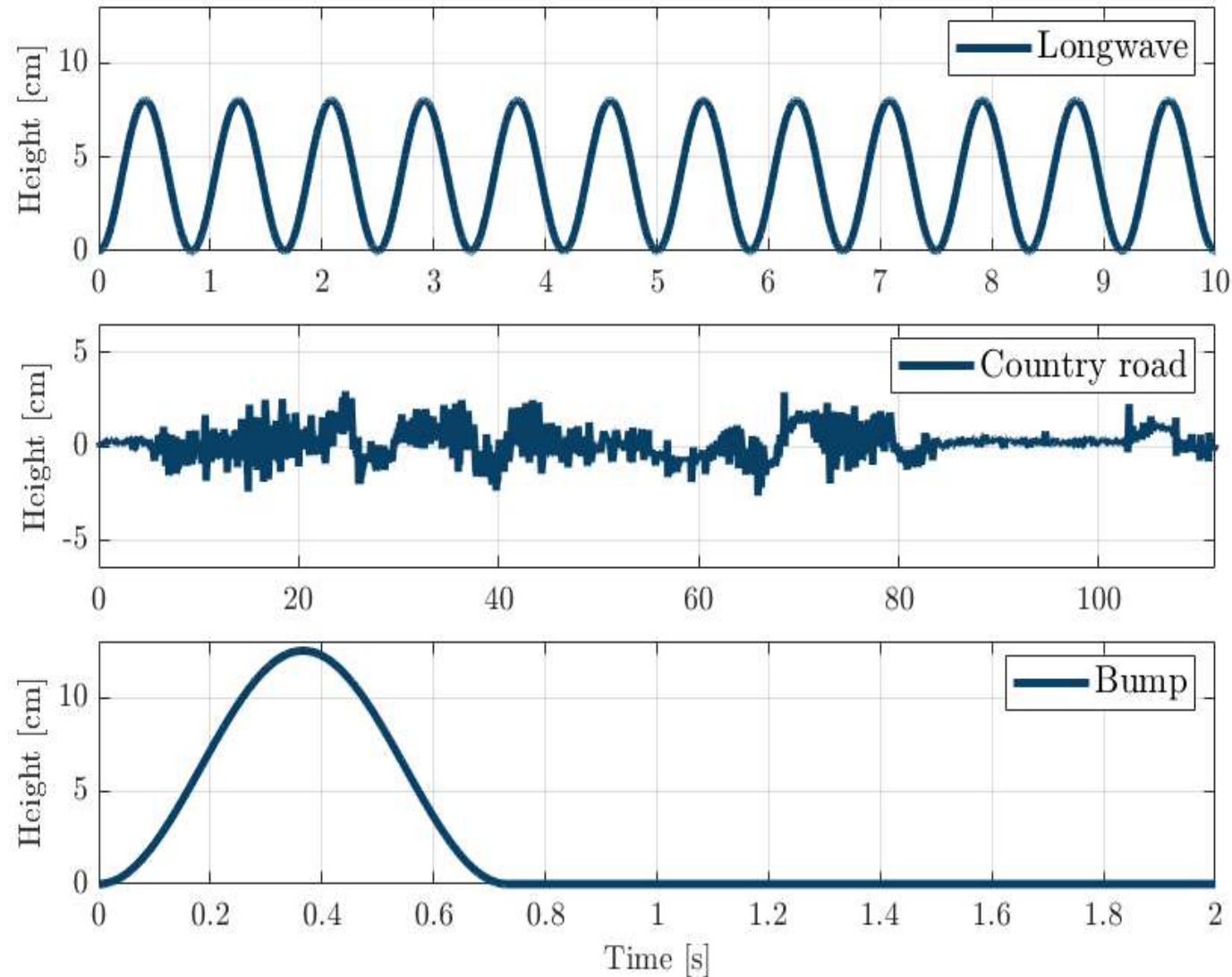
- $J_{impr}^{A_z} = -4\%$ ~ due to reduced setup
- $J_{impr}^{J_z} = 43\%$

Benchmark with Mix-1-Sensor:

- Better filtering of road excitation
- Better reduction of vertical jerk

Semi-Active Damping Control

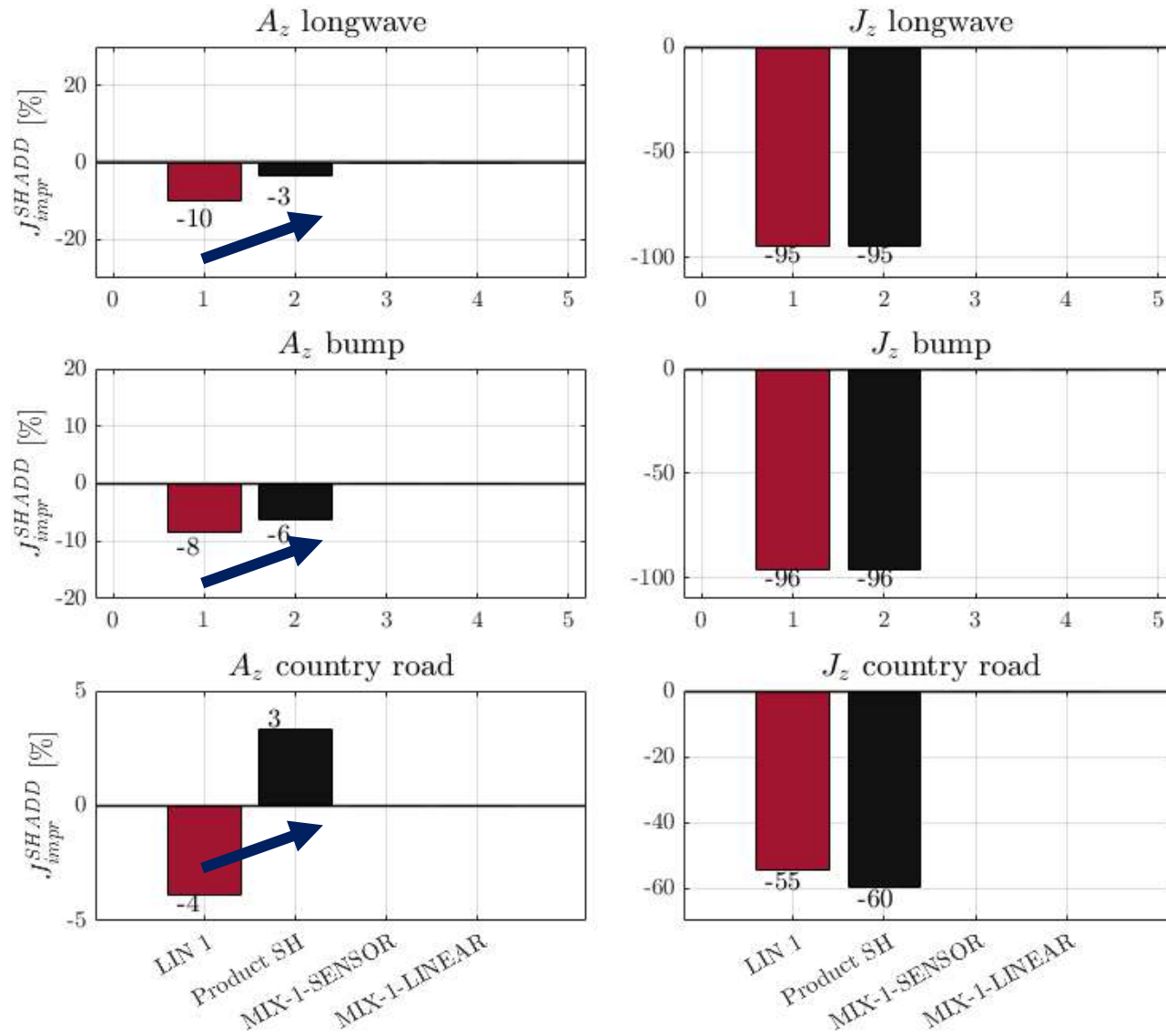
Validation



Performance indexes are the ones introduced for the validation on the ISO road profile.

Semi-Active Damping Control

Validation

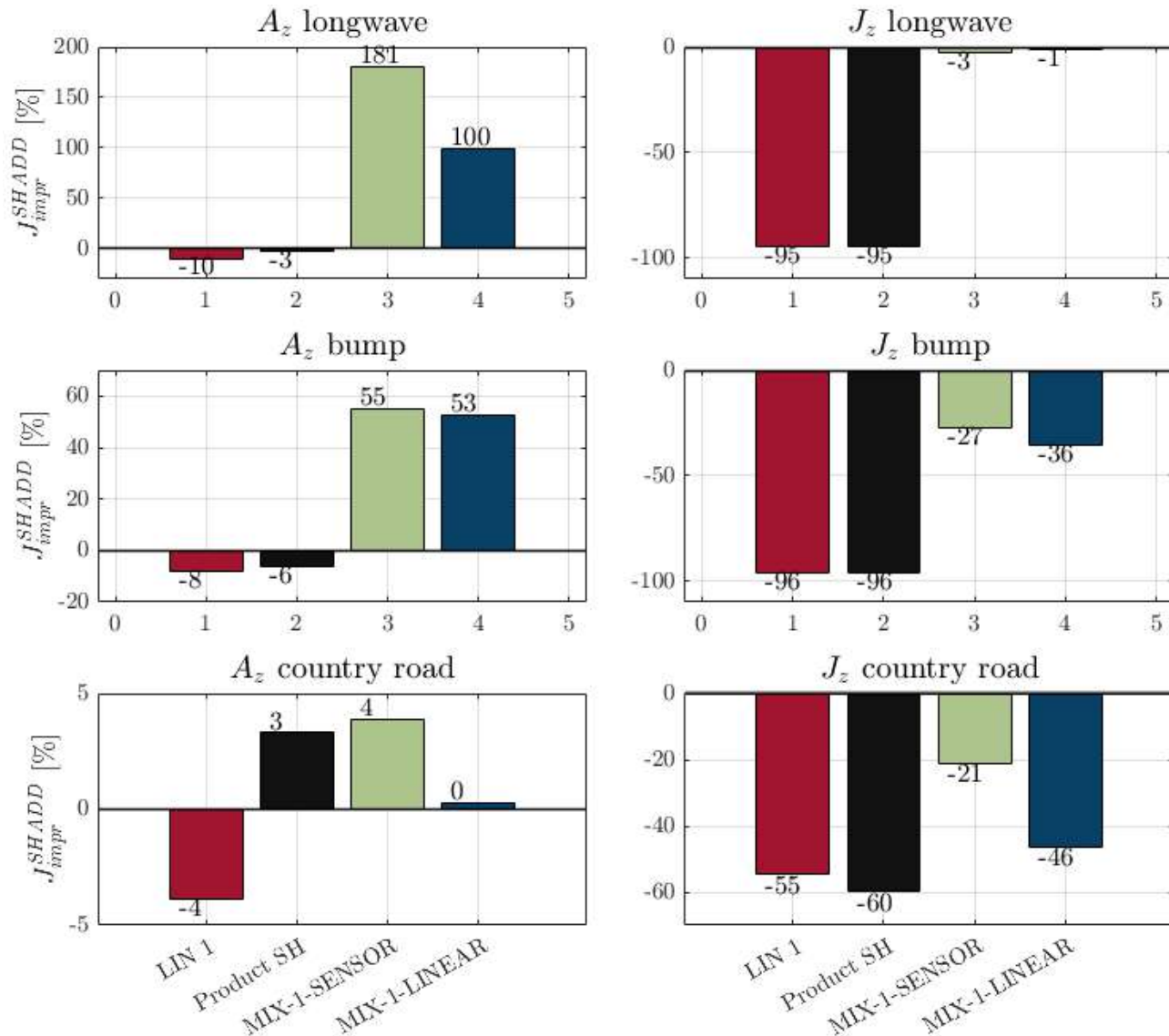


- Improvement in terms of A_z filtering on all validation profiles (up to 10%).
- Reduction of J_z on all validation profiles (up to 96%).

- Better filtering of road excitation on validation profiles.
- Comparable vertical jerk on all validation profiles.

Semi-Active Damping Control

Validation



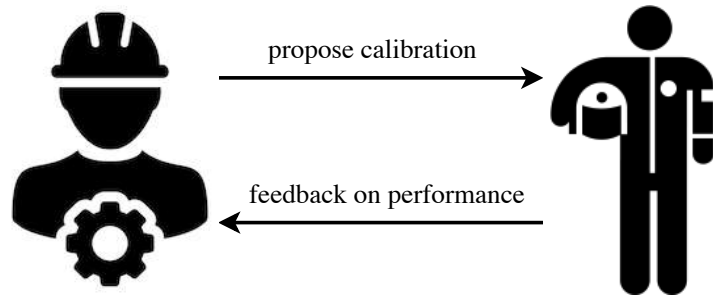
- Expected degradation of performance in terms of A_z filtering, due to reduced setup.
- Comparable or lower J_z on all validation profiles (up to 46% improvement on *country*).

- Better filtering of road excitation on *longwave* and *bump*, comparable on *country road*.
- Better reduction of vertical jerk on *bump* and *country road*, comparable on *longwave*.

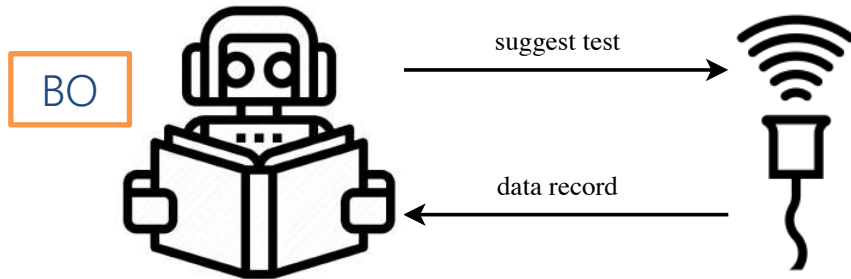
Semi-Active Damping Control

Calibration

(A) traditional calibration

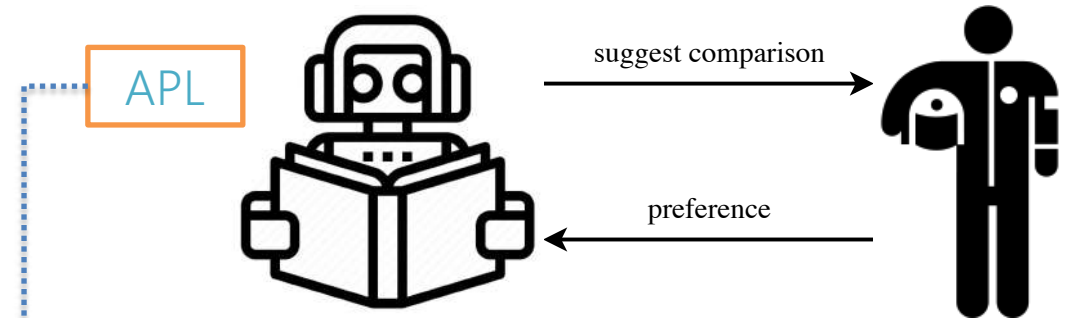


(B) automatic performance-based paradigm



Savaia, Sohn, Formentin, Panzani, Corno, Savaresi –
Experimental Automatic Calibration of a Semi-Active Suspension Controller
via Bayesian Optimization,
Journal of Systems and Control, 2021 [in press]

(C) semi-automatic preference-based paradigm



[Bemporad, 2020] – Active preference learning
based on radial basis functions.

- Advantages w.r.t. (A)
 - time/cost of experiments
- Advantages w.r.t. (B)
 - **model-free**
 - optimization **tailored to subjective preference**

APL Methodology

APL: problem statement

- $x \in \mathbb{R}^n$ **decision vector** (\mathbb{R}^n decision variable space).
- $\pi: \mathbb{R}^n \times \mathbb{R}^n \rightarrow \{-1, 0, 1\}$ **preference function** defined as:

$$x = \begin{bmatrix} \vartheta_F \\ \vartheta_R \end{bmatrix} \in \mathbb{R}^2$$

$$\pi(x_1, x_2) = \begin{cases} -1 & \text{if } x_1 \text{ is better than } x_2 \\ 0 & \text{if } x_1 \text{ is as good as } x_2 \\ 1 & \text{if } x_1 \text{ is worst than } x_2 \end{cases}$$

Assumption: properties of π .

➤ reflexivity

$$\pi(x_1, x_1) = 0 \quad \forall x_1 \in \mathbb{R}^n$$

➤ anticommutativity

$$\pi(x_1, x_2) = -\pi(x_2, x_1) \quad \forall x_1, x_2 \in \mathbb{R}^n$$

➤ transitivity

$$\pi(x_1, x_2) = \pi(x_2, x_3) = -1$$

$$\Rightarrow \pi(x_1, x_3) = -1 \quad \forall x_1, x_2, x_3 \in \mathbb{R}^n$$

Find **best preference vector**,
inside the **feasible space**.

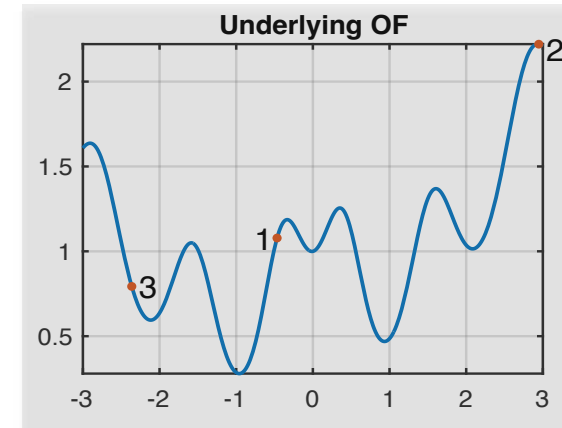
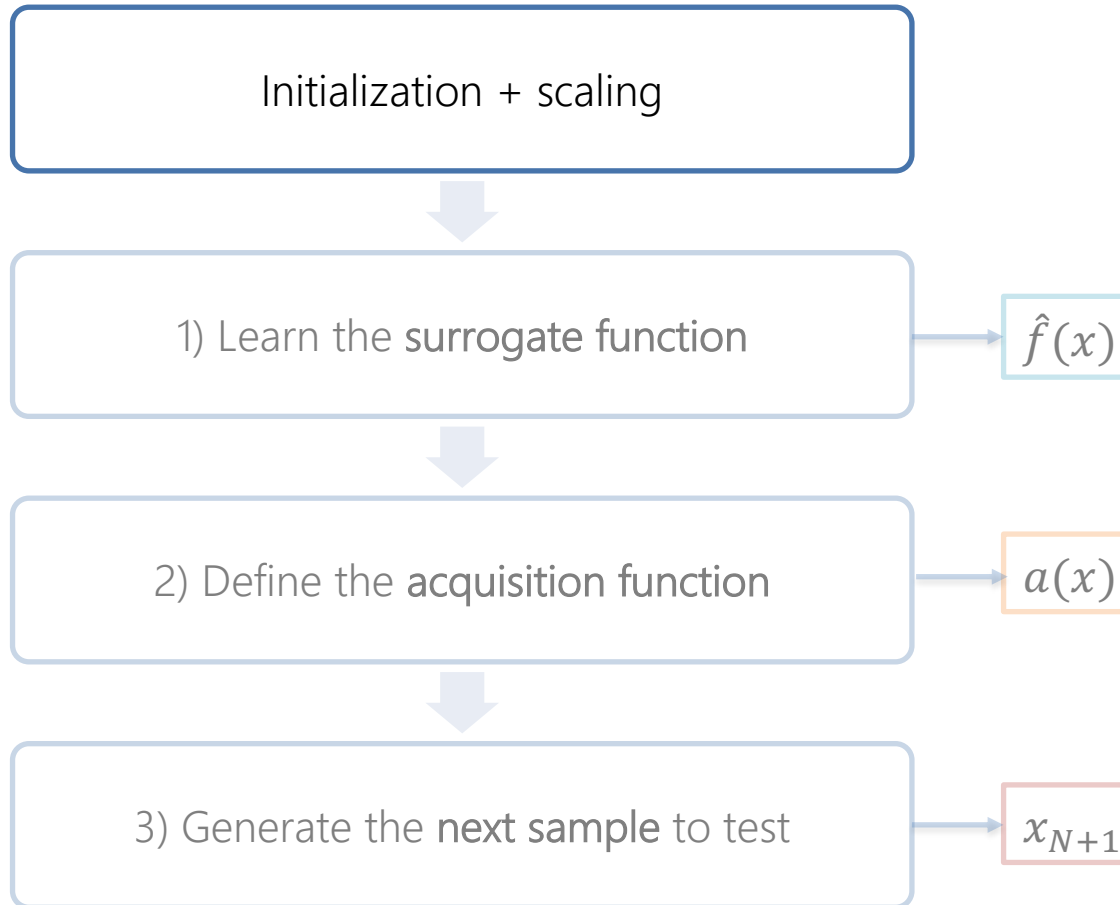
$$\text{find } x^* \text{ s.t. } \pi(x^*, x) \leq 0, \quad \forall x \in \mathbb{R}^n, \quad l \leq x \leq u$$

$l, u \in \mathbb{R}^n$: lower and upper bound on x .

$$l = \begin{bmatrix} 0 \\ 0 \end{bmatrix}, \quad u = \begin{bmatrix} 166 \\ 166 \end{bmatrix}$$

APL Methodology

APL: general scheme



$$\pi(x_1, x_2) = \begin{cases} -1 & \text{if } f(x_1) - f(x_2) < -\sigma_f \\ 0 & \text{if } |f(x_1) - f(x_2)| \leq \sigma_f \\ 1 & \text{if } f(x_1) - f(x_2) > \sigma_f \end{cases}$$

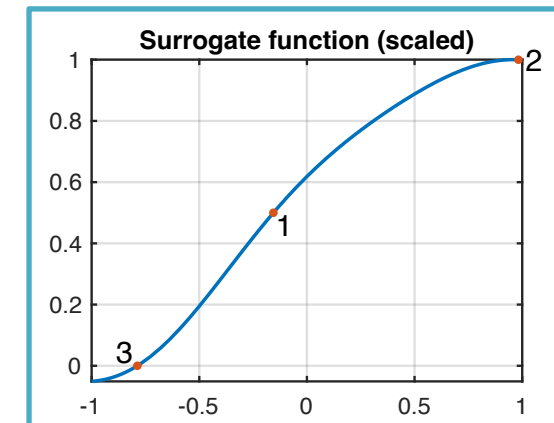
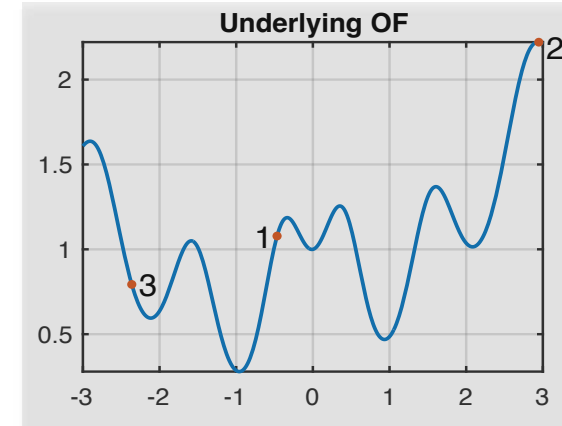
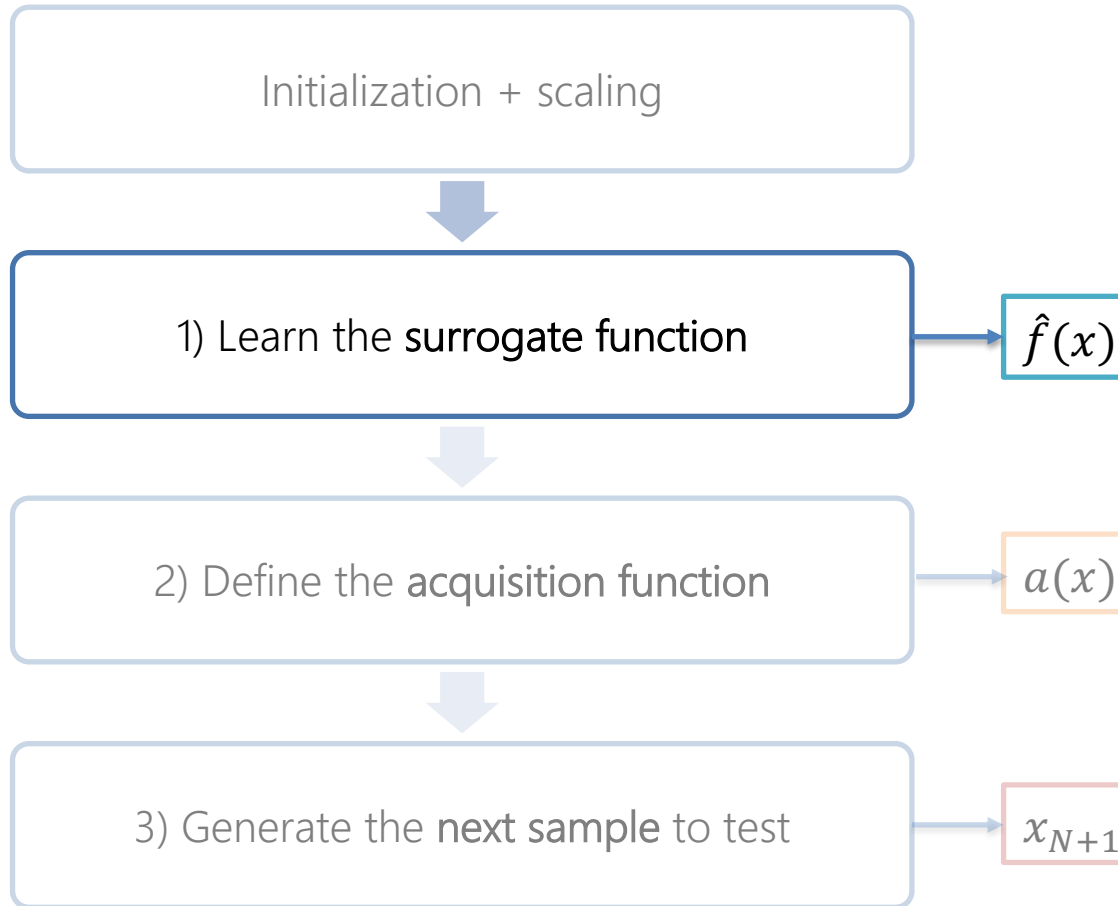
σ_f : comparison tolerance

Generate 3 samples with LHS.

- It. 1: observe $\pi(x_1, x_2) = -1$ ($x_1^* = x_1$)
- It. 2: observe $\pi(x_1, x_3) = 1$ ($x_2^* = x_3$)

APL Methodology

APL: general scheme



$$\begin{aligned} & \text{minimize: } \frac{\gamma}{2} \beta^T \beta + c^T \varepsilon \\ & \text{subject to } (\Psi^{i(h)} - \Psi^{j(h)}) \beta \leq -\sigma + \varepsilon_h \quad \forall h : b_h = -1, \\ & (\Psi^{i(h)} - \Psi^{j(h)}) \beta \geq \sigma - \varepsilon_h \quad \forall h : b_h = 1, \\ & (\Psi^{i(h)} - \Psi^{j(h)}) \beta \leq \sigma + \varepsilon_h \quad \forall h : b_h = 0, \\ & (\Psi^{i(h)} - \Psi^{j(h)}) \beta \geq -\sigma - \varepsilon_h \quad \forall h : b_h = 0, \\ & \varepsilon_h \geq 0 \quad \forall h \end{aligned}$$

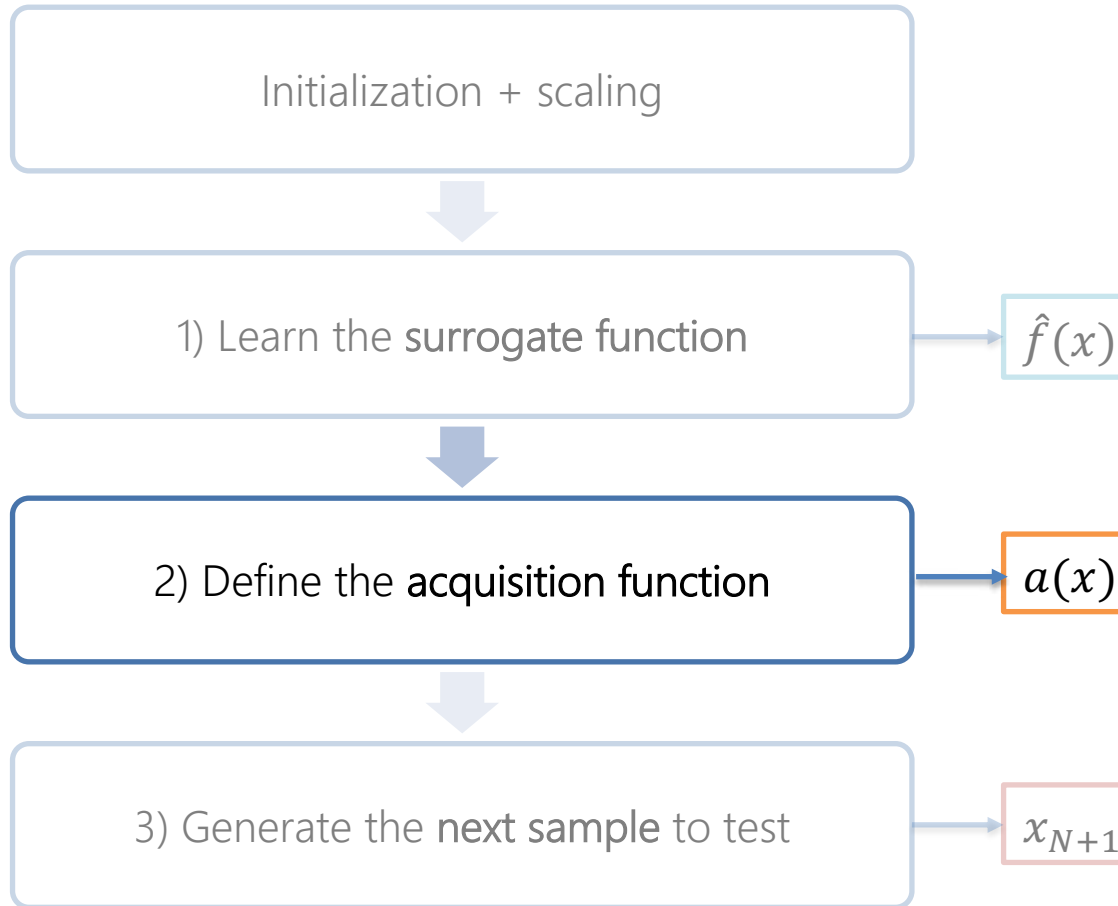
β

$$\hat{f}(x) = \sum_{i=1}^N \beta_i \phi(\varepsilon d(x, x_i))$$

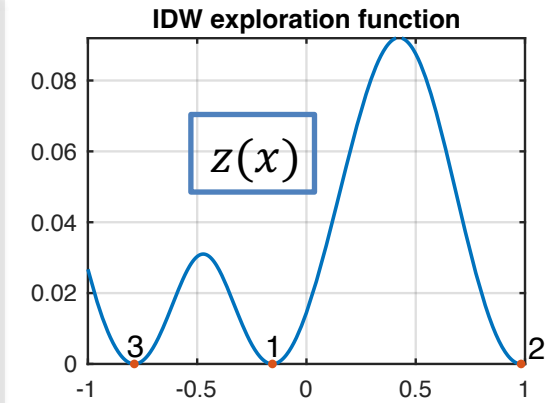
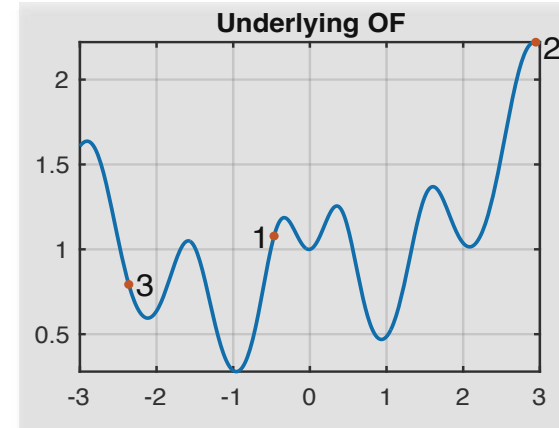
RBF-interpolant

APL Methodology

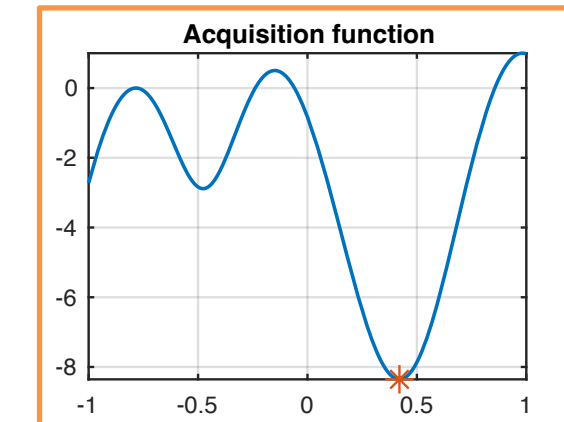
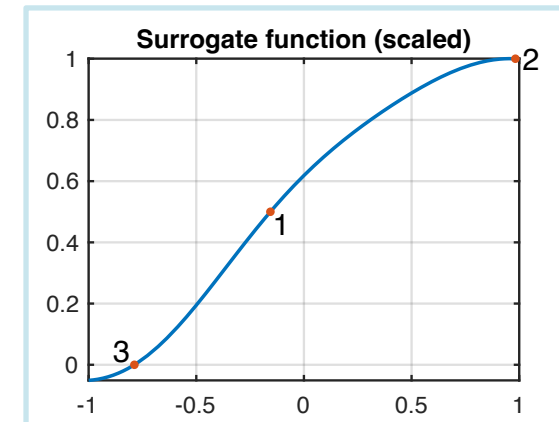
APL: general scheme



$$\hat{f}(x)$$



$$a(x)$$



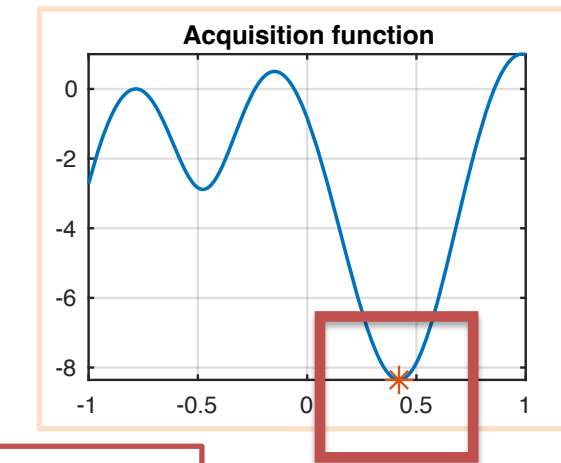
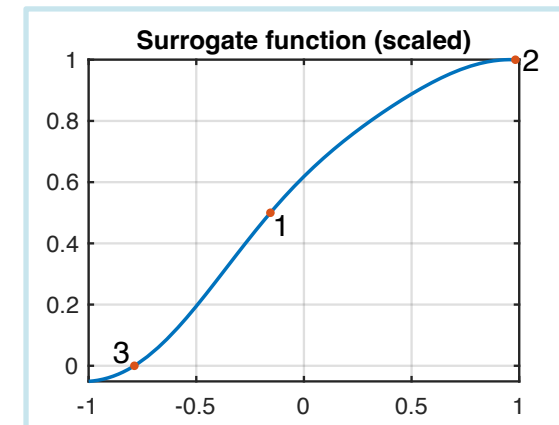
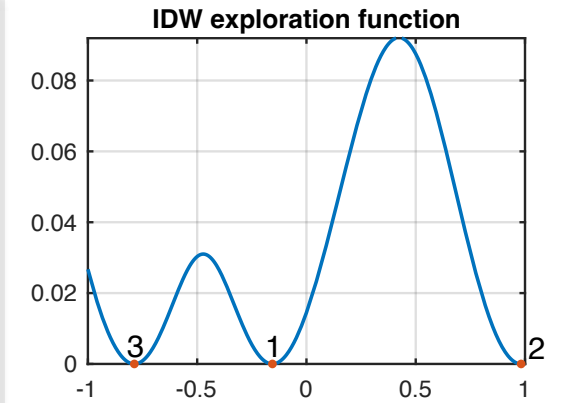
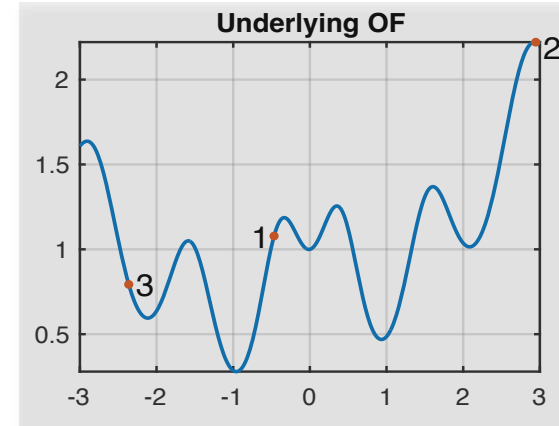
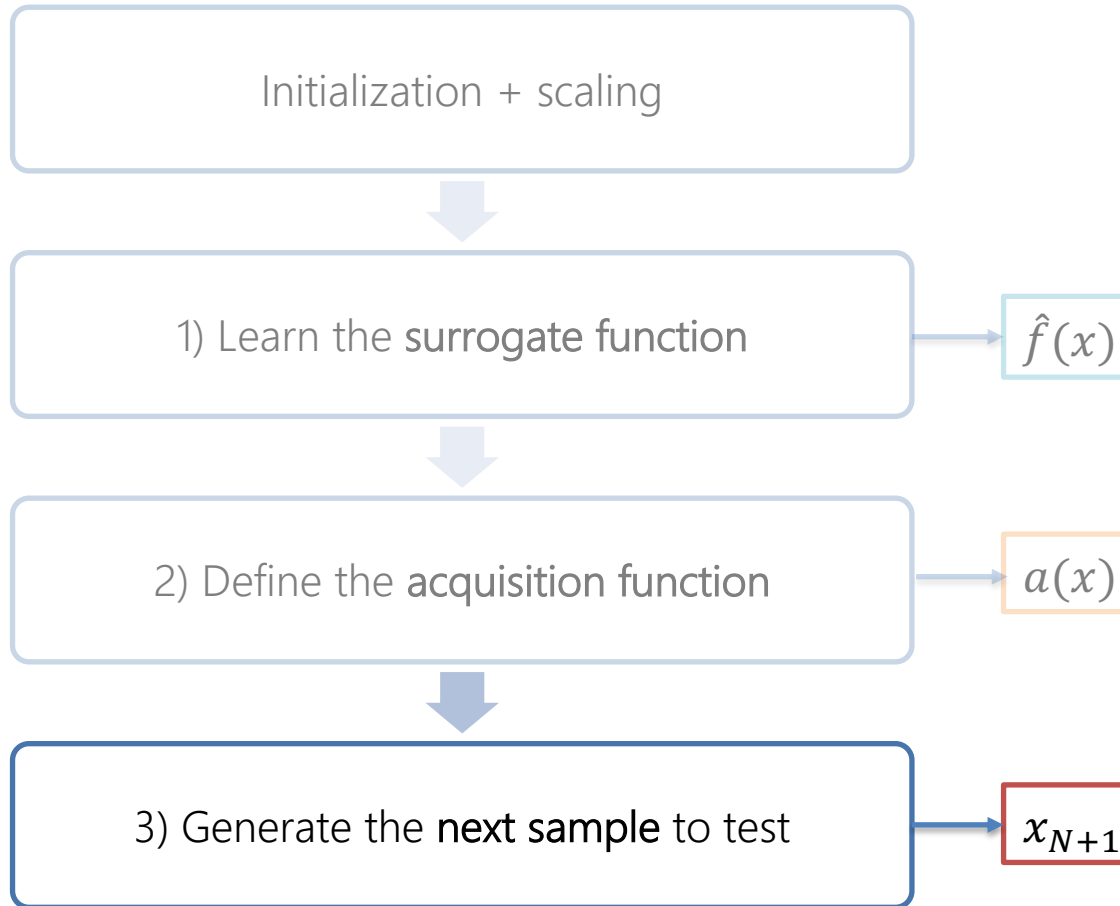
$$x_{N+1}$$

Exploration parameter $\delta \geq 0$

$$a(x) = \hat{f}(x) - \delta z(x)$$

APL Methodology

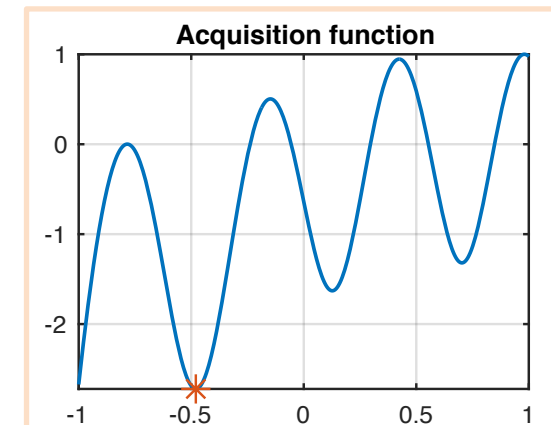
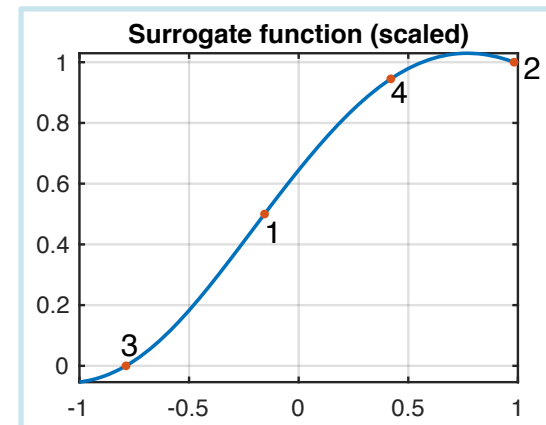
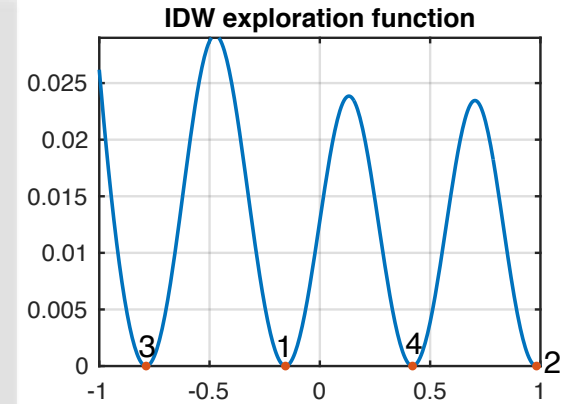
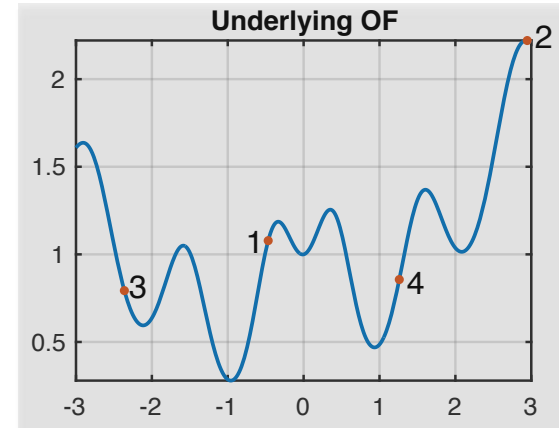
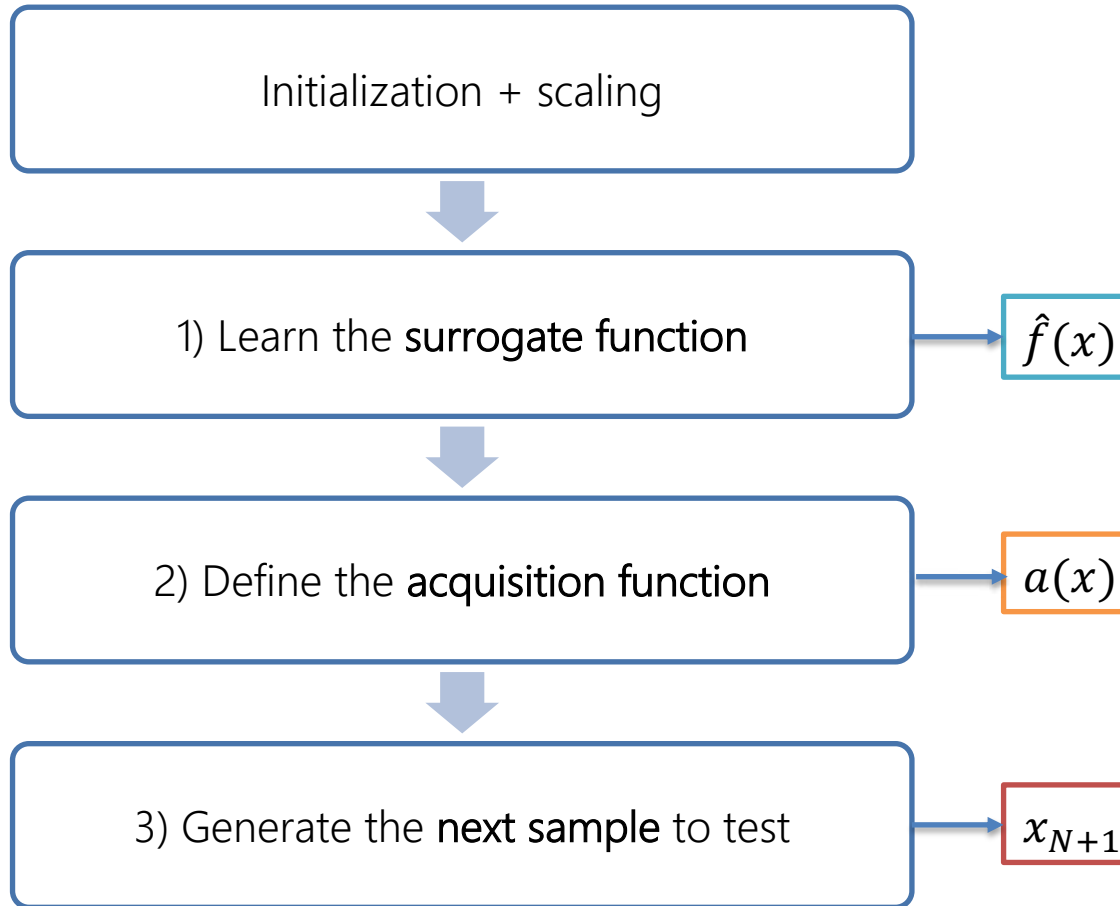
APL: general scheme



$$\begin{aligned} & \underset{x}{\text{minimize}} && a(x) \\ & \text{subject to} && l \leq x \leq u \end{aligned}$$

APL Methodology

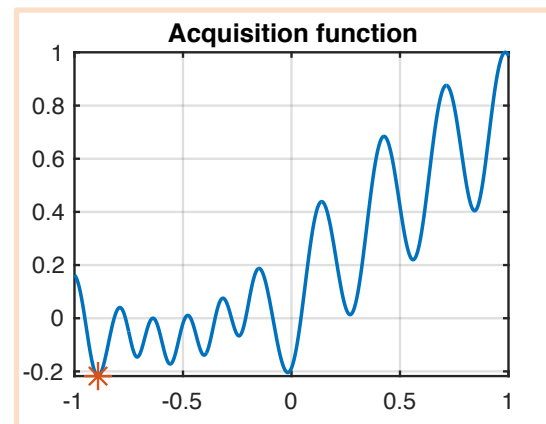
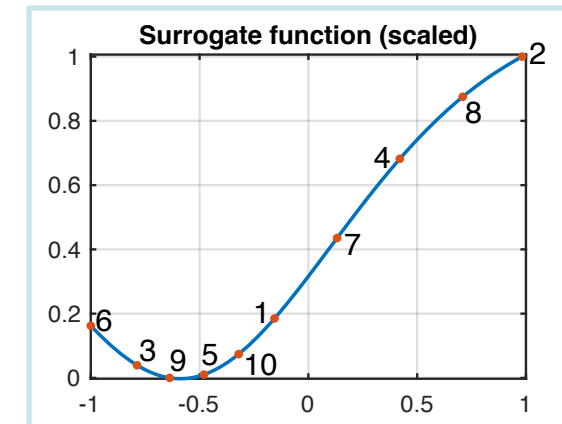
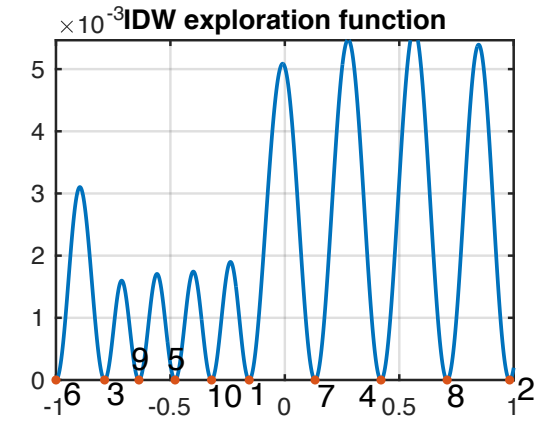
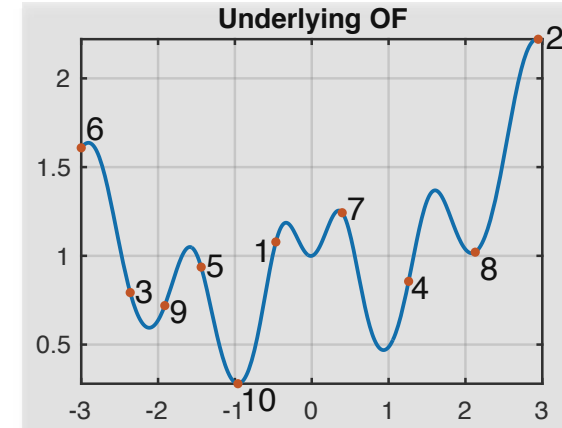
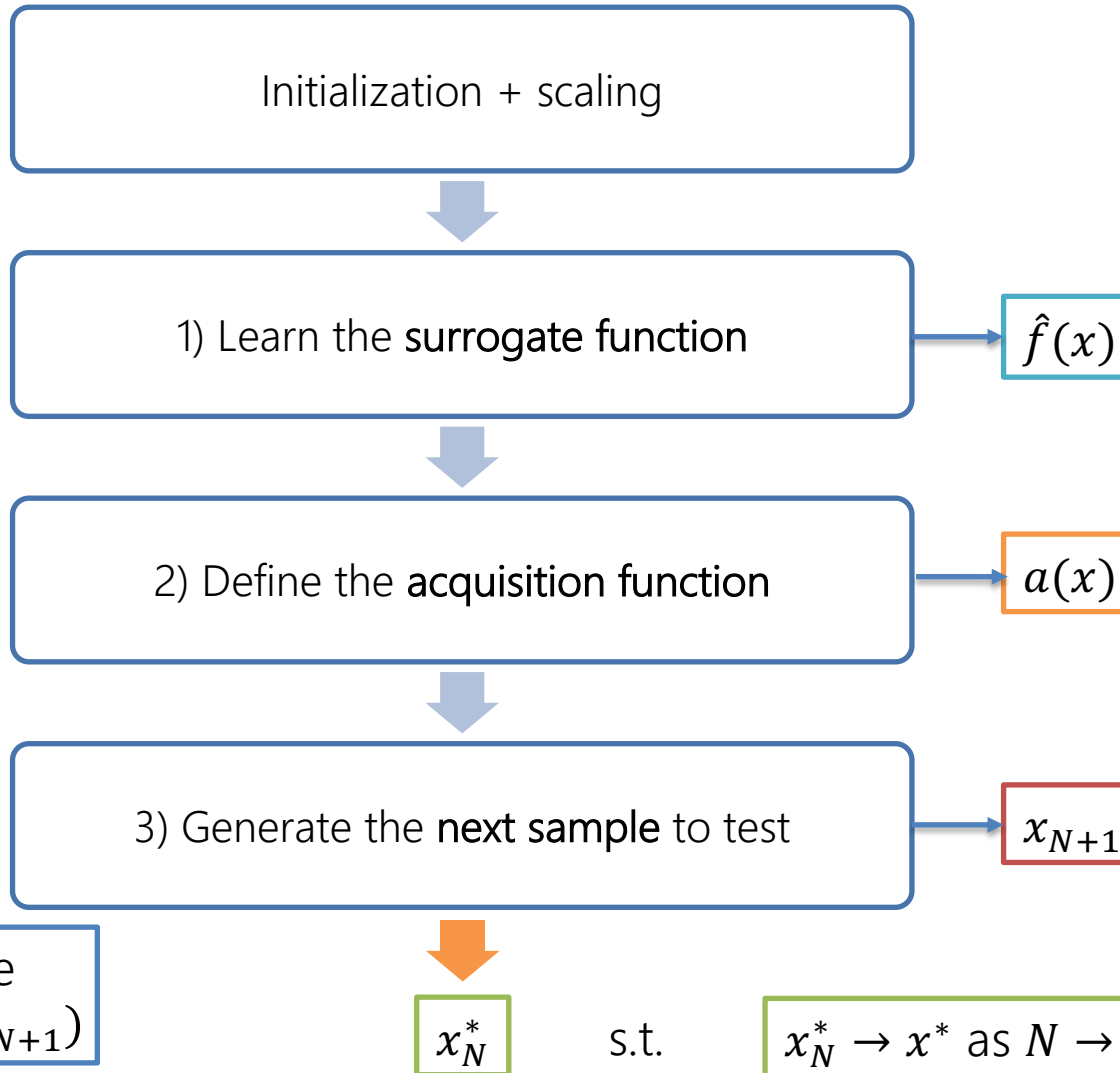
APL: general scheme



Observe $\pi(x_{i^*}, x_{N+1})$

APL Methodology

APL: general scheme



APL Methodology

Simulation study

Param	Description
N_{init}	Number of initial samples.
δ	Exploration parameter of acquisition function.
ϵ	Shape parameter of RBF.
σ	Tolerance of (QP) learning problem.
...	...

APL has many degrees of freedom

Sensitivity analysis
(via simulation)

Conclusion

$$a(x) = \hat{f}(x) - \delta z(x)$$

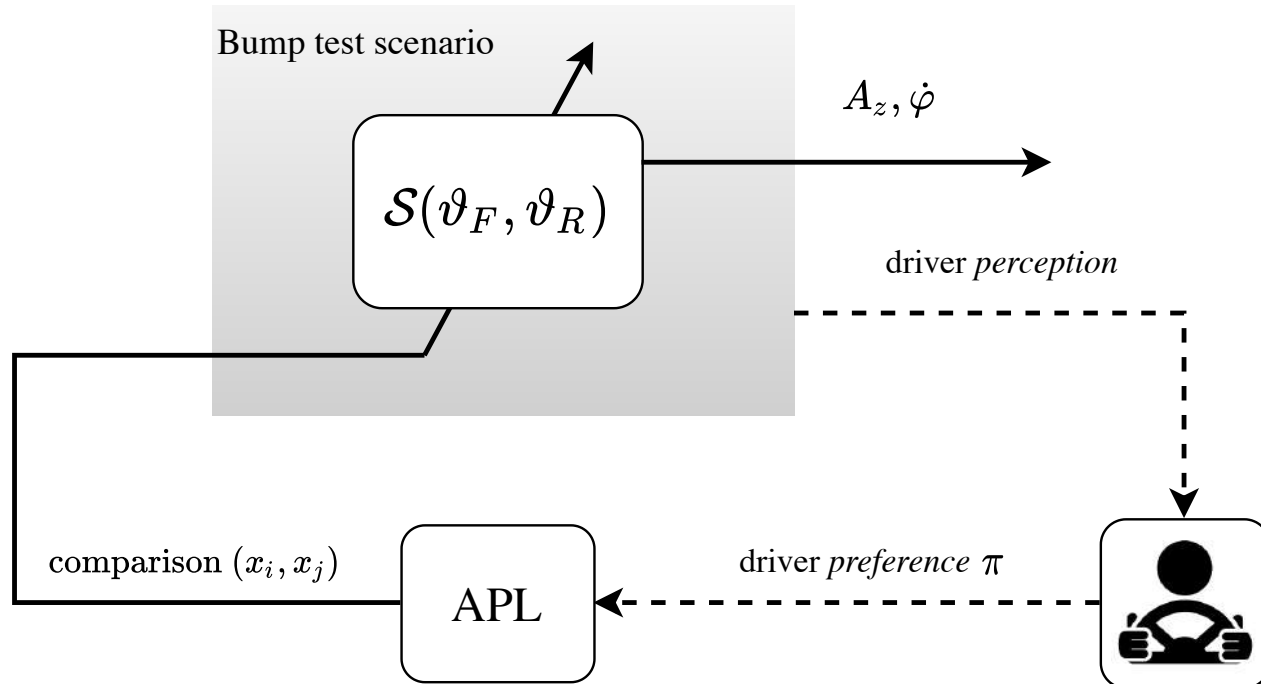
Exploration-exploitation trade-off:

- $x_N^* \rightarrow x^*$ only for δ sufficiently large
- too high δ shows slower convergence

- δ is the most important hyperparameter.
- Fine-tuning the others gives small benefit (once δ is tuned).

Bridging-the-gap from theory to practice

Bump test scenario



Bump test scenario

Negotiate a **speed bump** at constant speed.
(30 km/h using CC system)



Suspension in a car influence (mainly):

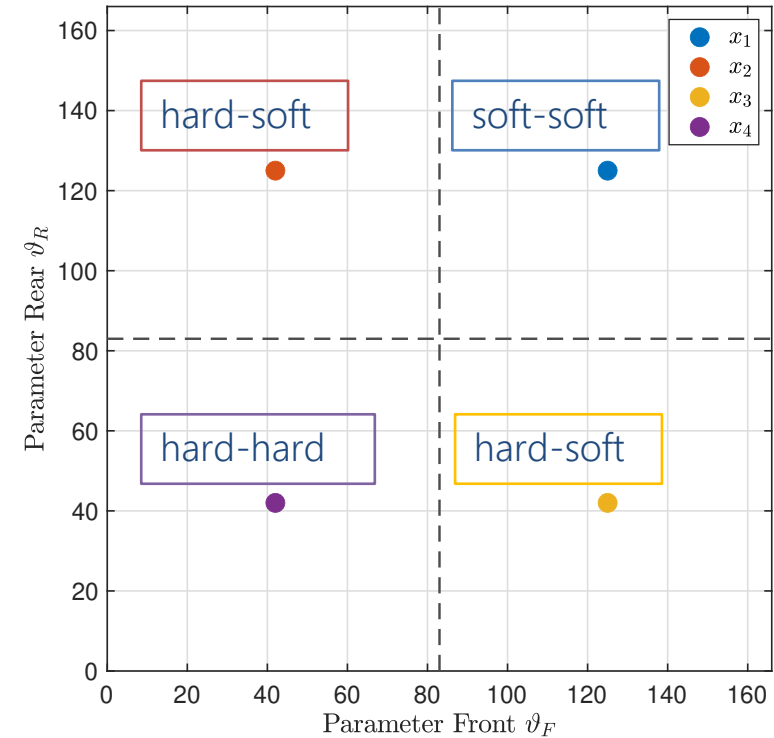
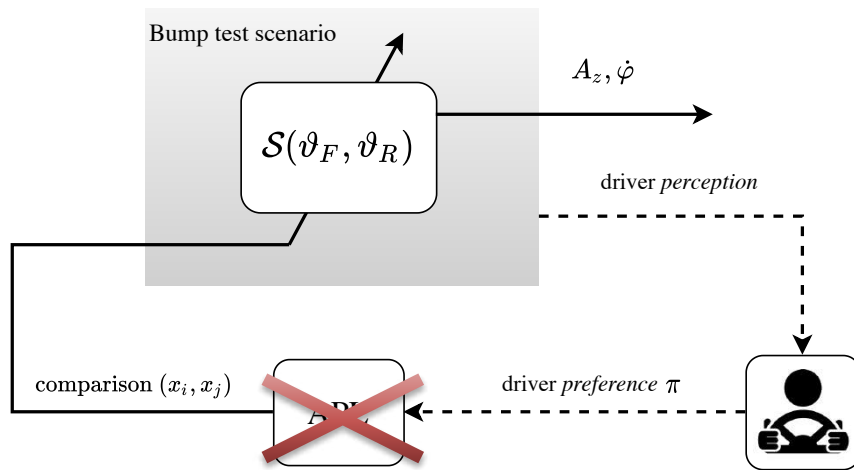
- Vertical movement $\rightarrow A_z$
- Pitch $\rightarrow \dot{\varphi}$
- Roll (negligible in this case)

Bridging-the-gap from theory to practice

Preliminary Experiment

Preliminary Experiment

- 1) Understand our **capability to perceive** different behaviors of the car.
- 2) Fit rough model of underlying OF.



4 benchmark settings in the parameters space:

x_1, x_2, x_3, x_4

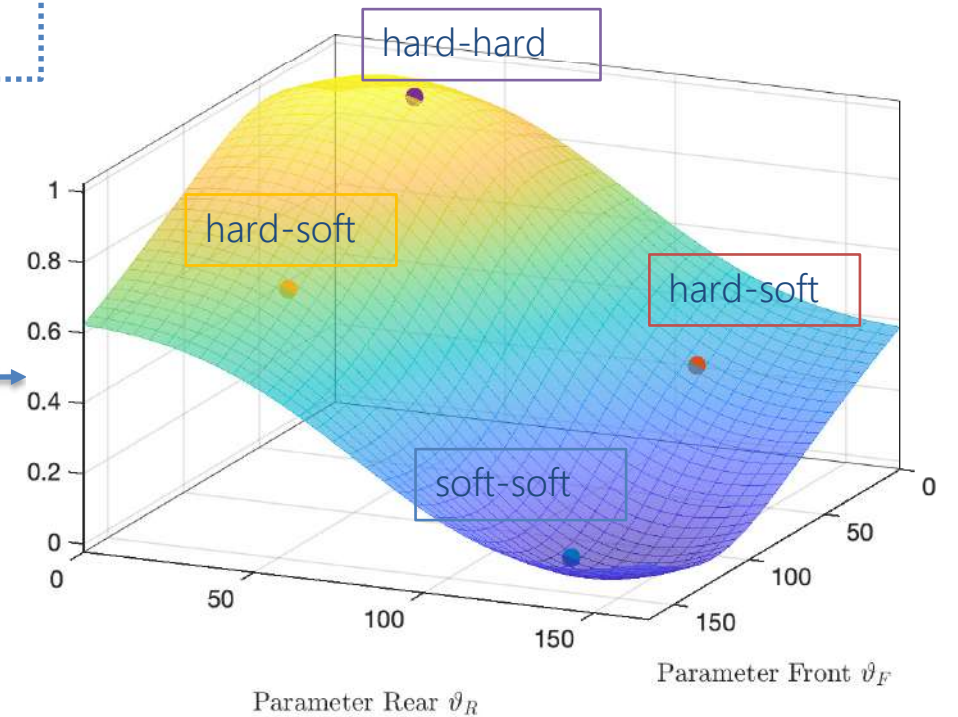
Bridging-the-gap from theory to practice

Preliminary Experiment

Same procedure as in APL to learn the surrogate.

Test #	1	2	3	4	5	6
x_i	x_2	x_1	x_1	x_3	x_4	x_3
x_j	x_1	x_3	x_4	x_2	x_2	x_4
best	x_1	x_1	x_1	x_2	x_2	x_3

- Driver is able to express committed preference.
- Transitive property satisfied \rightarrow ranking: s_s, h_s, s_h, h_h.

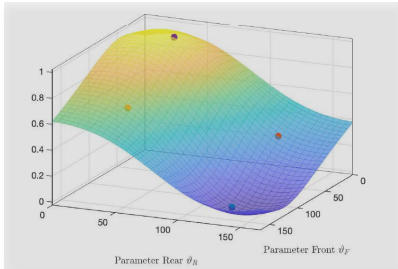


Preference-based identification of the underlying OF.

Bridging-the-gap from theory to practice

Simulation

Tuning hyperparameter δ via simulation



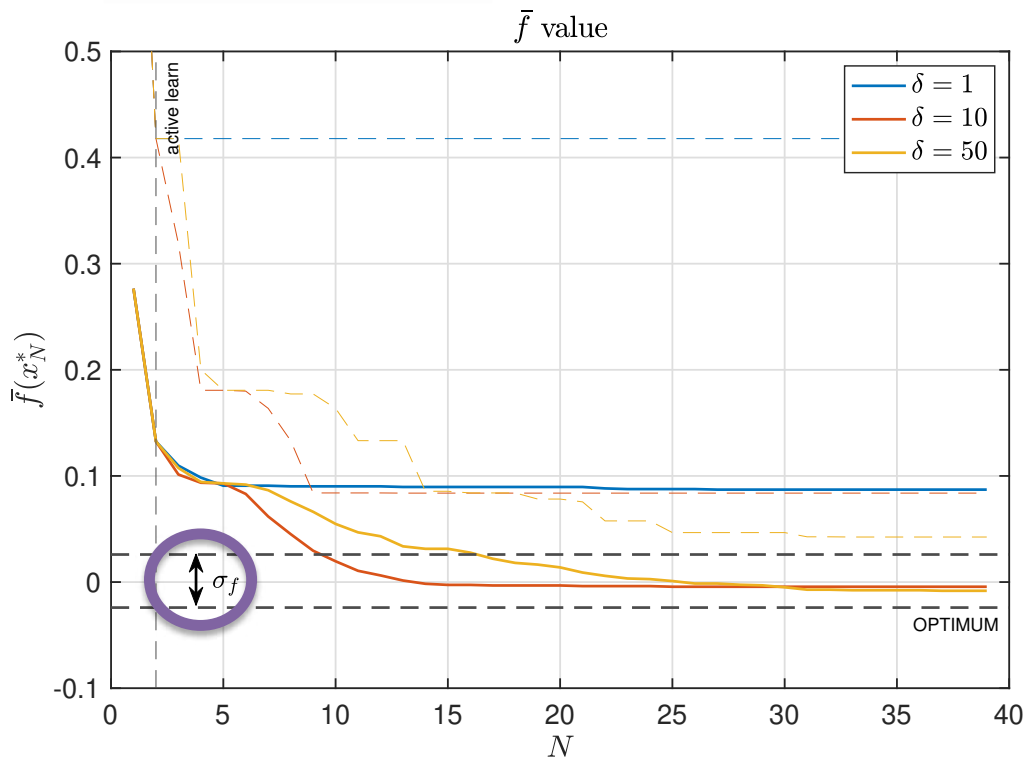
$$\sigma_f = 0.05$$

heuristics: equivalent to 20 steps of "resolution", expressing our preference

Stopping criterion

The APL procedure converges when:

- 3 consecutive "zeros"
- OR
- at least 4 "zeros" in 5 consecutive iterations



Best $\delta = 10$

	$\delta = 1$	$\delta = 10$	$\delta = 50$
N_{conv}	6	15	36

Bridging-the-gap from theory to practice

Preliminary Experiment

Experimental protocol

- Driver: express preference.
- Co-driver: update parameters.

Step#	Task description
1	APL suggest a pair-wise comparison: x_i VS x_j .
2	Update ϑ_F and ϑ_R according to x_i .
3	Perform first bump test .
4	Update ϑ_F and ϑ_R according to x_j .
5	Perform second bump test .
6	Driver expresses his preference $\pi(x_i, x_j)$.

Remarks:

- Driver must be **well-focused on his perception** (and familiar with the setup).
- The 2 bump tests should happen **close in time**.
- The test must be informative enough (eventually **repeat**).
- **Driver must not know** value of ϑ_F and ϑ_R .

Experimental results

APL Experiment

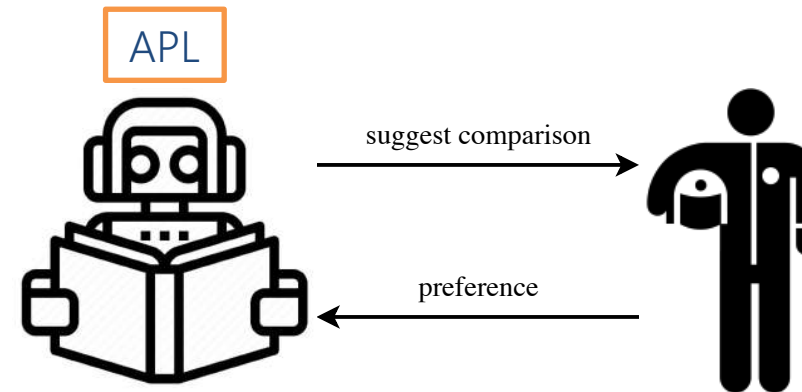
APL Experiment

- 1) Semi-automatic preference-based calibration via APL.
- 2) Sensitivity analysis w.r.t. δ (validate simulation results).

- $\delta = 1$ (3 repetitions) $\rightarrow \delta 1A, \delta 1B, \delta 1C$
Too low exploration expected.

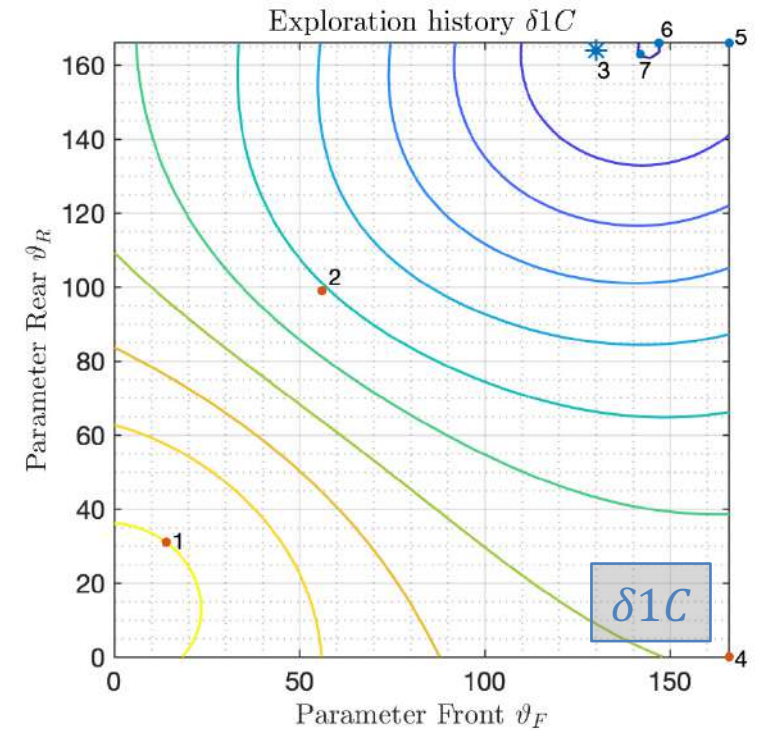
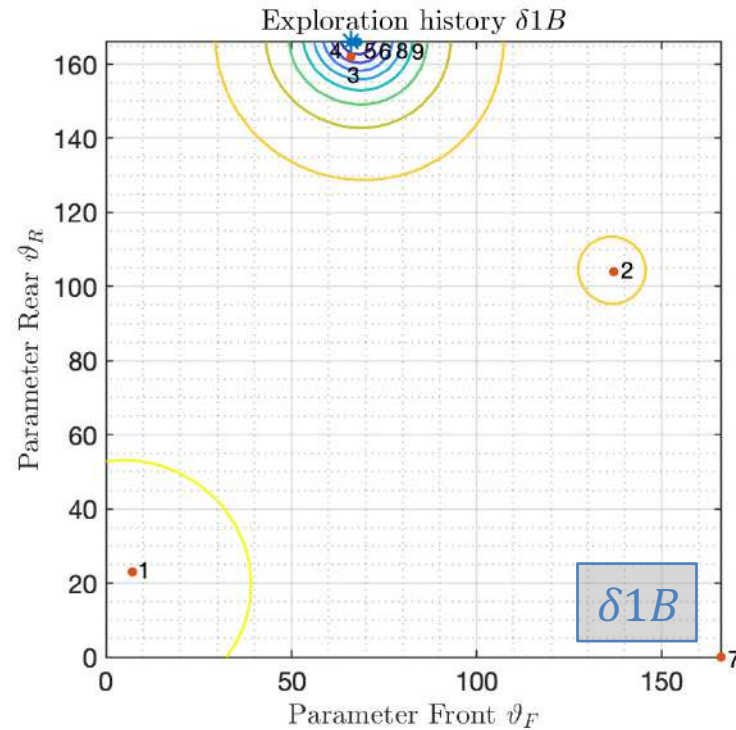
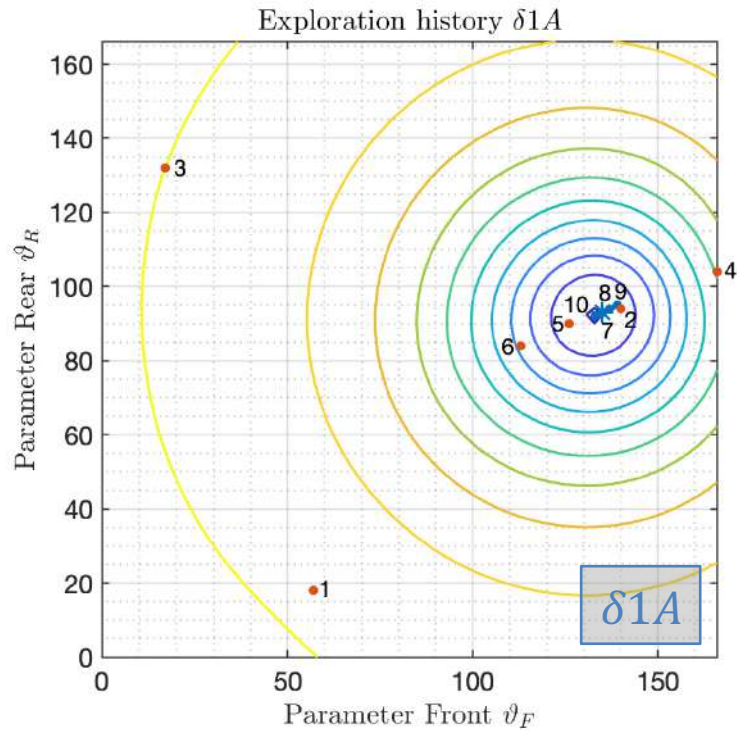
- $\delta = 10$ (2 repetitions) $\rightarrow \delta 10A, \delta 10B$
Best compromise.

- $\delta = 50$ (1 repetition) $\rightarrow \delta 50$
High exploration (too slow convergence) is expected, but most accurate result.



Experimental results

APL Experiment: comparison $\delta = 1$



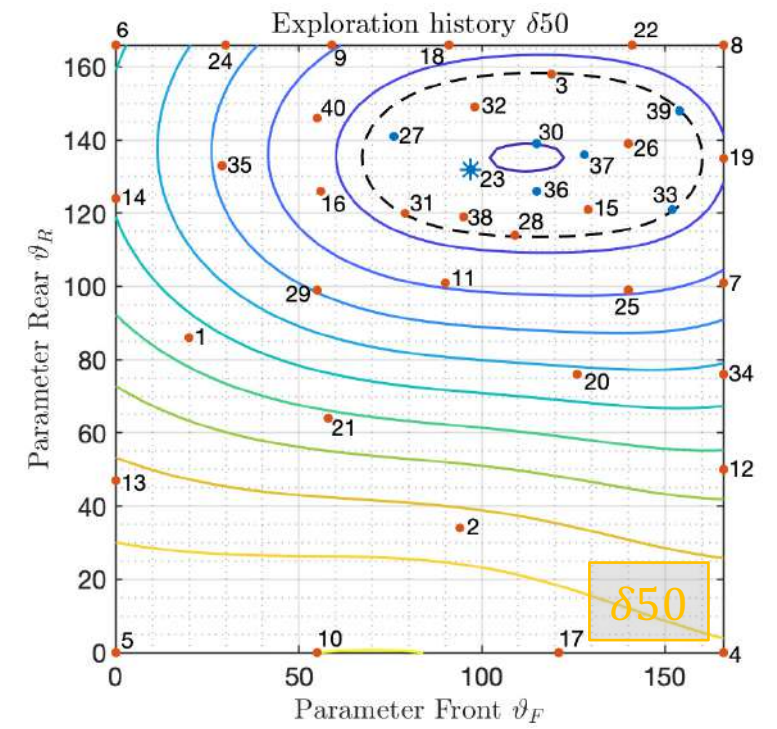
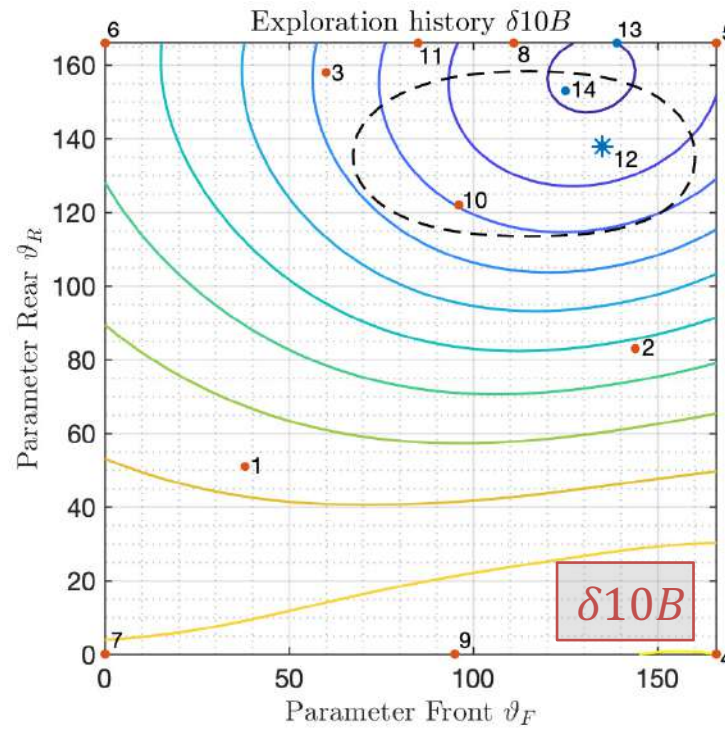
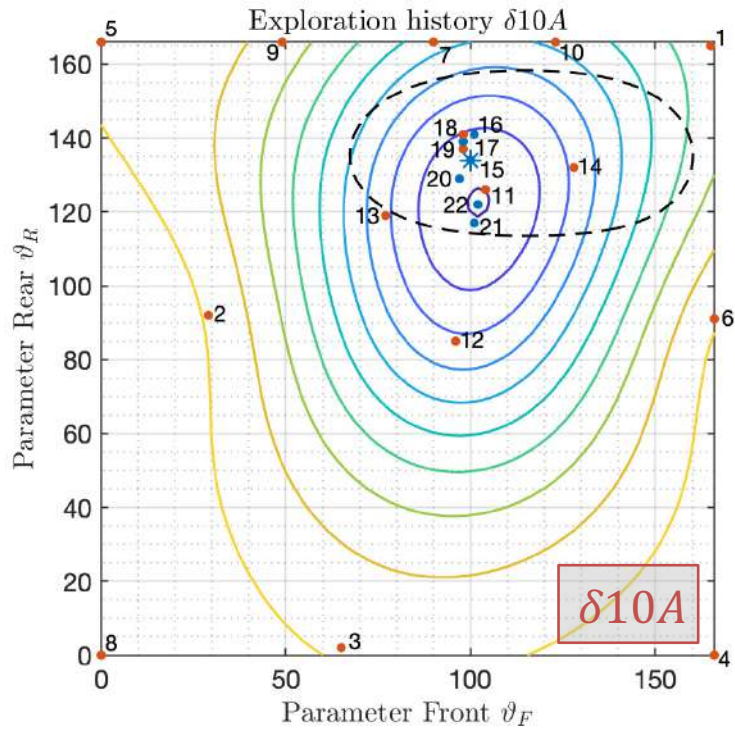
- APL $\delta = 1$ shows poor exploration of parameters space.
- Final result strongly depends on the initialization phase (first 3 samples).

Legend

- Red dots: all samples x_1, \dots, x_N
- ★ Blue star: best preference in-sample x_N^*
- Blue dots: equal-optimum outcomes
- Contour plot is the surrogate function

Experimental results

APL Experiment: comparison $\delta = 10$ / $\delta = 50$



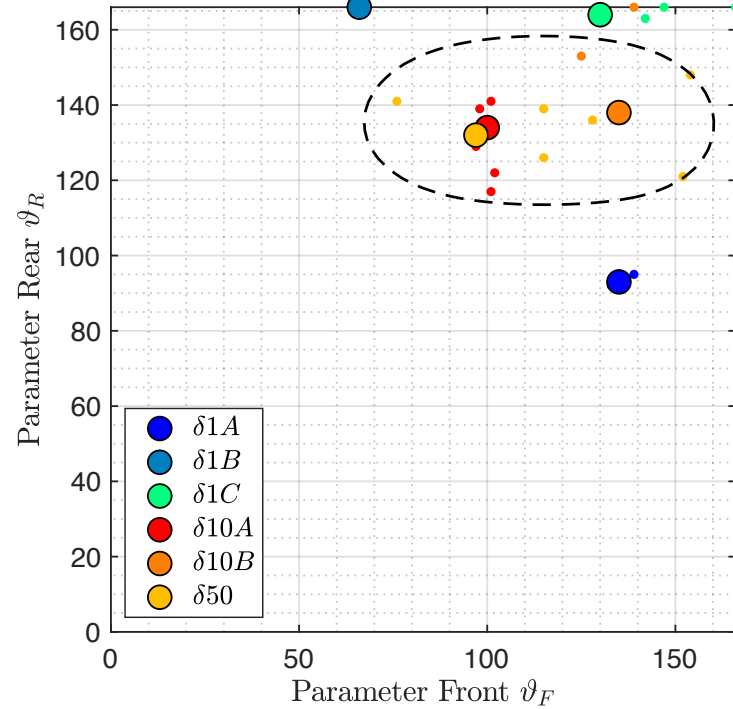
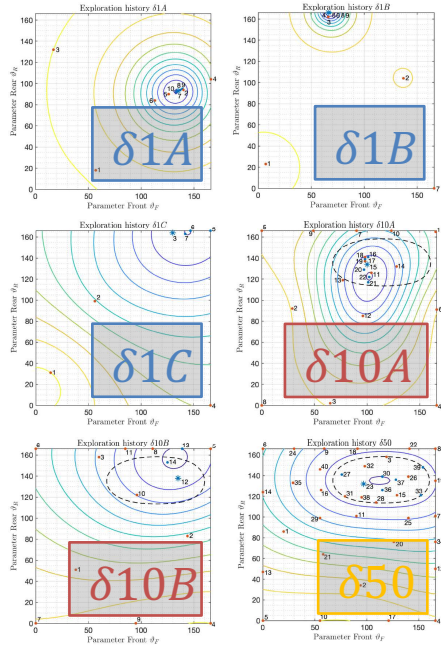
Exploration pattern

- first rule out "bad points" (exploration)
- then surround optimal point (exploitation)

Definition of equal-optimum area from $\delta 50$:
smallest-height contour-line enclosing all
equal-optimum outcomes ($\sigma_f = 0.07$)

Experimental results

APL Experiment



- Confirm poor exploration of $\delta = 1$
- Equal-optimum points with $\delta = 10$ are inside **equal-optimum area**
- $\delta = 10$ best compromise (considering N_{conv})
- Exploration-exploitation trade-off in agreement with simulation

N_{conv}	Simulation	(A)	(B)	(C)	
$\delta = 1$	6	9	8	6	8
$\delta = 10$	15	21	13		17
$\delta = 50$	36		> 39*		/

*budget cap

How to validate/explain this result?

Experimental results

A preference-based comfort index

$$J^\lambda = J^V + \lambda J^P$$
$$J^V = \sqrt{\frac{1}{T} \int_0^T A_z^2 dt}$$
$$J^P = \sqrt{\frac{1}{T} \int_0^T \dot{\varphi}^2 dt}$$

Learn weighting coefficient λ from preference

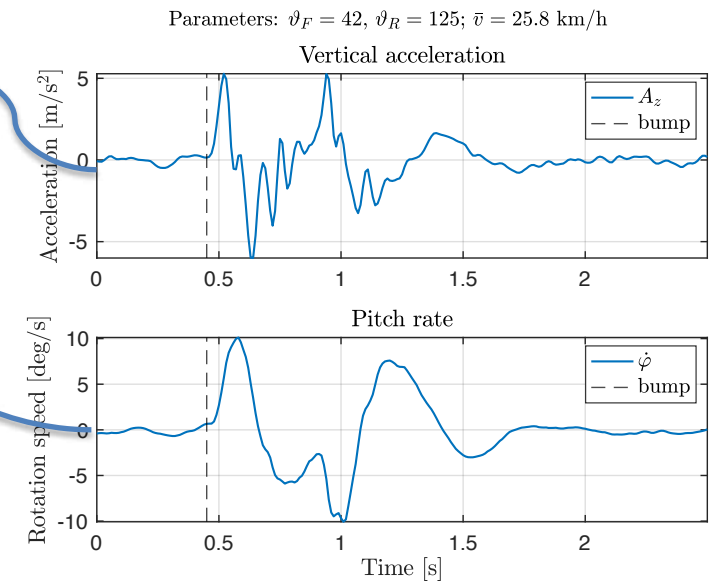


Supervised multiclass classification problem

- $u = [J_{hi}^V \ J_{hi}^P \ J_{hj}^V \ J_{hj}^P]$ input
- $y \in \{-1, 0, 1\}$ output
 $\Rightarrow D = \{(u_1, y_1), \dots, (u_K, y_K)\}$ dataset

Vertical acceleration RMS

Pitch rate RMS



- $\tilde{\pi}: U \rightarrow Y$ interpretation function

$$\tilde{\pi}(u) = \begin{cases} -1 & \text{if } J_i^\lambda - J_j^\lambda < -\sigma_J \\ 0 & \text{if } |J_i^\lambda - J_j^\lambda| \leq \sigma_J \\ 1 & \text{if } J_i^\lambda - J_j^\lambda > \sigma_J \end{cases}$$

Experimental results

A preference-based comfort index

Learning procedure

Slack-variable minimization problem, which constraints imposes:

$$\tilde{\pi}(x_h) = y_h, \forall h = 1, \dots, K$$

$$\begin{aligned} & \text{minimize} && \varepsilon \\ & \lambda, \sigma_J, \varepsilon \\ & \text{subject to} && J_{hi}^V + \lambda J_{hi}^P - J_{hj}^V - \lambda J_{hj}^P \leq -\sigma_J + \varepsilon_h \quad \forall h : y_h = -1, \\ & && J_{hi}^V + \lambda J_{hi}^P - J_{hj}^V - \lambda J_{hj}^P \geq \sigma_J - \varepsilon_h \quad \forall h : y_h = 1, \\ & && J_{hi}^V + \lambda J_{hi}^P - J_{hj}^V - \lambda J_{hj}^P \leq \sigma_J + \varepsilon_h \quad \forall h : y_h = 0, \\ & && J_{hi}^V + \lambda J_{hi}^P - J_{hj}^V - \lambda J_{hj}^P \geq -\sigma_J - \varepsilon_h \quad \forall h : y_h = 0, \\ & && \lambda \geq 0, \sigma_J \geq 10^{-6}, \varepsilon \geq 0 \end{aligned}$$

→ λ (and σ_J)

Cross-validation procedure

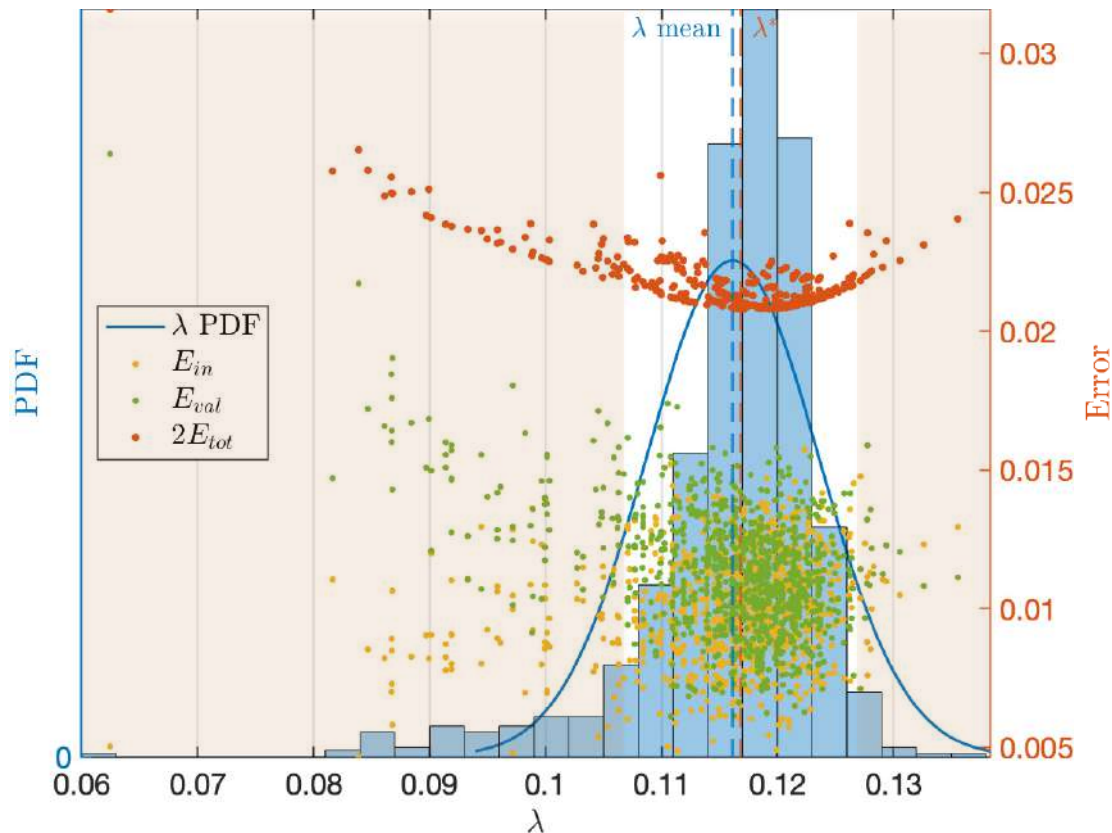
- Training set → to train the model solving optimization pb.
- Validation set → to detect overfitting (E_{val}).

Mean prediction error:
measure how far is the
model from correct label
prediction

Experimental results

A preference-based comfort index

J^λ from dataset Driver1
(113 preference data)



- E_{tot} has a convex quadratic-like shape.
⇒ best $\lambda^* = 0.117$.
- λ far from λ^* are outliers (big E_{val} → overfitting)
- Model J^λ cannot make $E_{tot} = 0$ because of noise
 - regressors (sensors measurements)
 - labels (human preference)



$\lambda \approx 0.12$

Experimental results

BO with J^λ Experiment

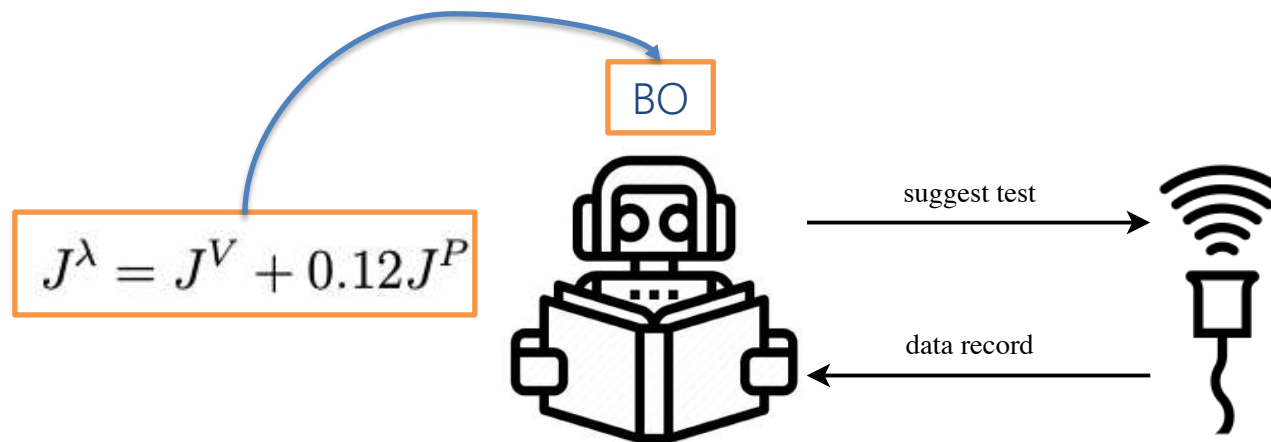
BO with J_λ Experiment:

- 1) Automatic calibration via BO with J^λ .
- 2) Check if BO optimum is similar to APL → results validation.



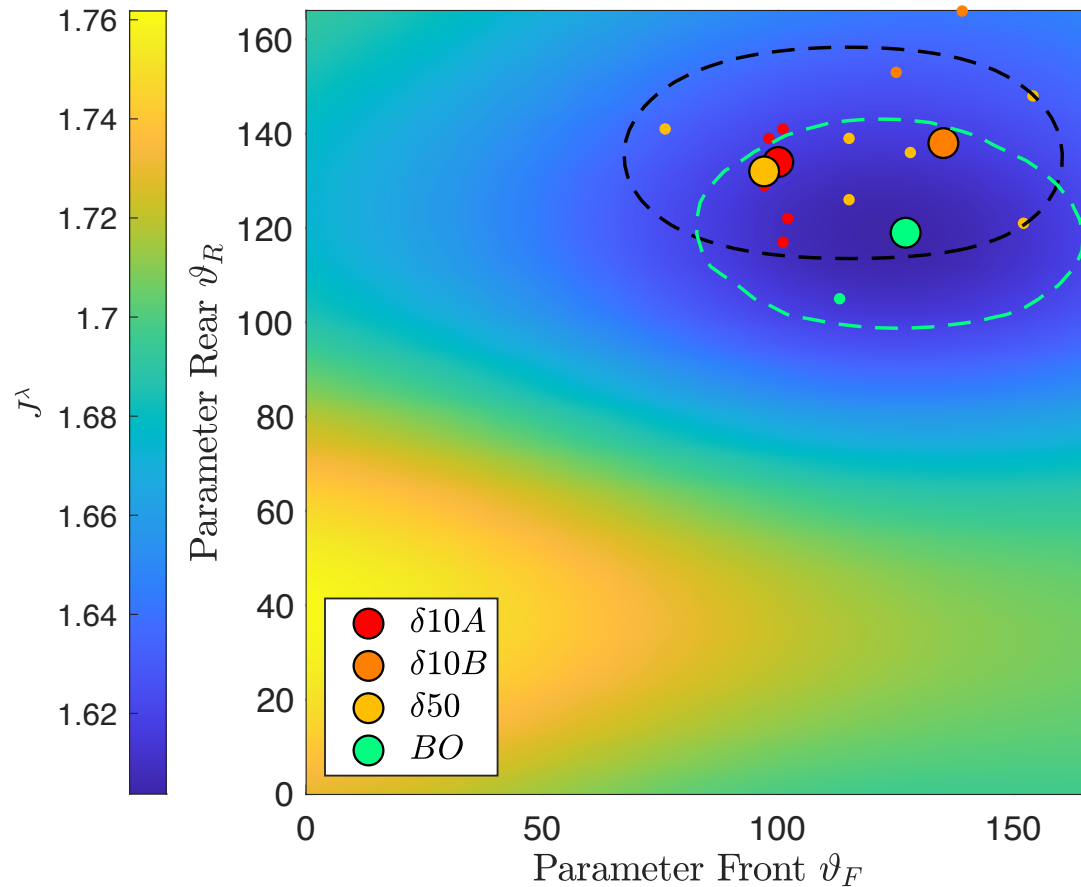
Same experimental setup.

Same scenario: bump test at 30 km/h.



Experimental results

APL Vs BO



- equal-optimum area from APL
- equal-optimum area from BO

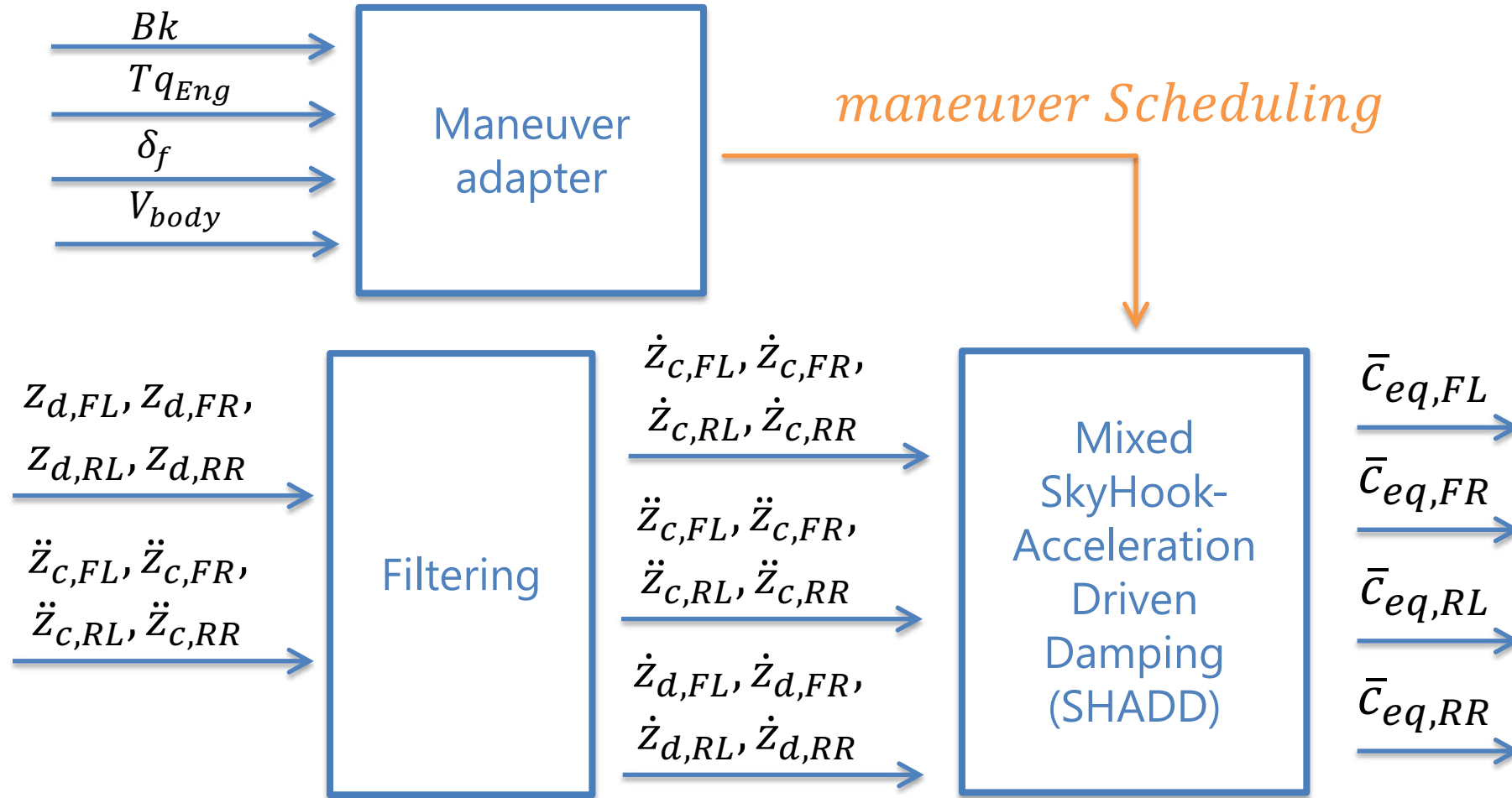
- J^λ gives interpretation of APL result
→ model of driver preference
- APL with $\delta \geq 10$ retrieve optimal solution according to J^λ

APL is time/cost effective

- BO ~40 min Vs
- APL ~50 min (but...)

Semi-Active Damping Control

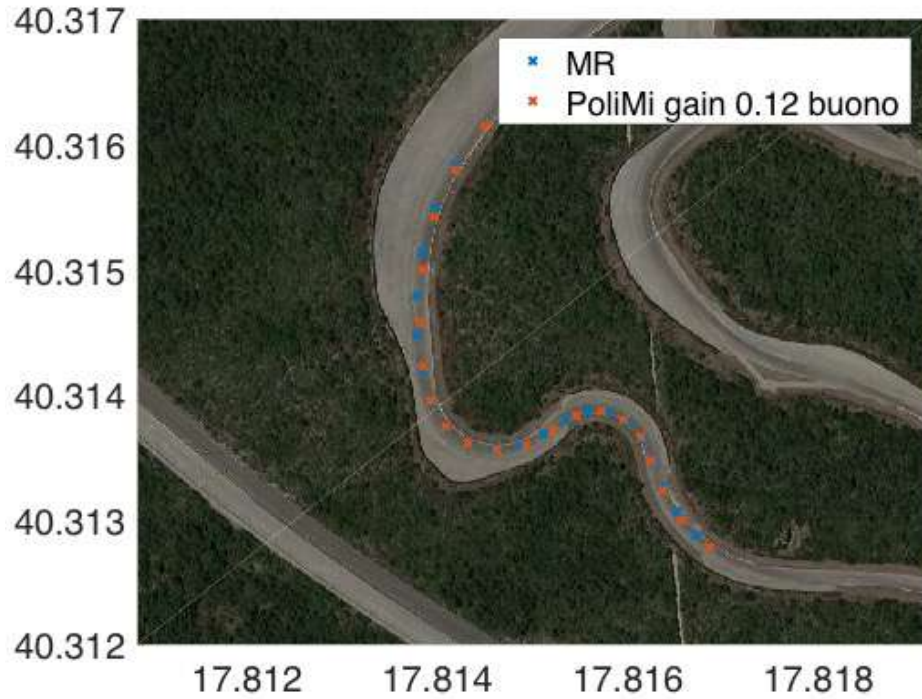
Full Body Control



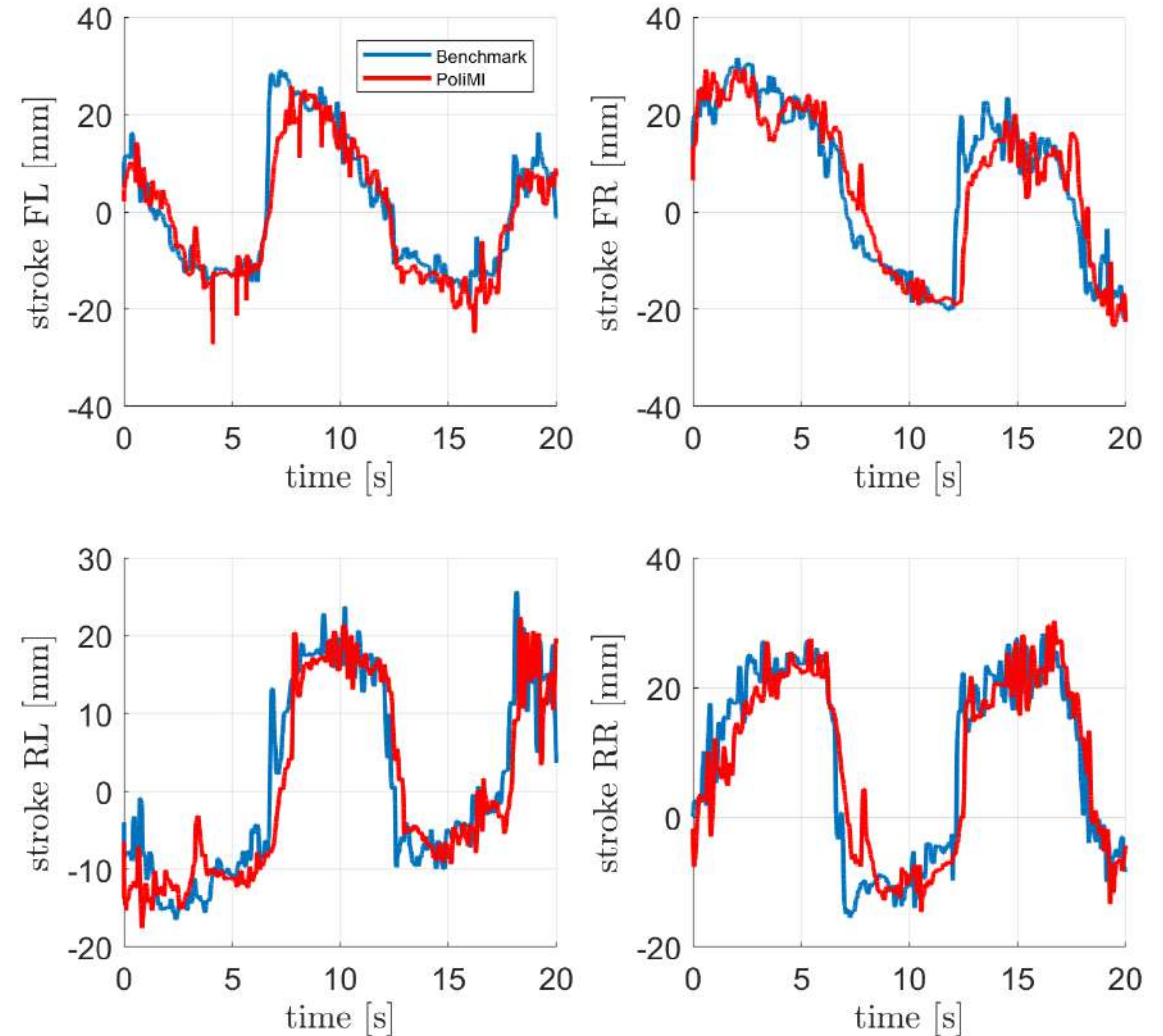
$$c_{ref} = \text{sat}_{[c_{min}, c_{max}]}(c_{nom} + k_{SH}\dot{z}_b\Delta z + k_{ADD}\ddot{z}_b\Delta z)$$

Semi-Active Damping Control

Full Body Control



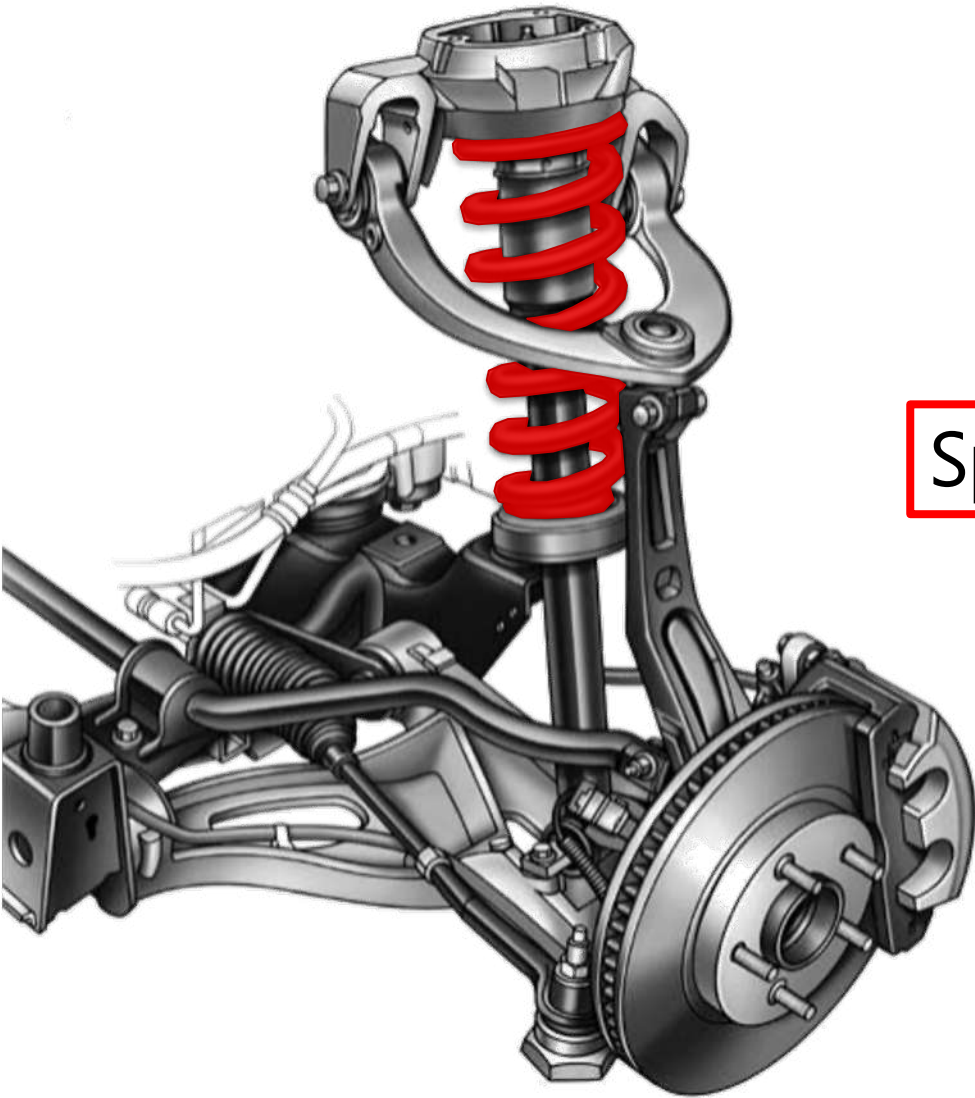
Thanks to the use of the driver scheduling, it is possible to slow down the load transfer and thus yield a more stable feeling while negotiating corners.



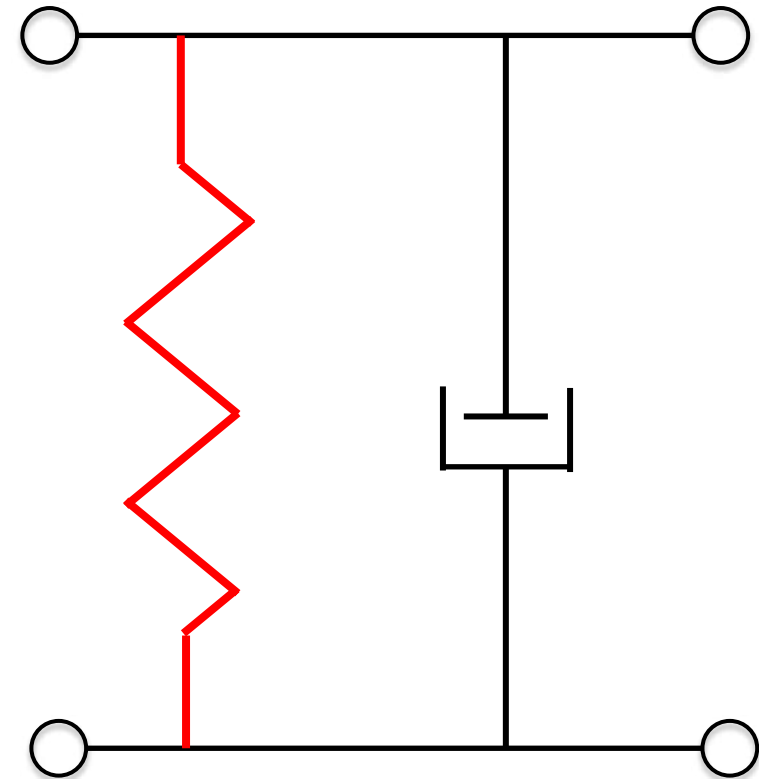
- Introduction
- Semi-Active Damping Control
 - Actuators
 - Models
 - Benchmark
 - Causal Control
- **Semi-Active Stiffness Control**
 - Actuators
 - Benchmark
 - Causal Control
- Sensing Preliminaries
- A look at the future
- Conclusions

Semi-Active Stiffness Control

Actuators



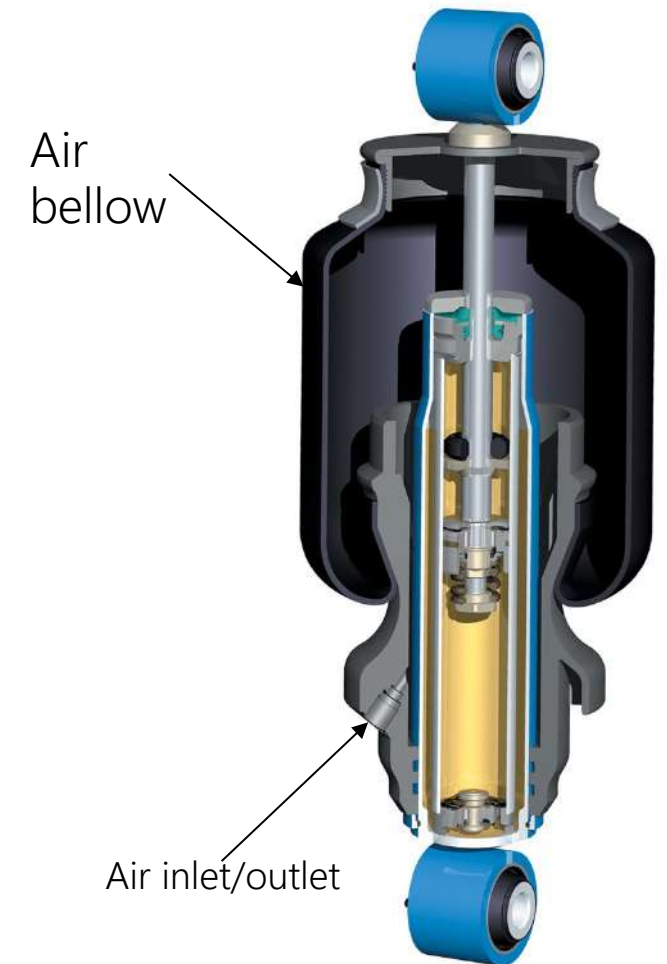
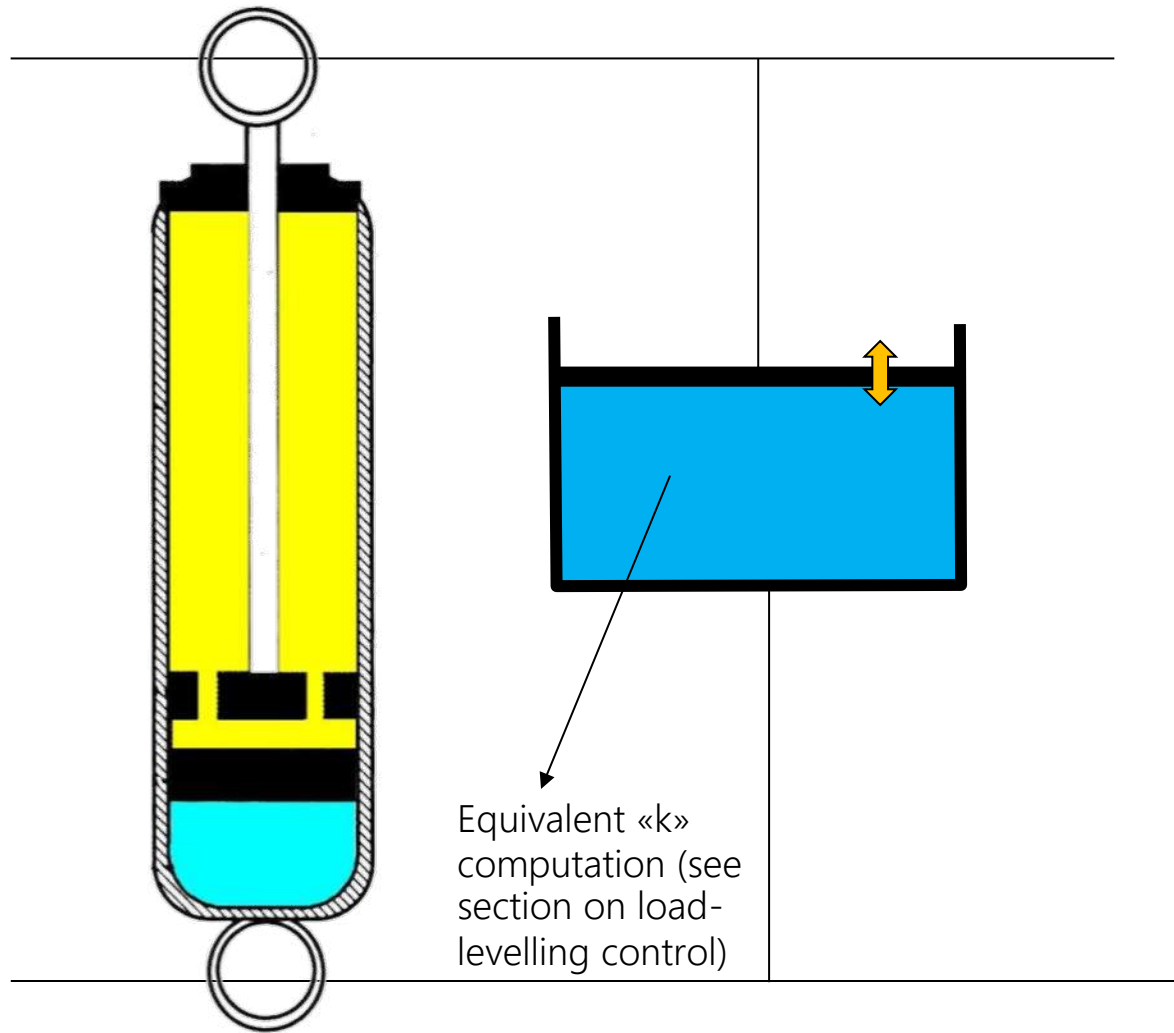
Spring (k)



A mechanical spring does not allow for any kind of modulation

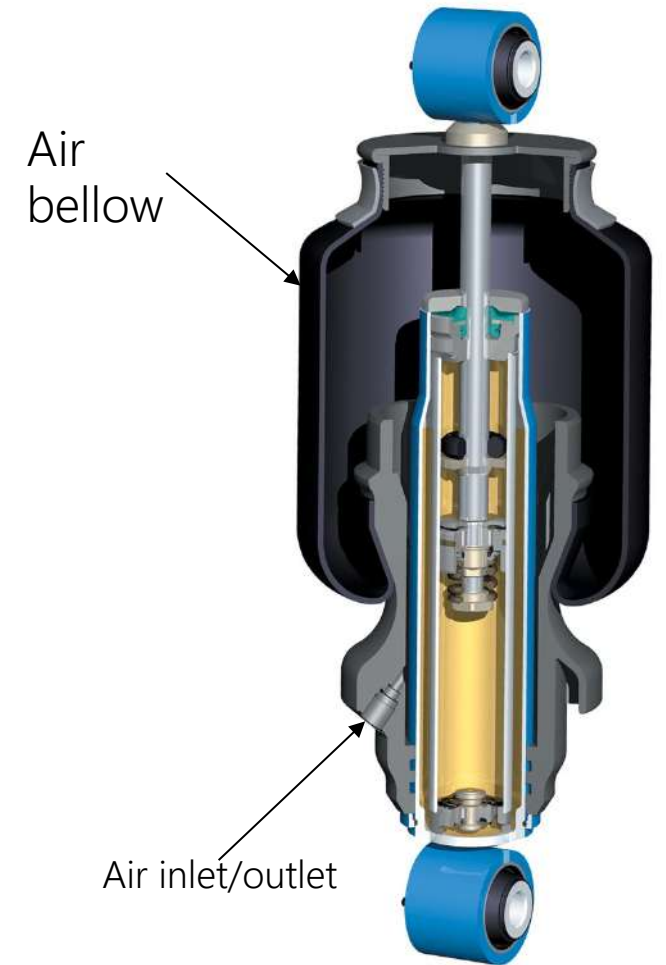
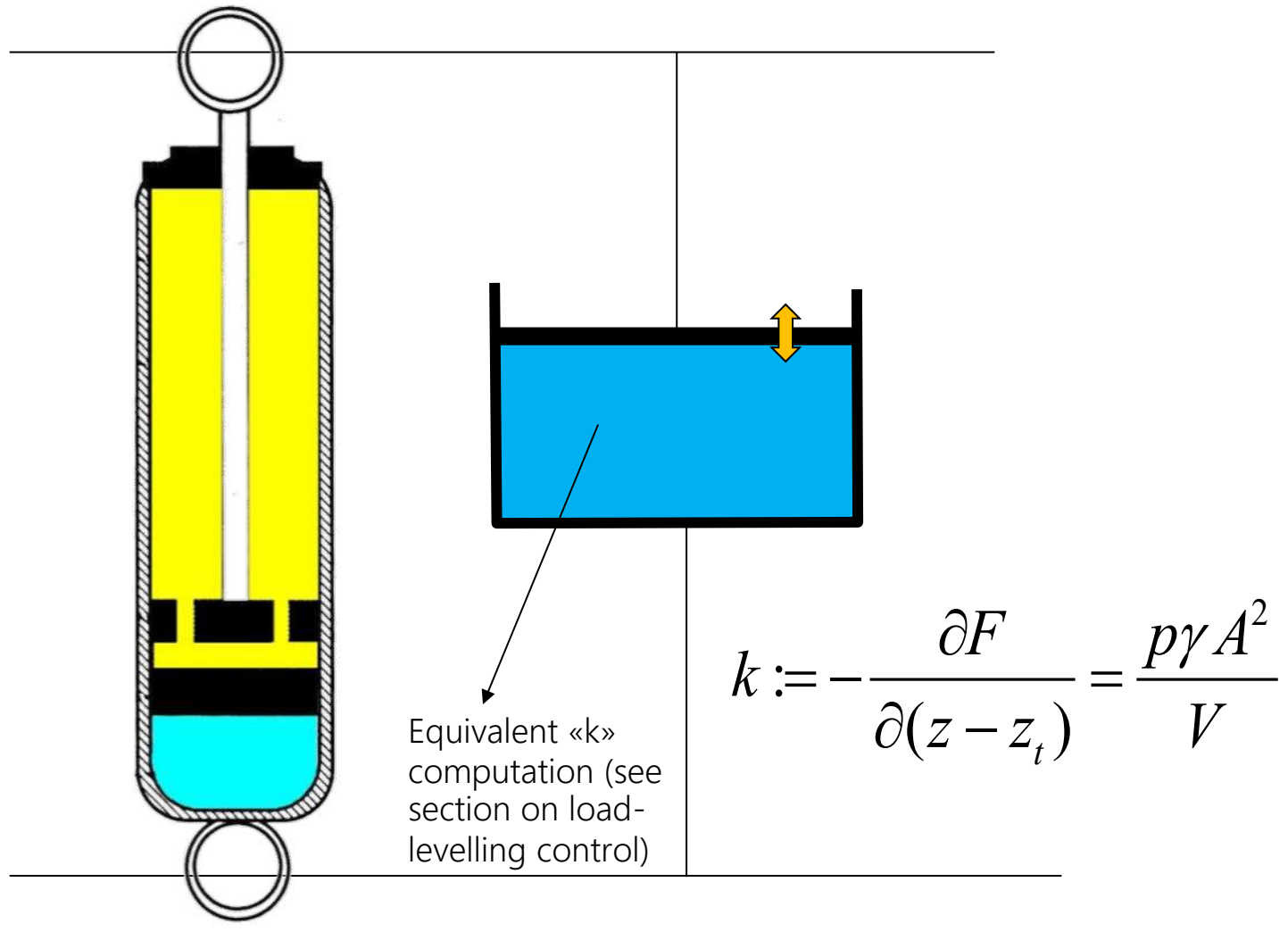
Semi-Active Stiffness Control

Air Spring – Pneumatic Spring



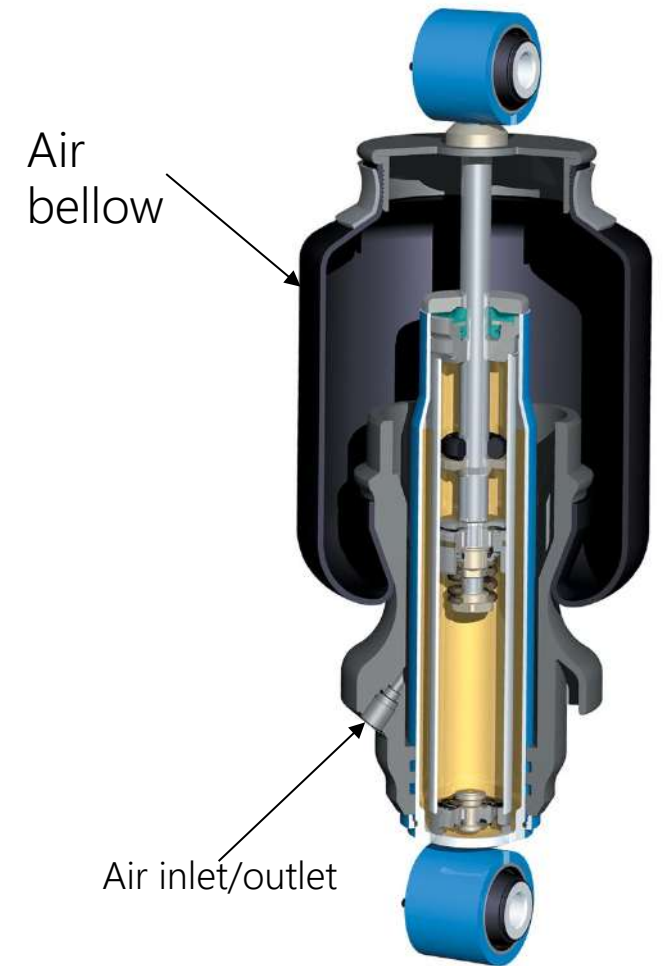
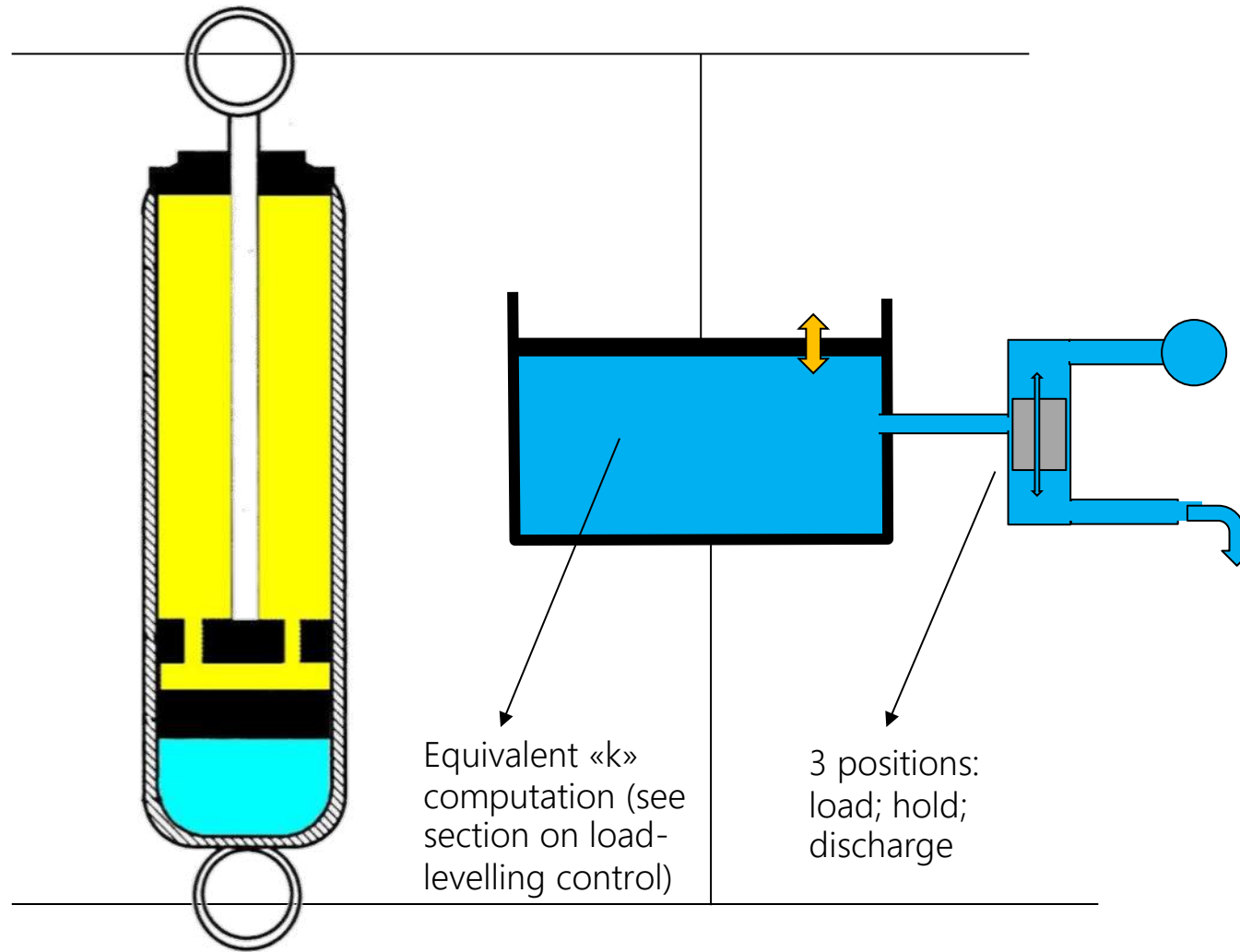
Semi-Active Stiffness Control

Air Spring – Pneumatic Spring



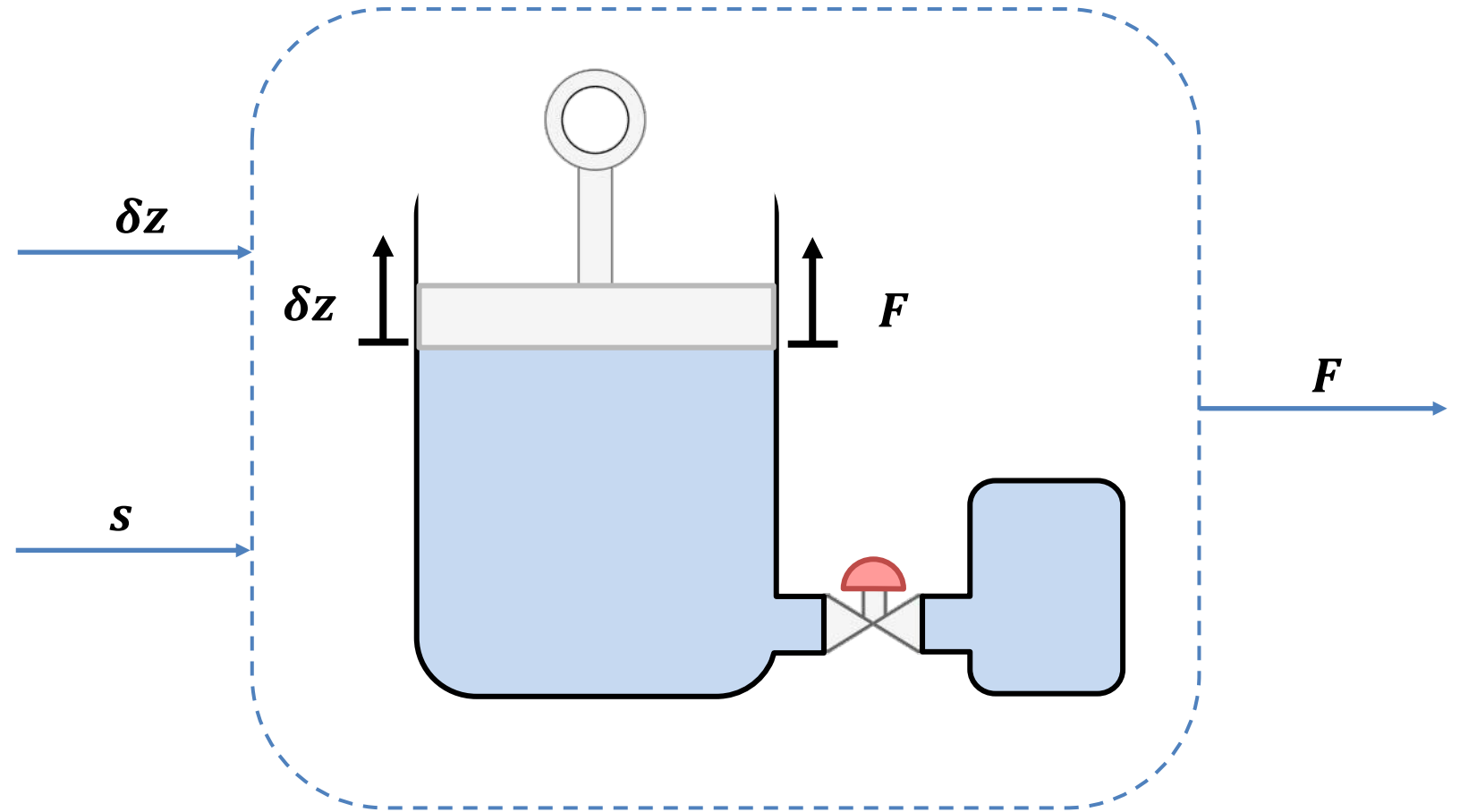
Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Slow Active



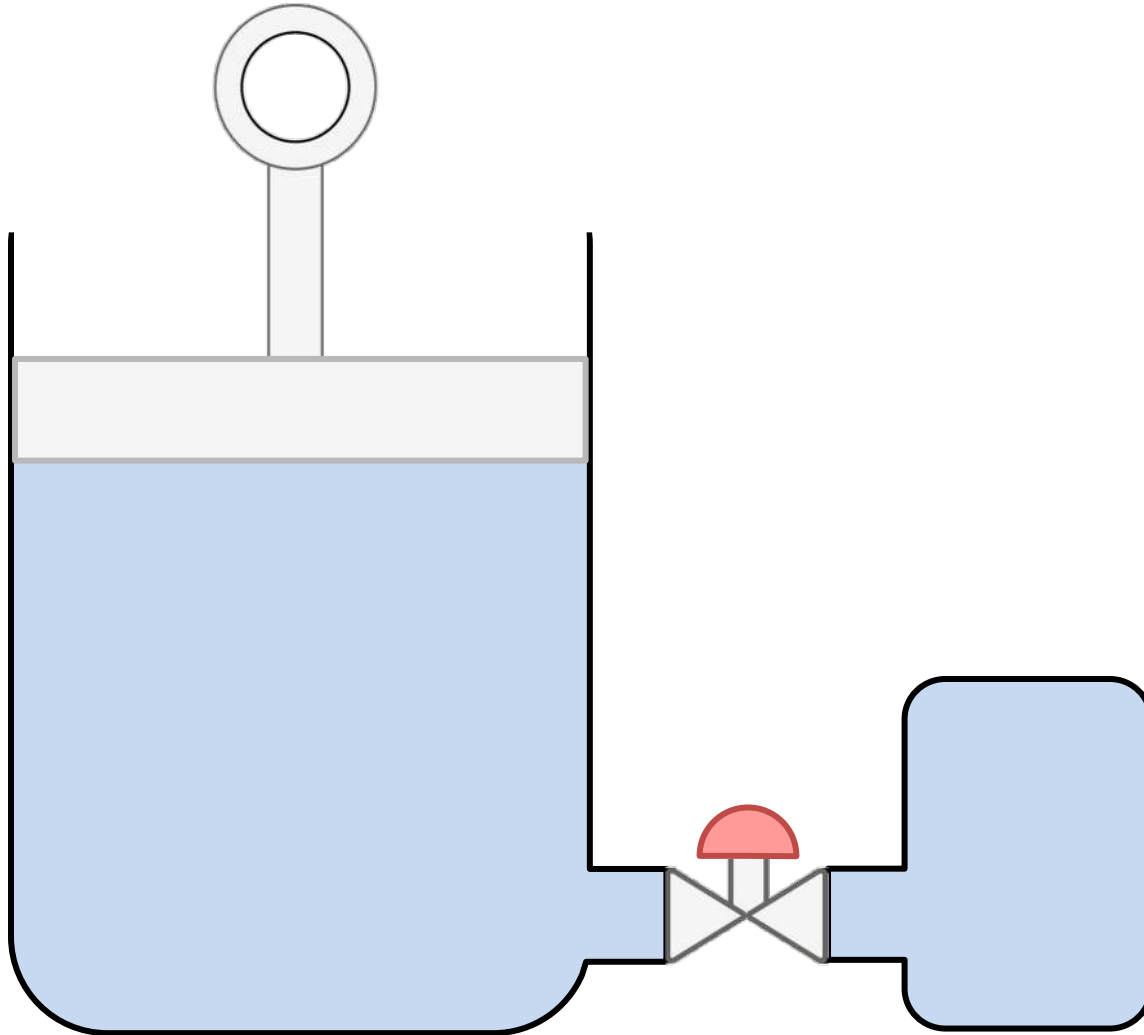
Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active



Semi-Active Stiffness Control

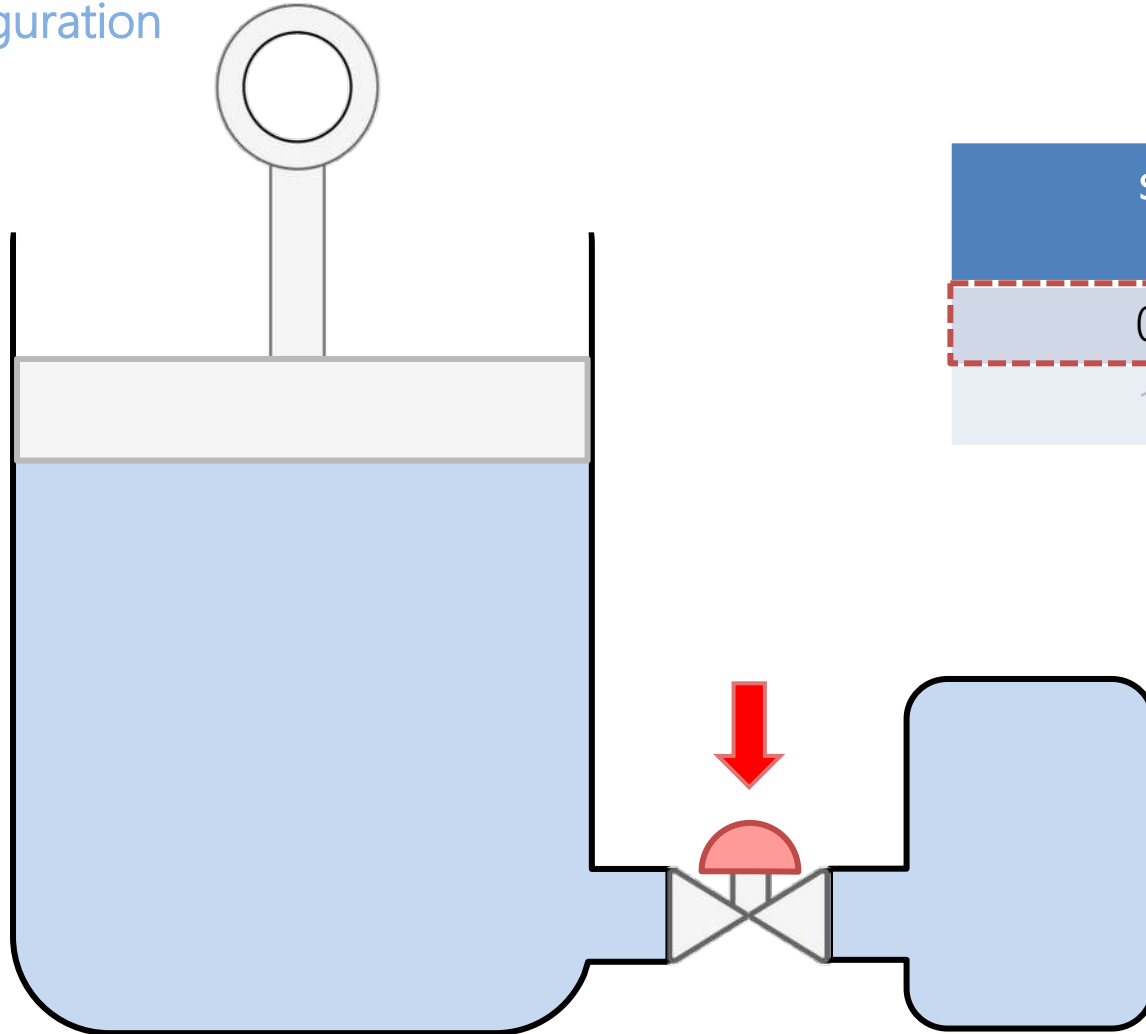
Air Spring – Pneumatic Spring – Semi-Active



Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active

Hard configuration

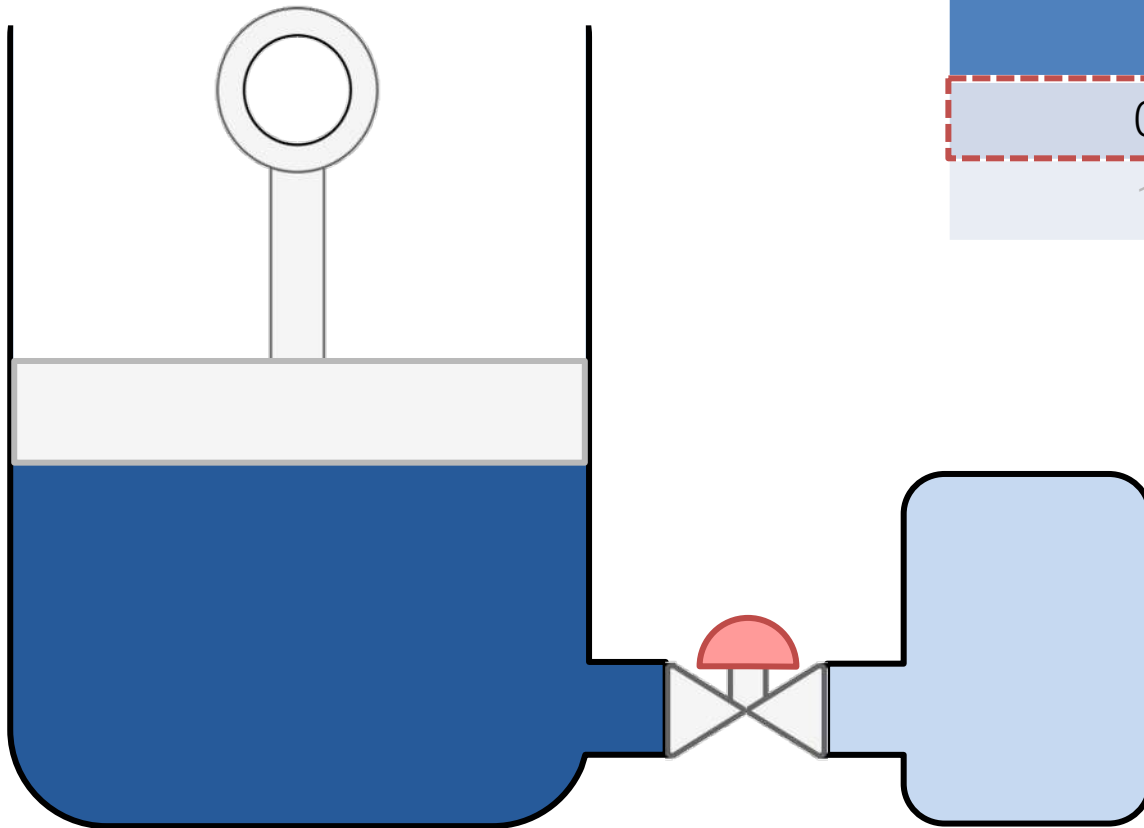


s	Valve configuration	System configuration
0	Closed	Hard
1	Open	Soft

Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active

Hard configuration

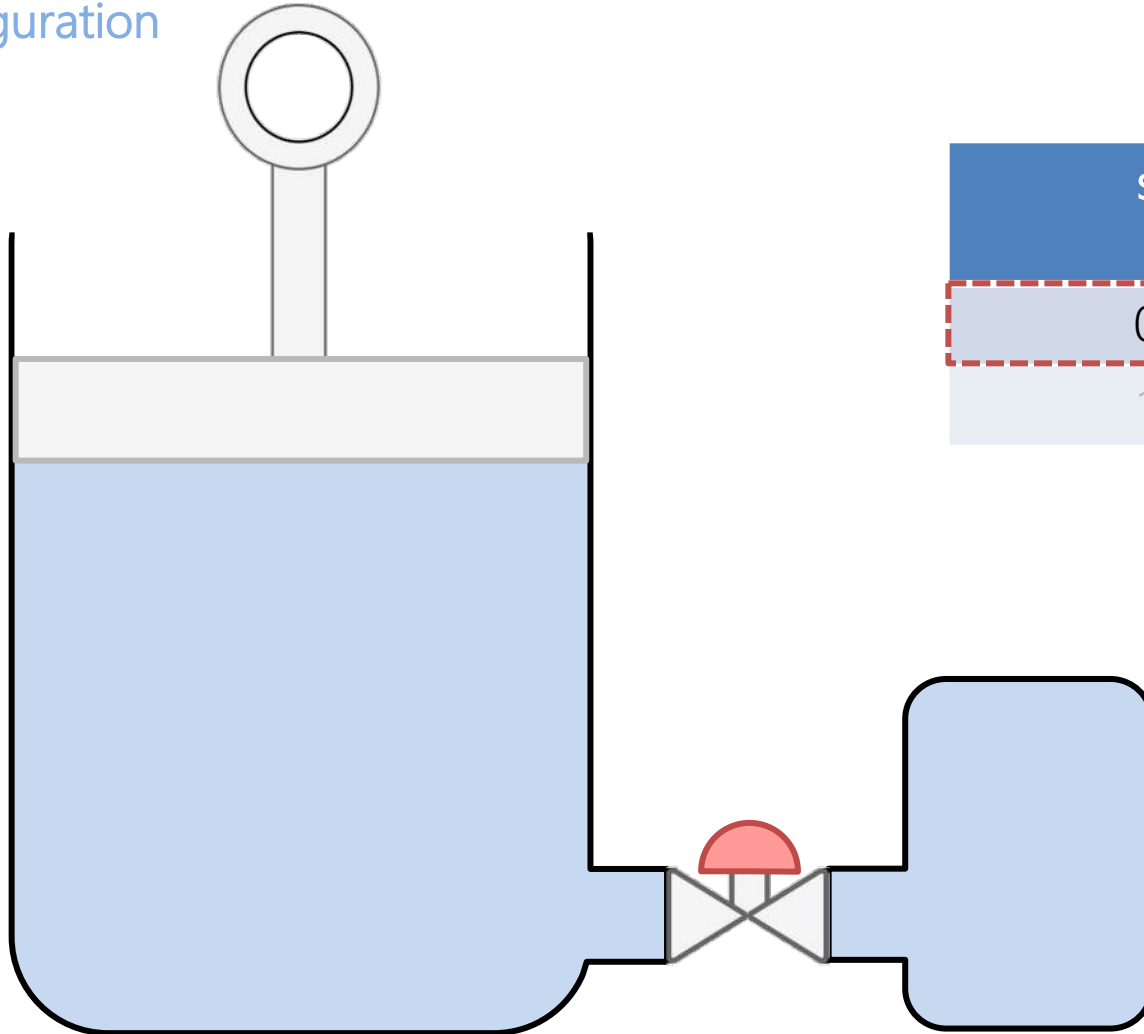


s	Valve configuration	System configuration
0	Closed	Hard
1	Open	Soft

Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active

Hard configuration

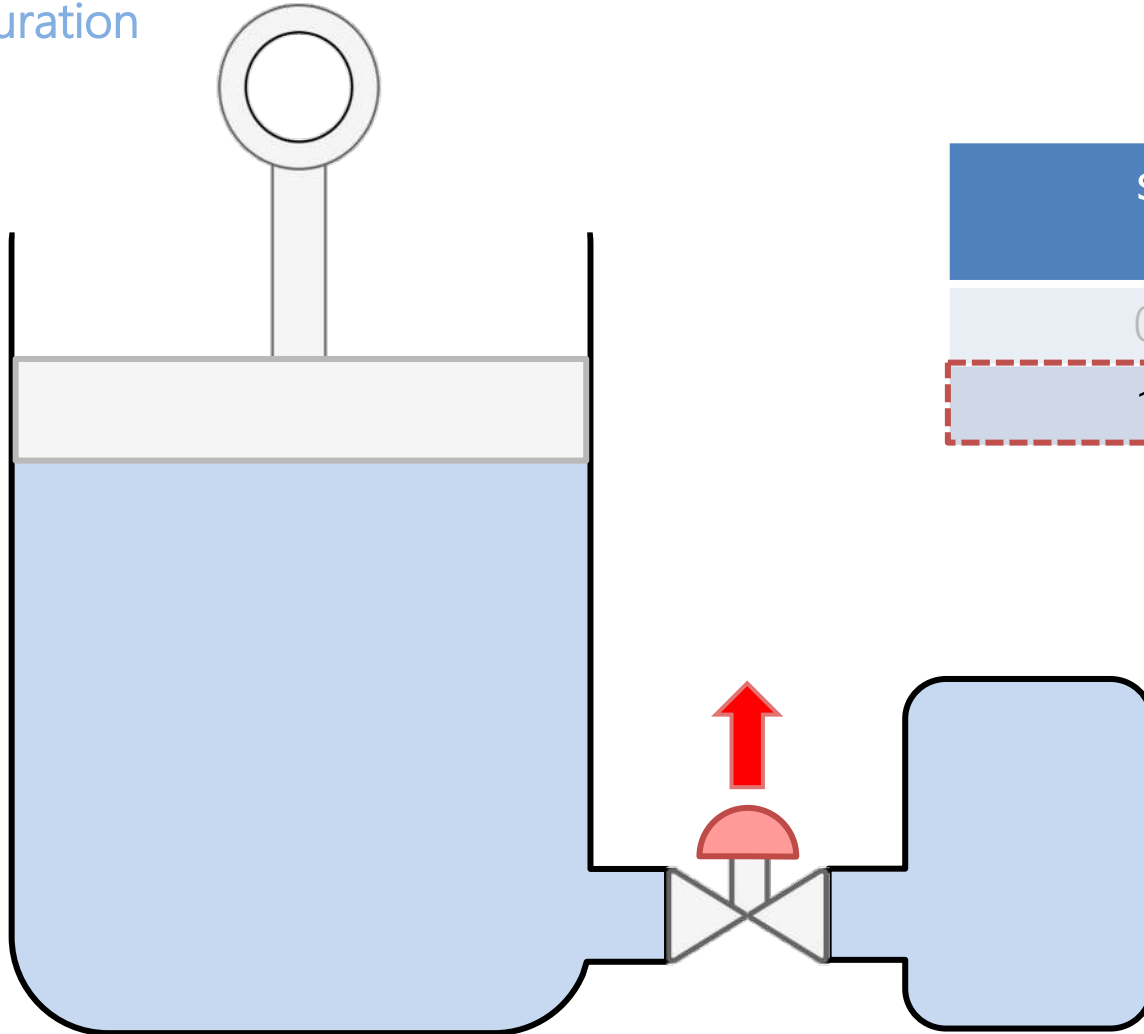


s	Valve configuration	System configuration
0	Closed	Hard
1	Open	Soft

Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active

Soft configuration

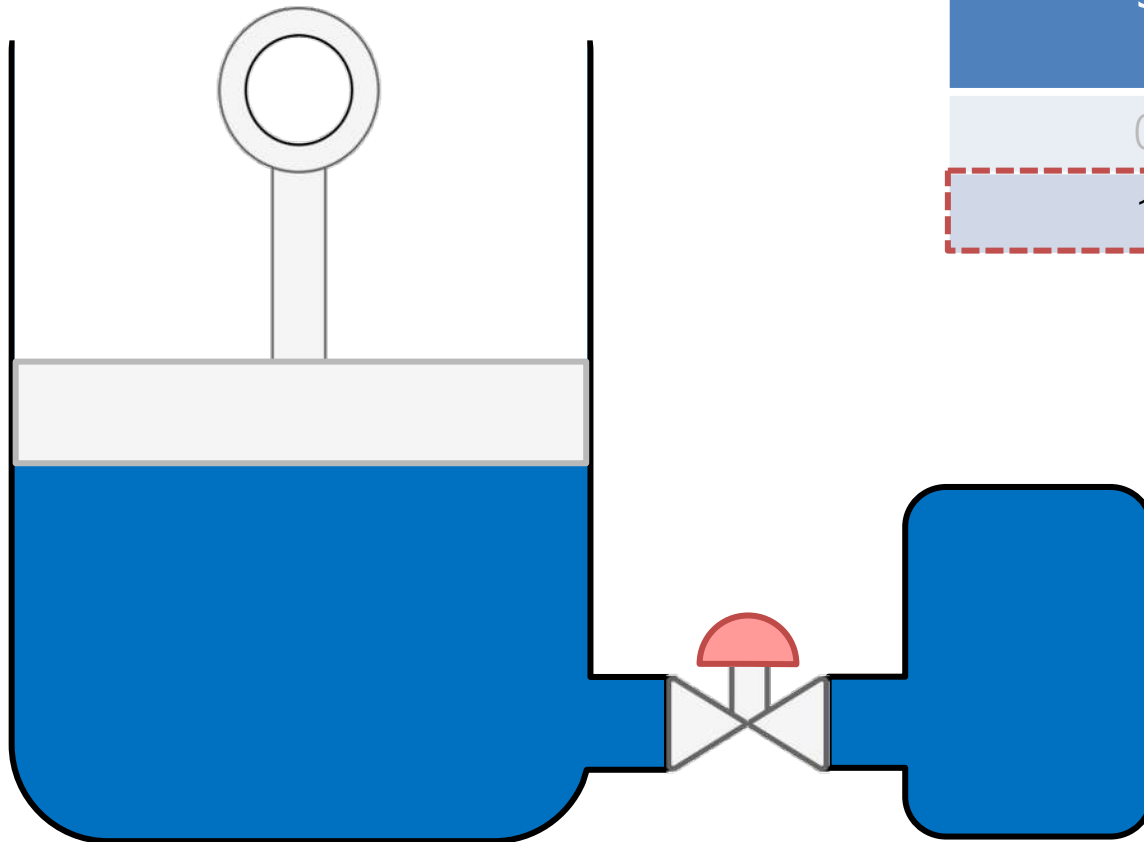


s	Valve configuration	System configuration
0	Closed	Hard
1	Open	Soft

Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active

Soft configuration

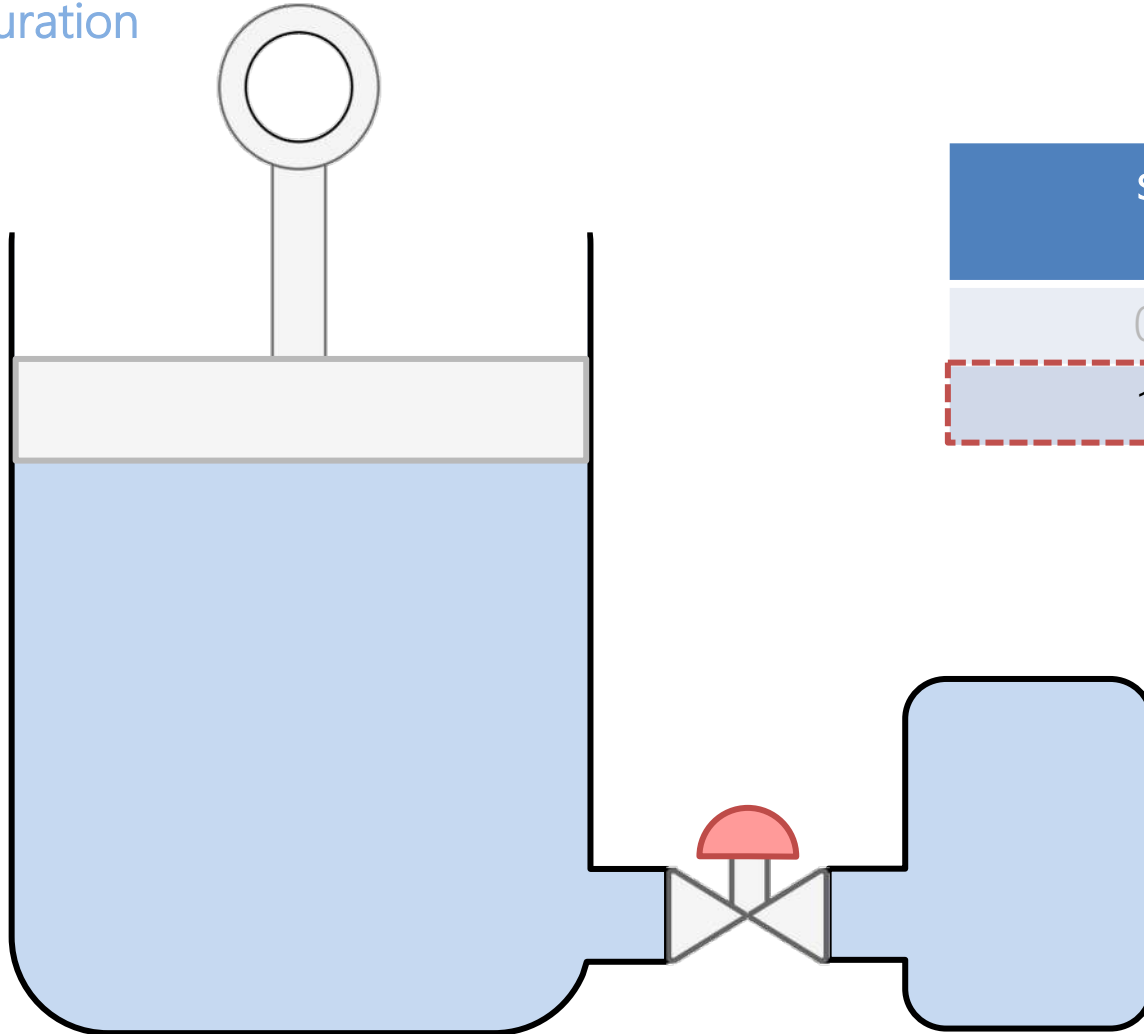


s	Valve configuration	System configuration
0	Closed	Hard
1	Open	Soft

Semi-Active Stiffness Control

Air Spring – Pneumatic Spring – Semi-Active

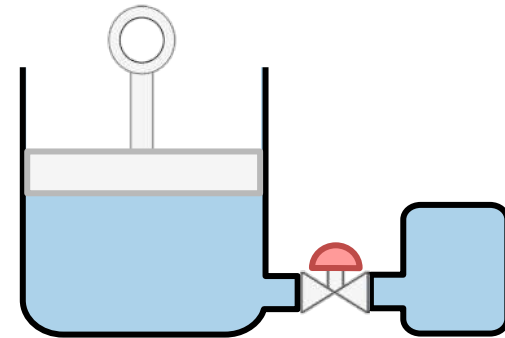
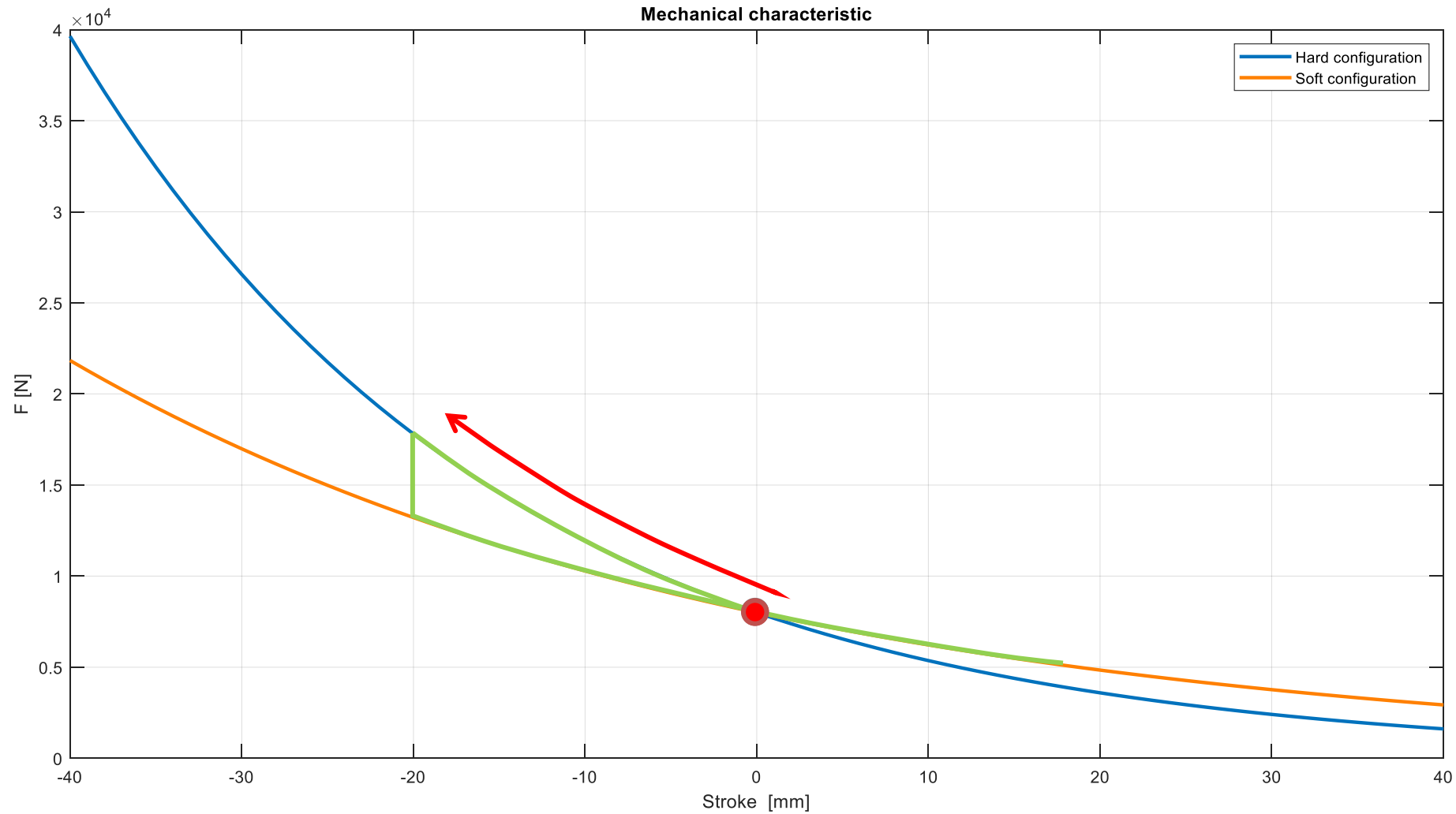
Soft configuration



s	Valve configuration	System configuration
0	Closed	Hard
1	Open	Soft

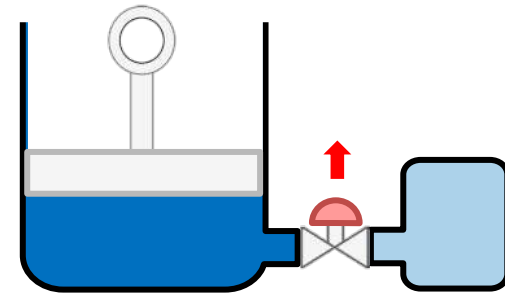
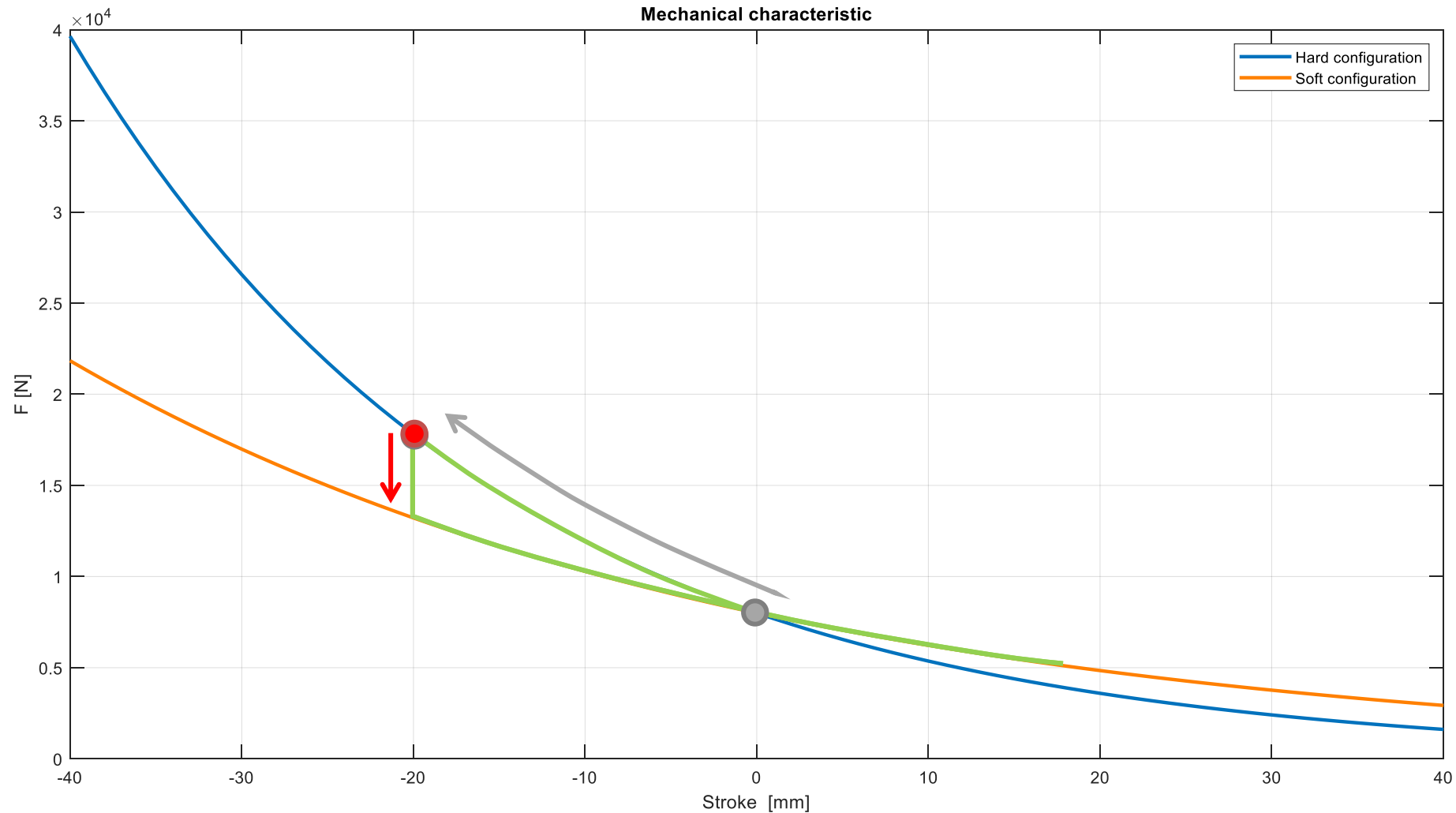
Semi-Active Stiffness Control

Kick-back



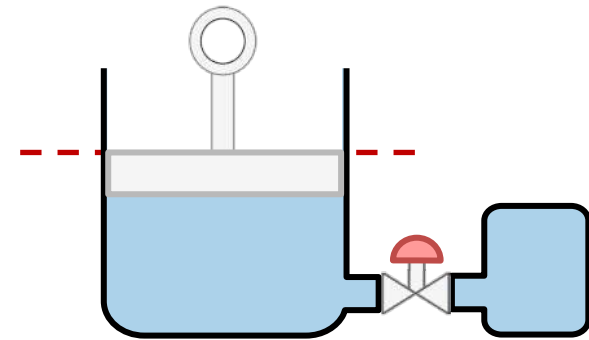
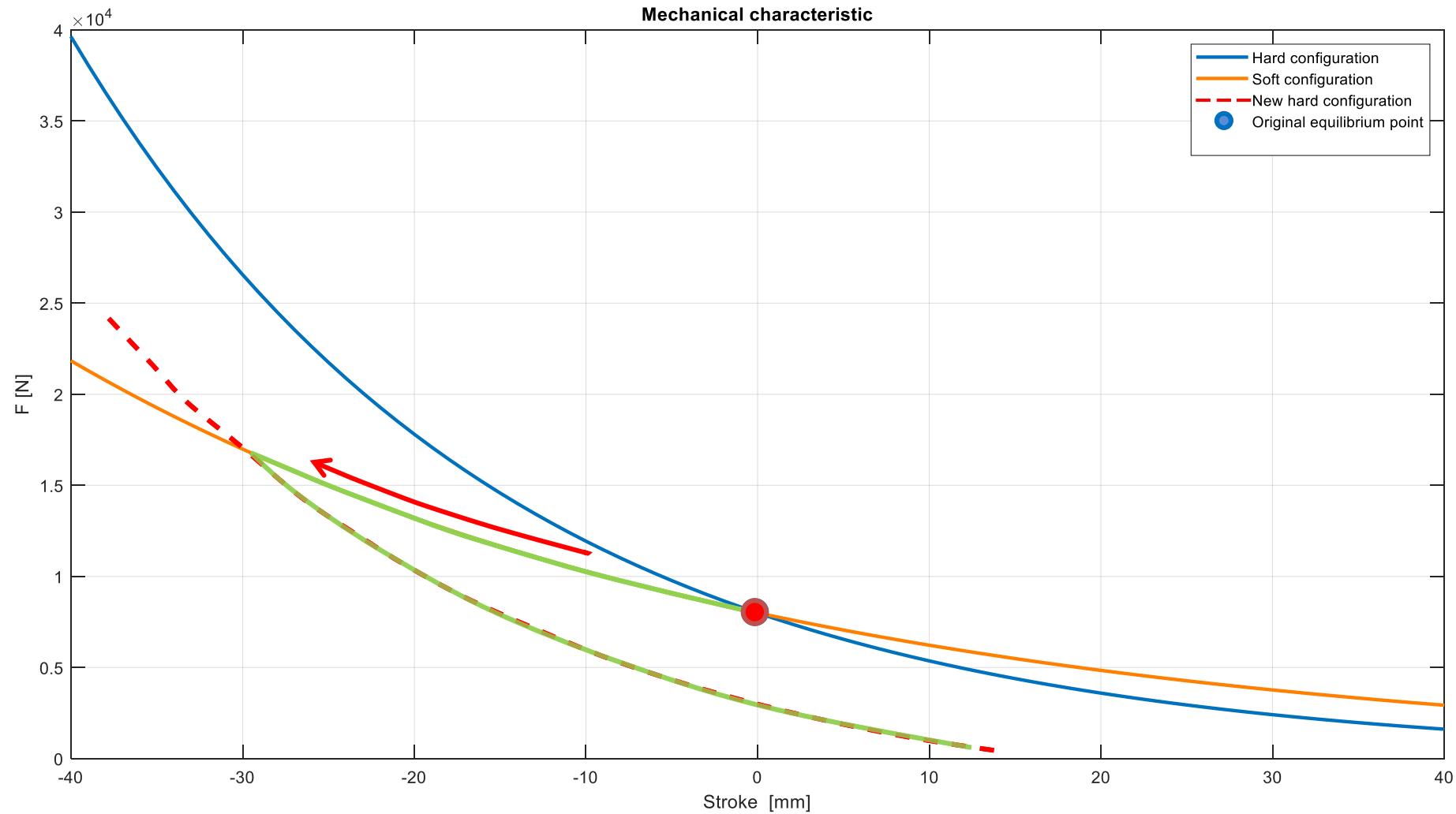
Semi-Active Stiffness Control

Kick-back



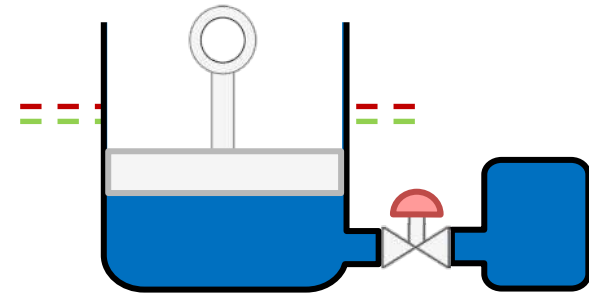
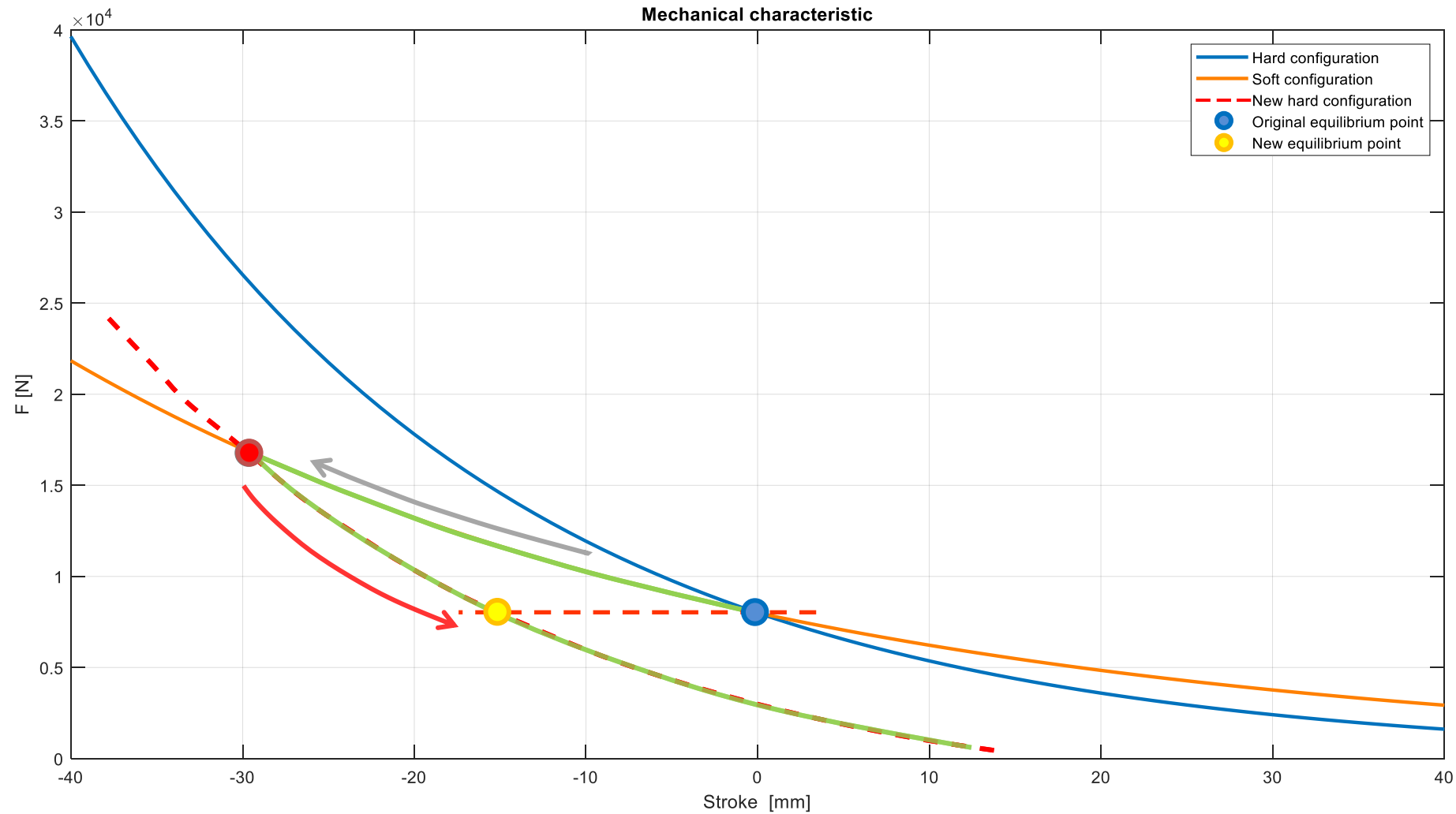
Semi-Active Stiffness Control

Kick-back



Semi-Active Stiffness Control

Kick-back



Law of ideal gases

$$pV = mRT$$

Law of conservation of energy

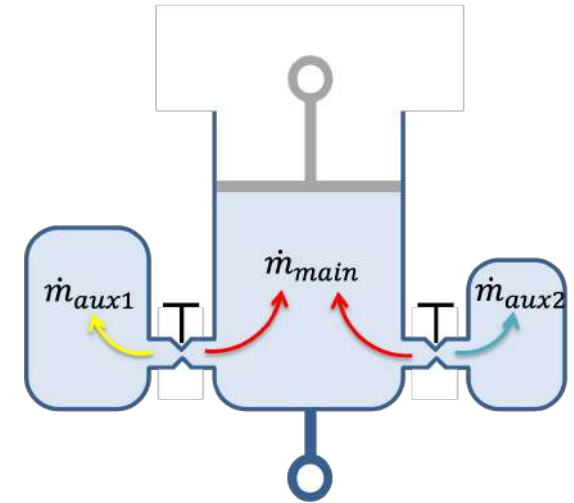
$$\delta U = \delta Q + \delta H - \delta W$$

Law of conservation of mass

$$\dot{m}_{main} + \dot{m}_{aux1} + \dot{m}_{aux2} = const.$$

Flow through valves

$$q_{m,i}^{sub} = s_i A_v C_v p_{max} \sqrt{\frac{2\gamma}{RT_{up}(\gamma - 1)} \left[\left(\frac{p_{min}}{p_{max}} \right)^{\frac{2}{\gamma}} - \left(\frac{p_{min}}{p_{max}} \right)^{\frac{\gamma+1}{\gamma}} \right]}$$



Semi-Active Stiffness Control

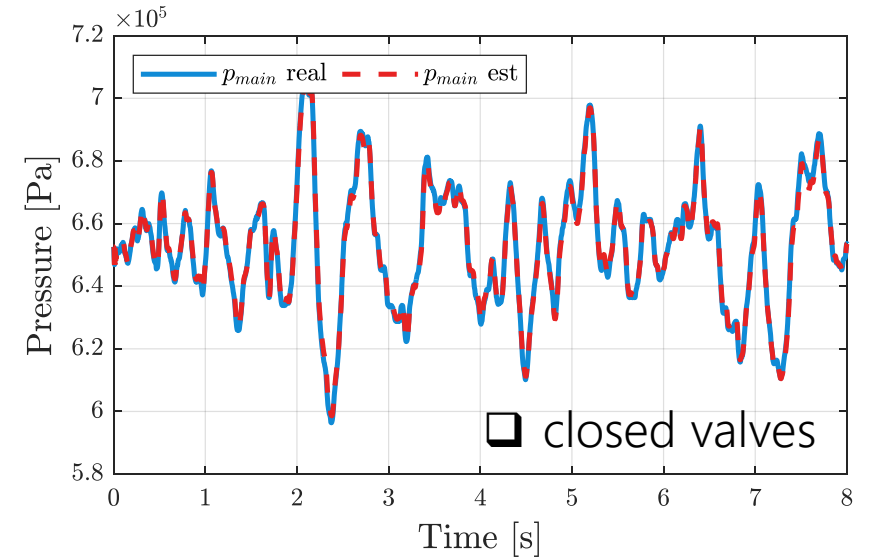
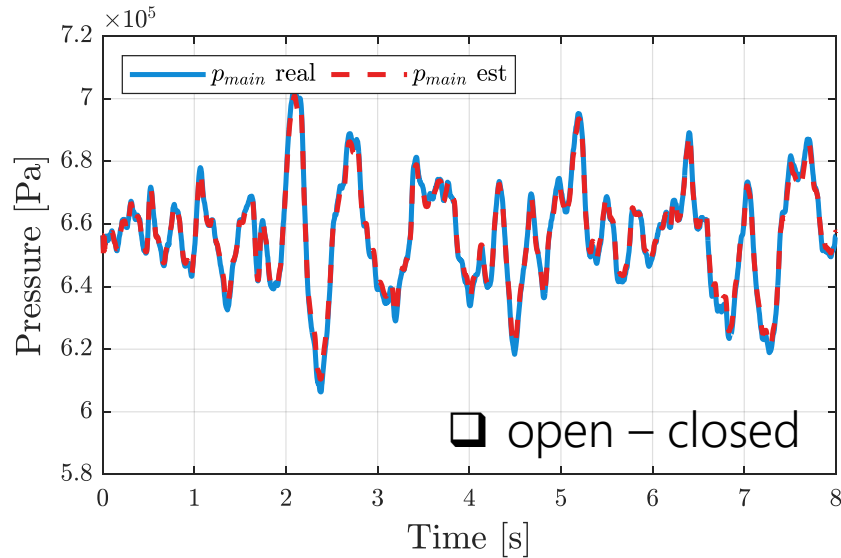
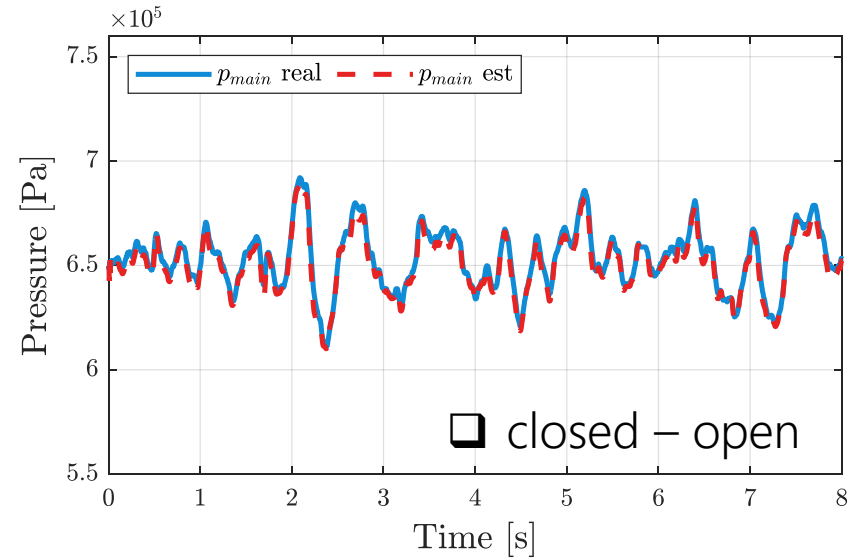
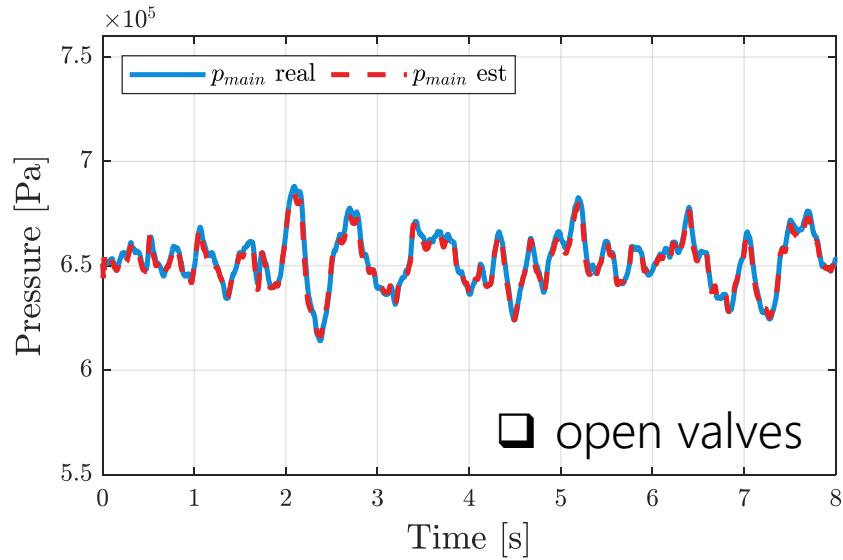
Model Identification

$$\left\{ \begin{aligned}
 \dot{p}_{main} &= -\frac{\gamma p_{main} \dot{V}_{main}}{V_{main}} + \frac{\gamma R (T_{main} \dot{m}_{main} - T_{aux,1} \dot{m}_{aux,1} - T_{aux,2} \dot{m}_{aux,2})}{V_{main}} \\
 \dot{p}_{aux,1} &= -\frac{\gamma R (T_{main} \dot{m}_{aux,1} + T_{aux,1} \dot{m}_{aux,1})}{V_{aux,1}} \\
 \dot{p}_{aux,2} &= -\frac{\gamma R (T_{main} \dot{m}_{aux,2} + T_{aux,2} \dot{m}_{aux,2})}{V_{aux,2}} \\
 \dot{T}_{main} &= \frac{(1-\gamma) T_{main} \dot{V}_{main}}{V_{main}} + \frac{(\gamma-1) R T_{main}^2 \dot{m}_{main}}{V_{main} p_{main}} - \frac{\gamma R T_{main} (T_{aux,1} \dot{m}_{aux,1} + T_{aux,2} \dot{m}_{aux,2})}{V_{main} p_{main}} \\
 \dot{T}_{aux,1} &= \frac{(\gamma-1) R T_{aux,1}^2 \dot{m}_{aux,1}}{V_{aux,1} p_{aux,1}} + \frac{\gamma R T_{main} T_{aux,1} \dot{m}_{aux,1}}{V_{aux,1} p_{aux,1}} \\
 \dot{T}_{aux,2} &= \frac{(\gamma-1) R T_{aux,2}^2 \dot{m}_{aux,2}}{V_{aux,2} p_{aux,2}} + \frac{\gamma R T_{main} T_{aux,2} \dot{m}_{aux,2}}{V_{aux,2} p_{aux,2}} \\
 \dot{m}_{main} &= s_1 \cdot A_{v,max} C_{v1} \cdot p_{max} \sqrt{\frac{2\gamma}{RT_{up}(\gamma-1)} \left[\left(\frac{p_{min}}{p_{max}} \right)^{\frac{2}{\gamma}} - \left(\frac{p_{min}}{p_{max}} \right)^{\frac{\gamma+1}{\gamma}} \right]} \text{sign}(p_{aux,1} - p_{main}) + \\
 &+ s_2 \cdot A_{v,max} C_{v2} \cdot p_{max,2} \sqrt{\frac{2\gamma}{RT_{up,2}(\gamma-1)} \left[\left(\frac{p_{min,2}}{p_{max,2}} \right)^{\frac{2}{\gamma}} - \left(\frac{p_{min,2}}{p_{max,2}} \right)^{\frac{\gamma+1}{\gamma}} \right]} \text{sign}(p_{aux,2} - p_{main}) \\
 \dot{m}_{aux,1} &= s_1 \cdot A_{v,max} C_{v1} \cdot p_{max} \sqrt{\frac{2\gamma}{RT_{up}(\gamma-1)} \left[\left(\frac{p_{min}}{p_{max}} \right)^{\frac{2}{\gamma}} - \left(\frac{p_{min}}{p_{max}} \right)^{\frac{\gamma+1}{\gamma}} \right]} \text{sign}(p_{main} - (p_{aux,1})) \\
 \dot{m}_{aux,2} &= s_2 \cdot A_{v,max} C_{v2} \cdot p_{max,2} \sqrt{\frac{2\gamma}{RT_{up,2}(\gamma-1)} \left[\left(\frac{p_{min,2}}{p_{max,2}} \right)^{\frac{2}{\gamma}} - \left(\frac{p_{min,2}}{p_{max,2}} \right)^{\frac{\gamma+1}{\gamma}} \right]} \text{sign}(p_{main} - (p_{aux,2})) \\
 F_k &= (p_{main} - p_{atm}) \cdot A
 \end{aligned} \right.$$



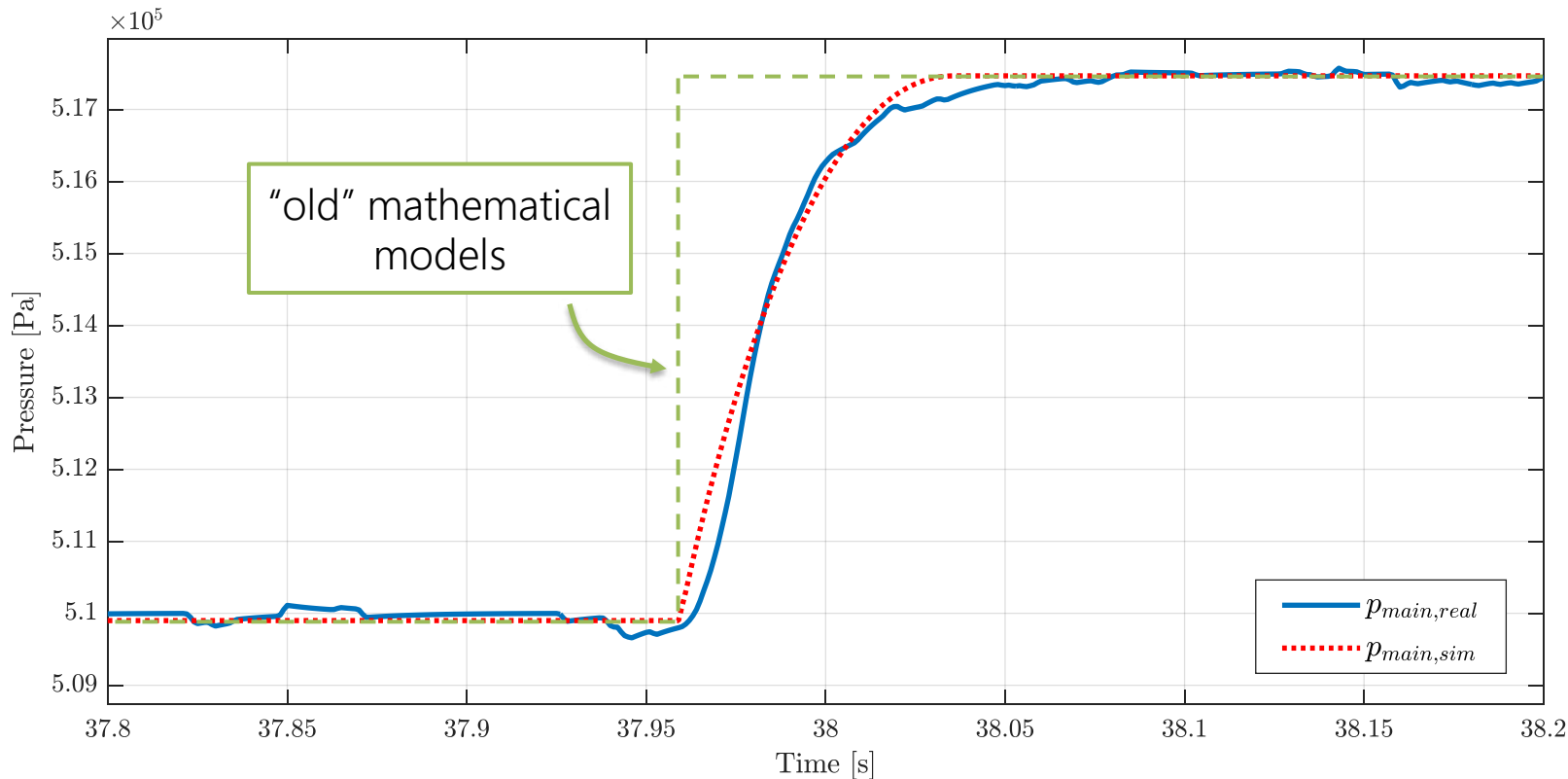
Semi-Active Stiffness Control

Model Identification



Semi-Active Stiffness Control

Model Identification



Opening of the valve

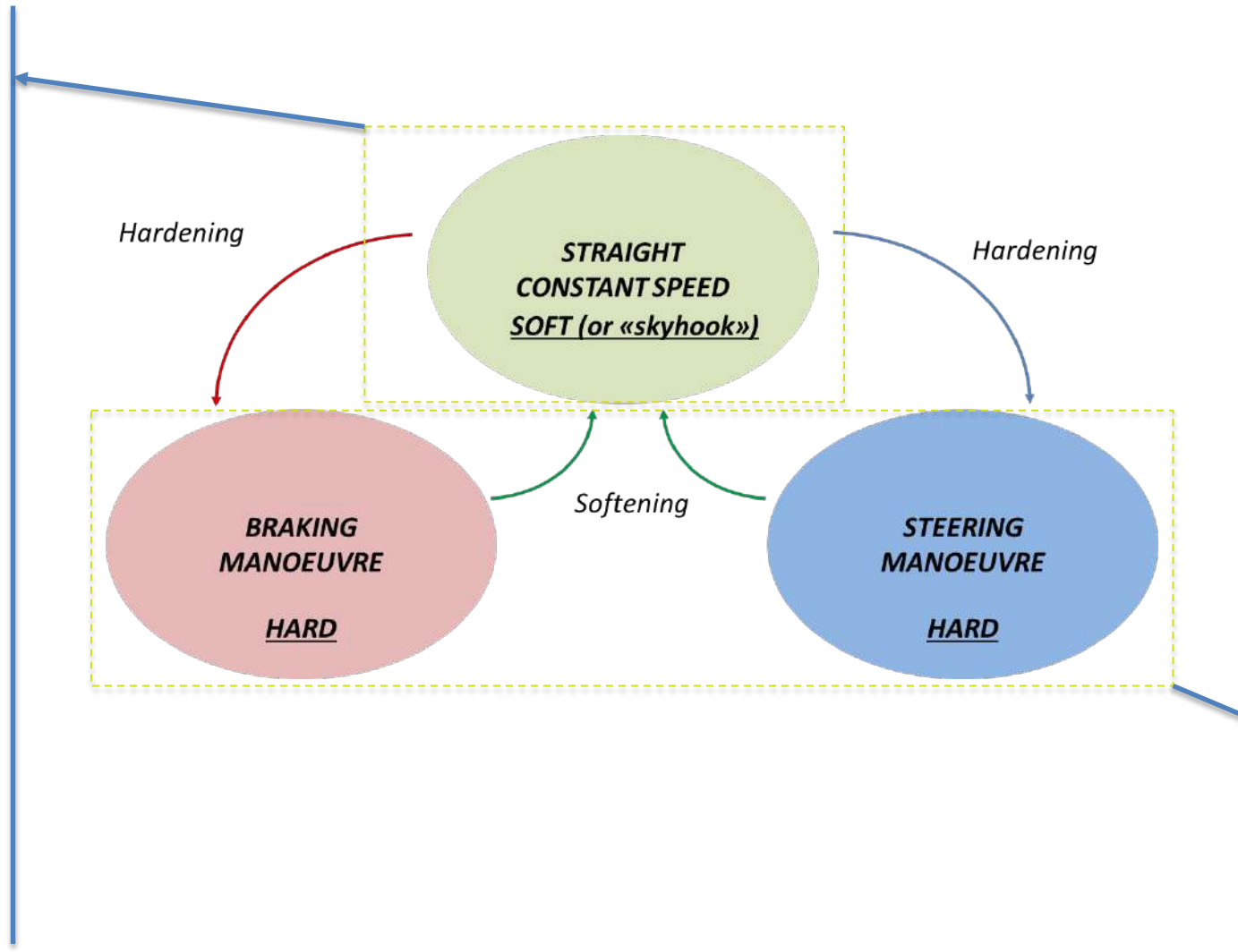
- When a valve is opened, the pressure (and consequently the elastic force) has a jump. The mathematical model is able to describe the pressure dynamics at the valve opening.
- The old models do not capture the real behaviour.

Semi-Active Stiffness Control

General Control Scheme

Car designed to be very comfortable on straight road; FIXED low-stiffness and FIXED low-damping

Good-Comfort - Poor handling



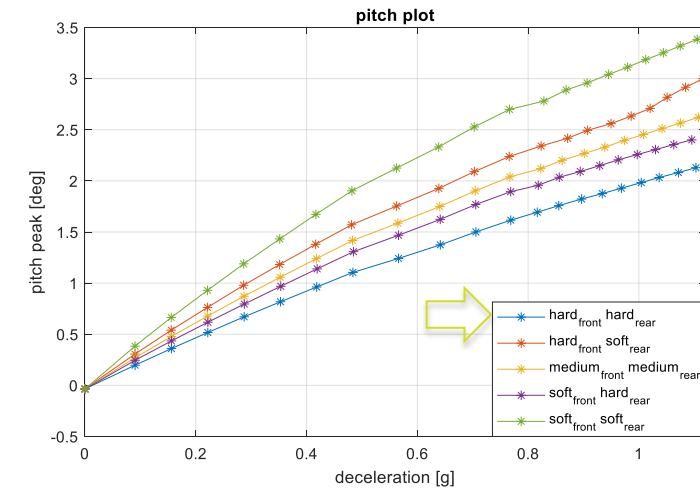
Car designed to have a good handling on curvy-roads; FIXED high-stiffness and FIXED high-damping

Good-Handling – Poor-comfort



Semi-Active Stiffness Control

Longitudinal Control Example

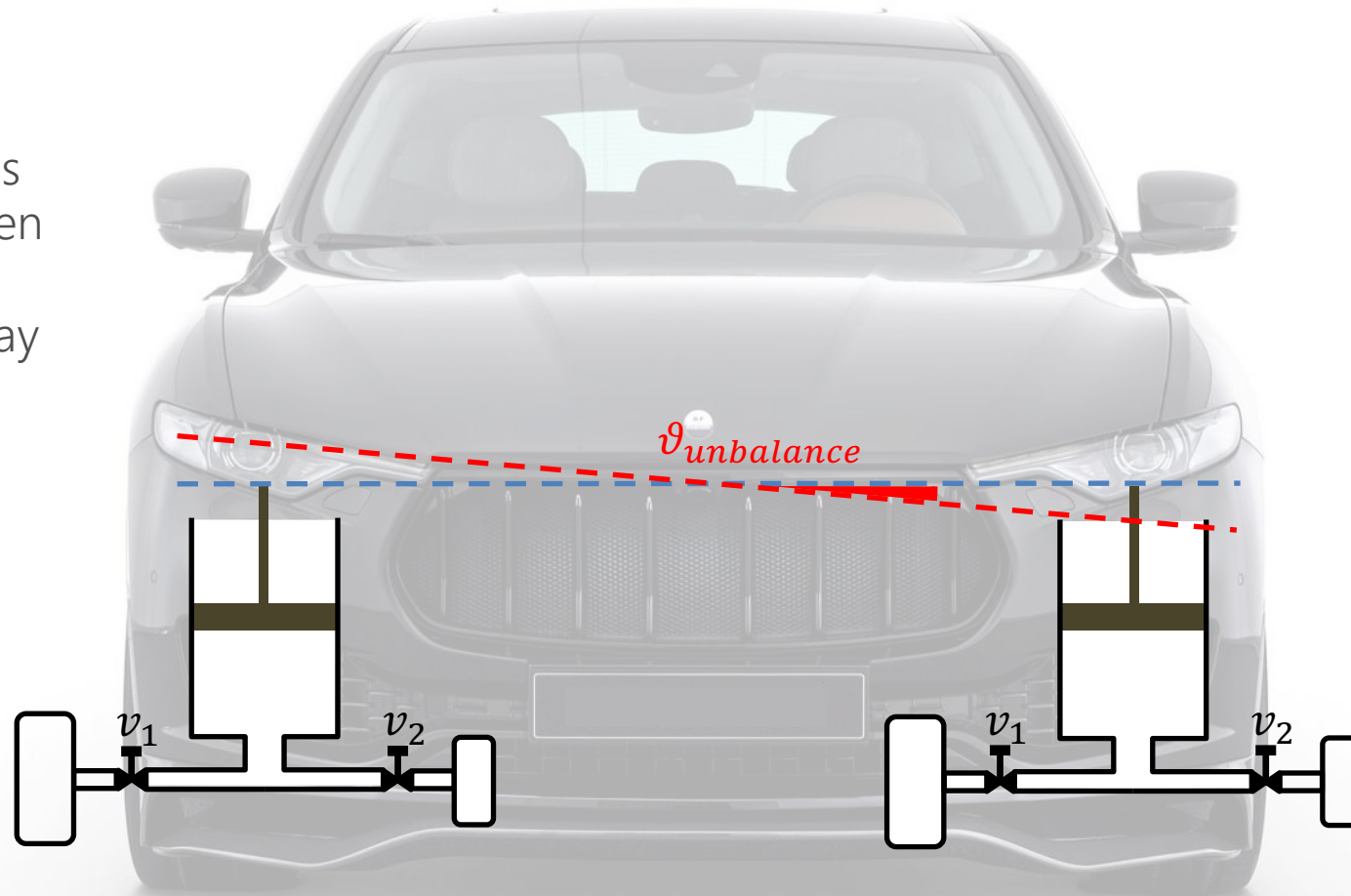


The «all-hard» K configuration guarantees the best «anti-dive» effect in braking (and «anti-squat» in acceleration)

Semi-Active Stiffness Control

Longitudinal Control Example

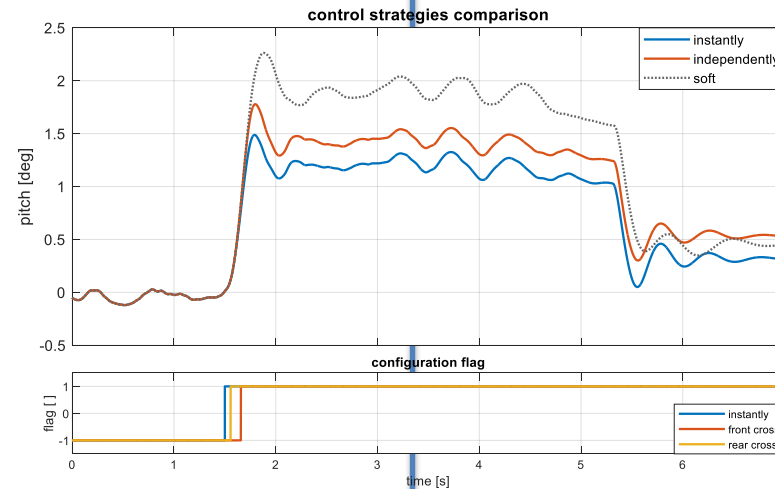
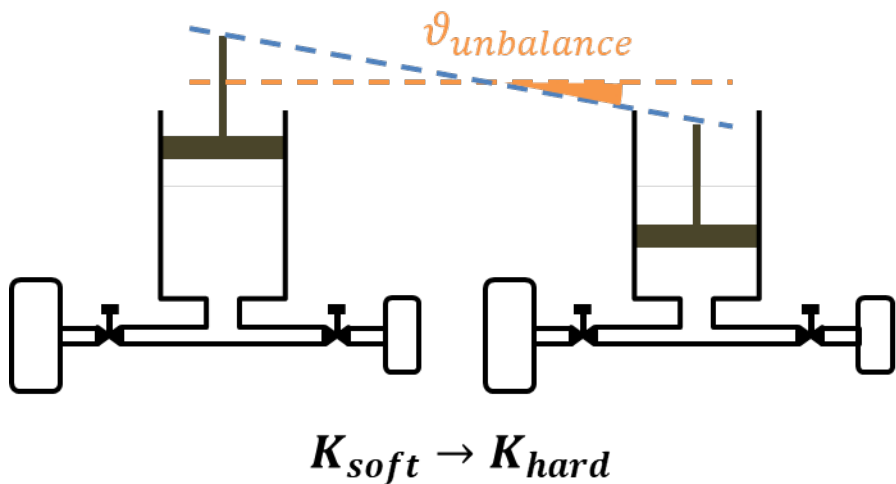
If the hardening-switch is immediately applied when braking, an unbalanced equilibrium roll angle may arise



Semi-Active Stiffness Control

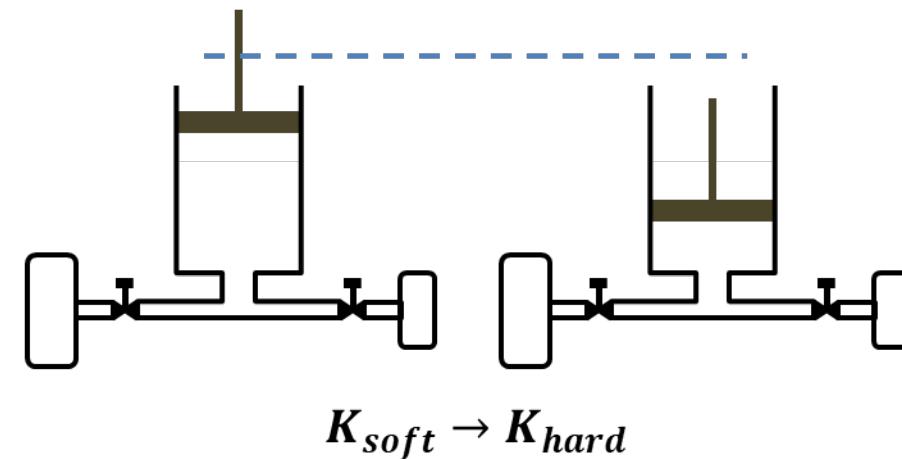
Hardening suspensions stiffness as soon as starts braking manoeuvre

PRO	CONS
Minimized control response time	Effects given by suspensions unbalancing

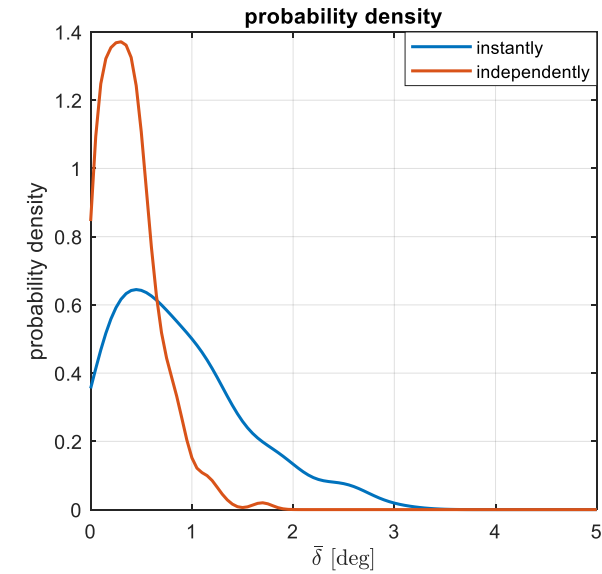
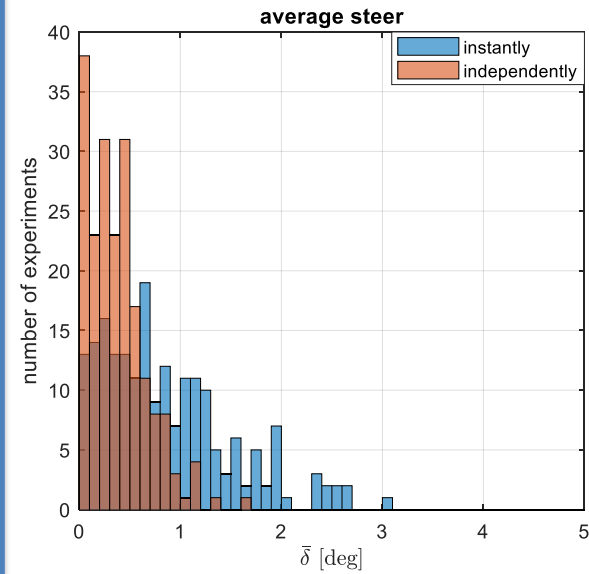
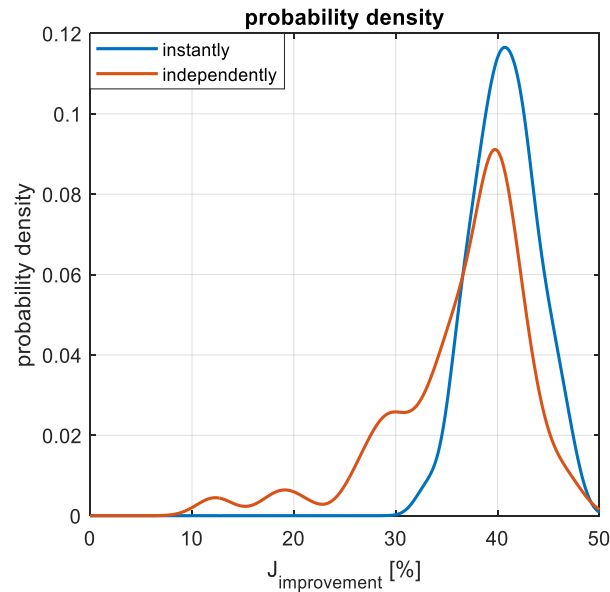
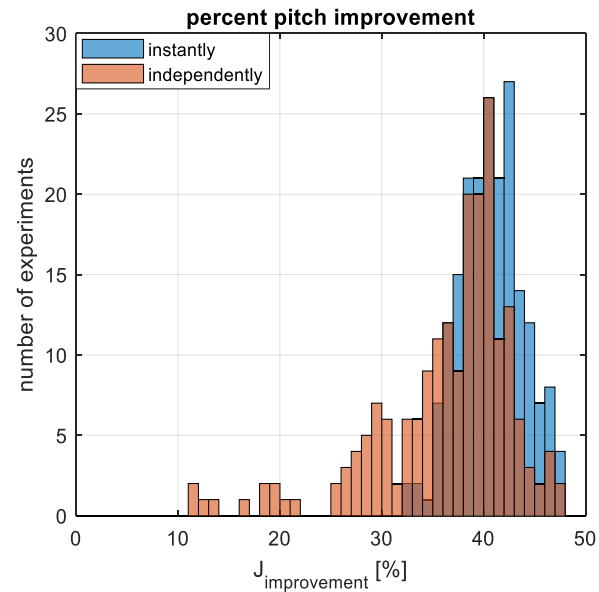


Hardening independently front and rear suspensions stiffness when braking manoeuvre is started and left and right suspensions are at the same stroke

PRO	CONS
Left and right suspensions balanced for each side	Pitch improvement delayed



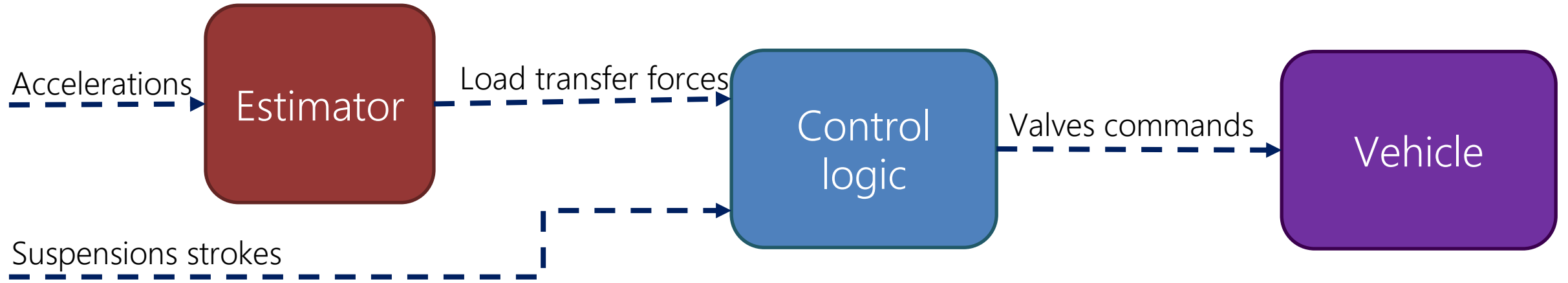
Semi-Active Stiffness Control



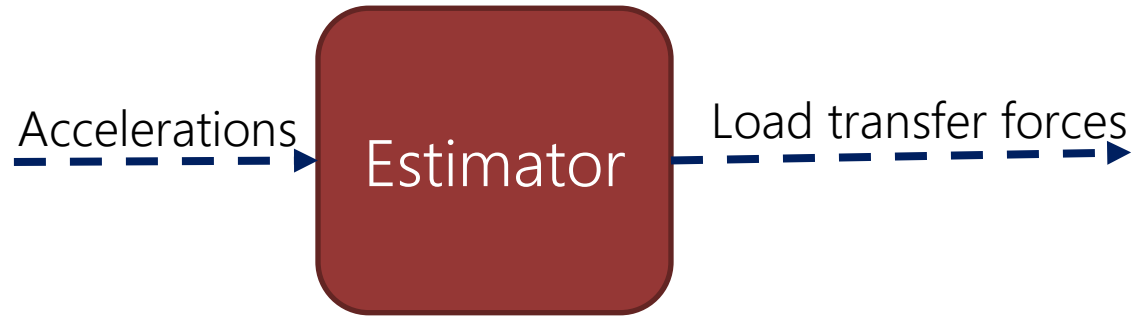
Pitch-unbalancing effect: the «instantly» control approach guarantees (slightly) better performance

Pitch-unbalancing negative effect: can be seen with the steer-angle correction needed to keep a straight line

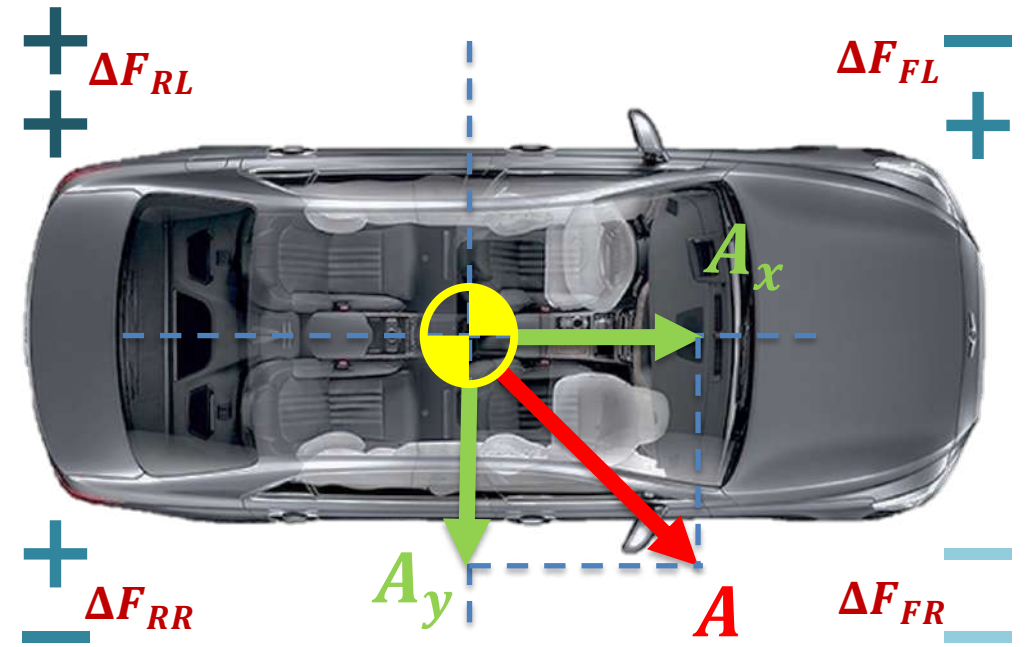
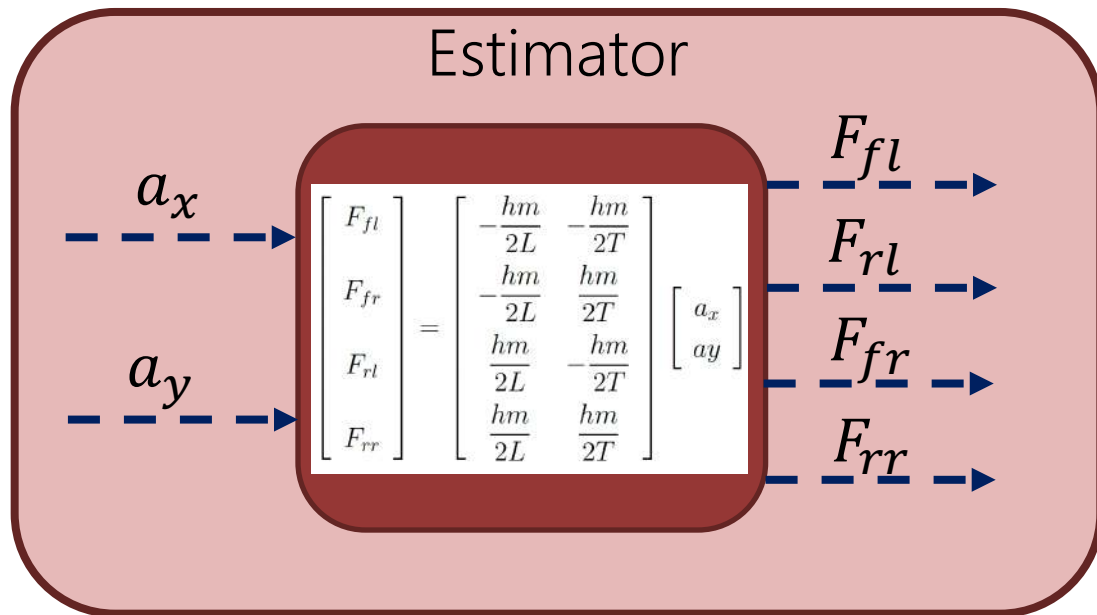
Semi-Active Stiffness Control



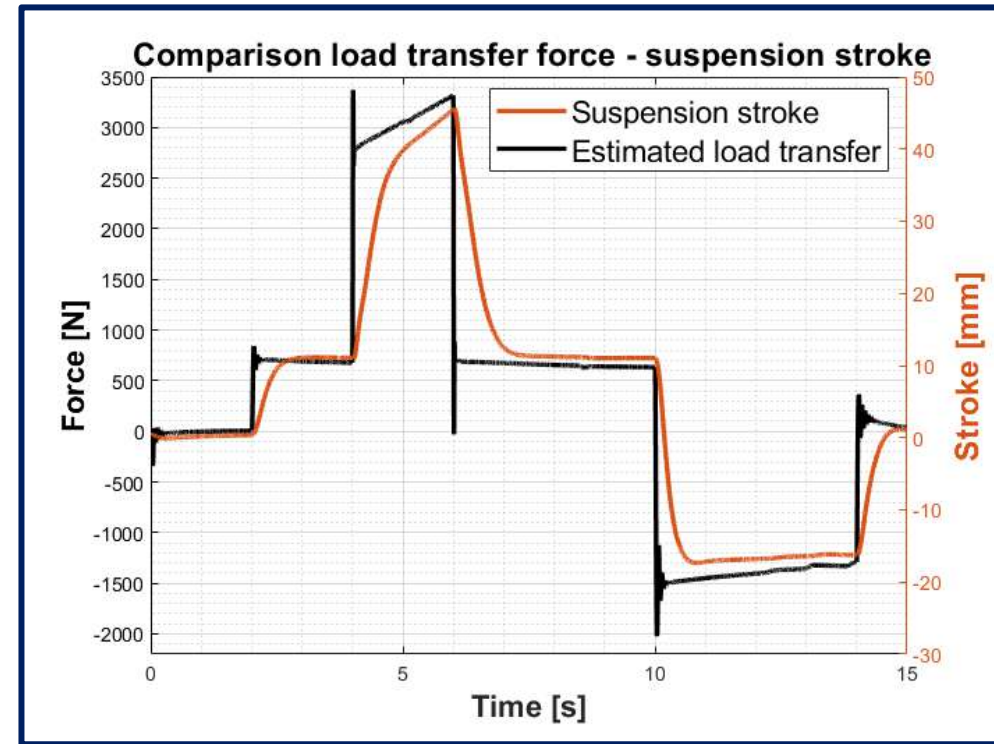
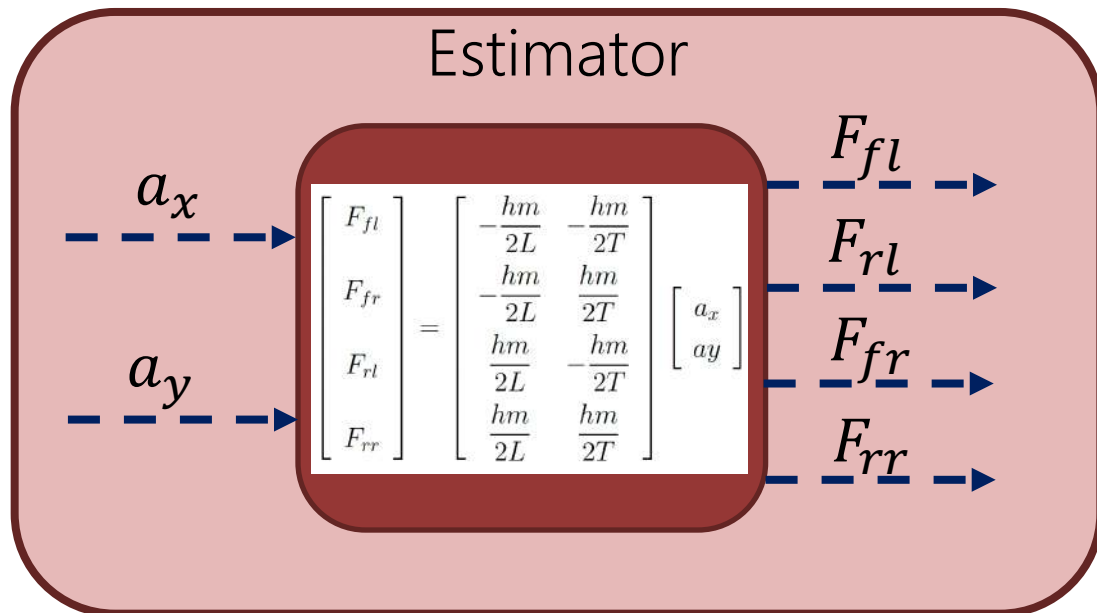
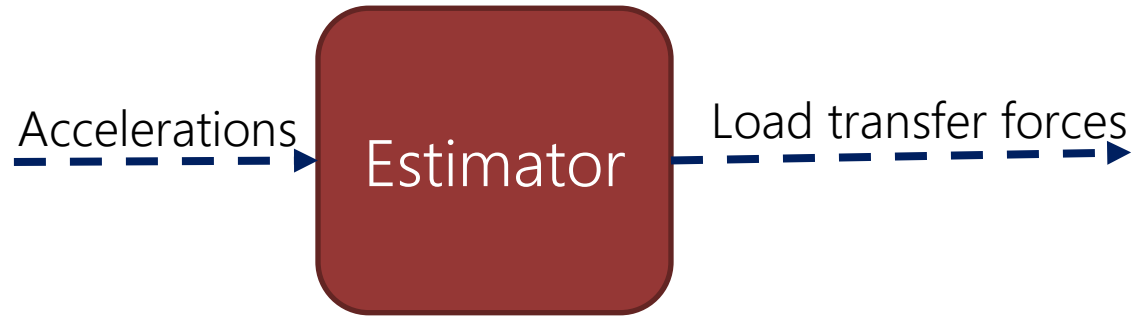
Semi-Active Stiffness Control



The load transfer force of each corner is estimated using a linear system that takes as input the longitudinal and lateral acceleration of the vehicle's COG.

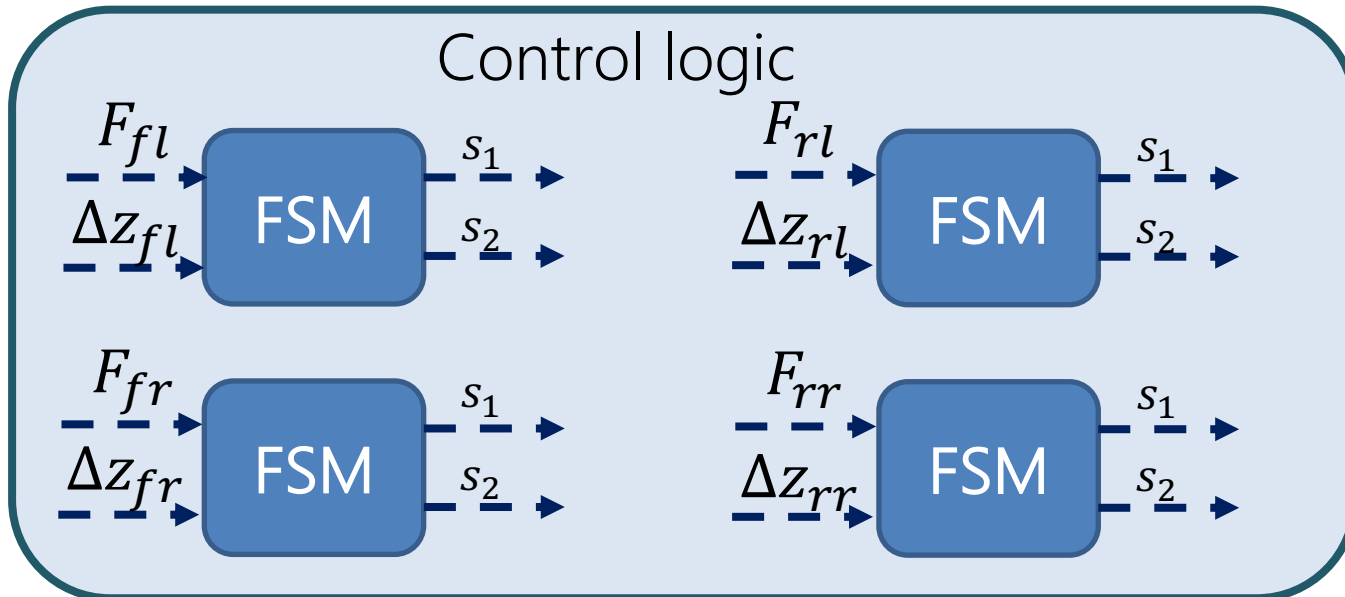
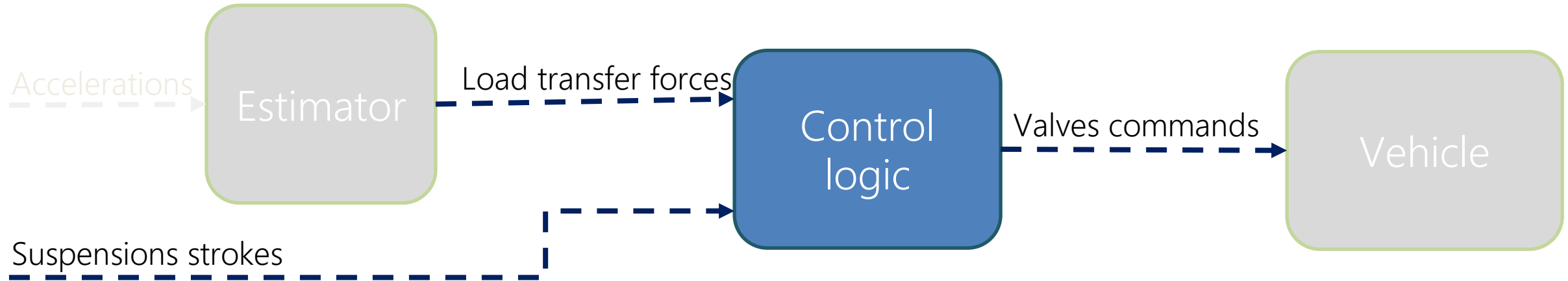


Semi-Active Stiffness Control



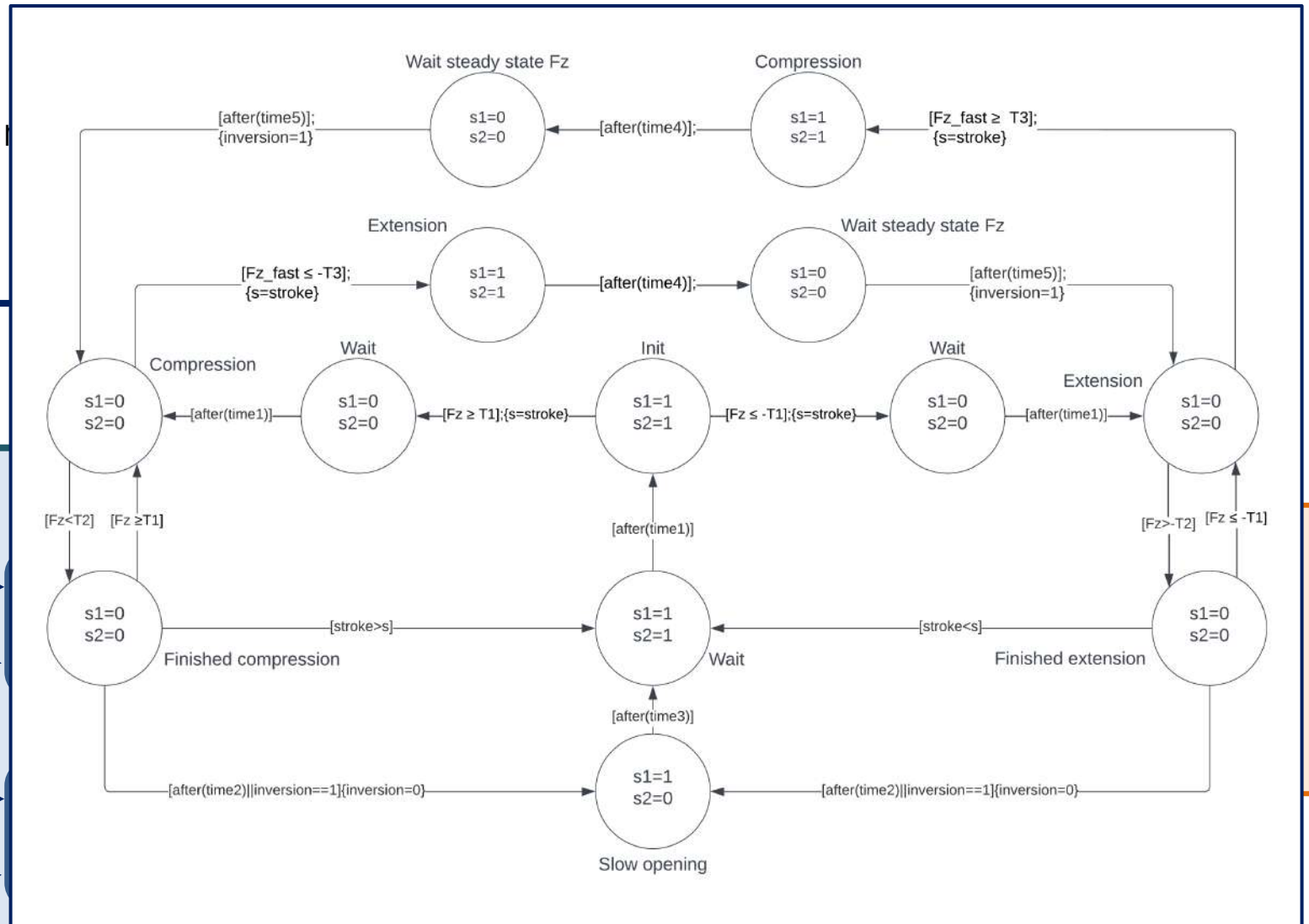
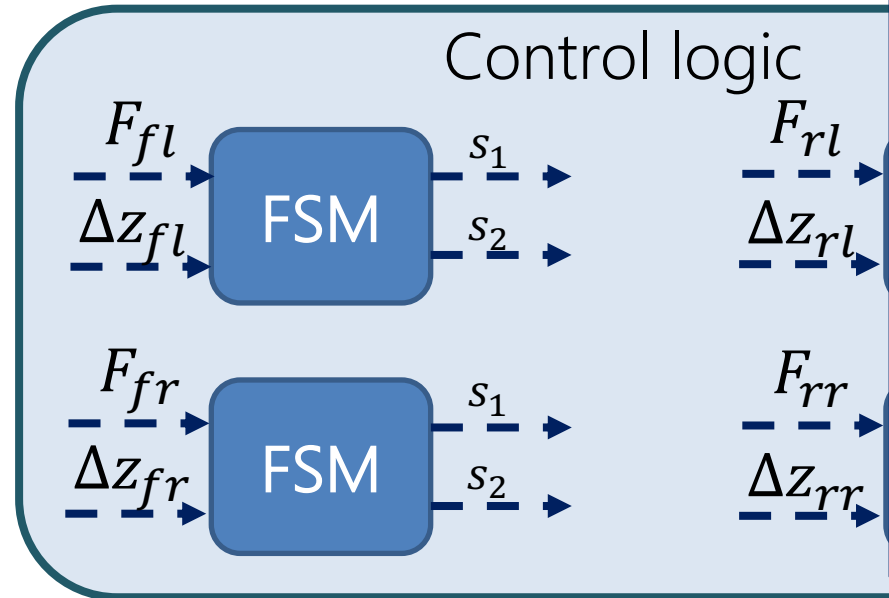
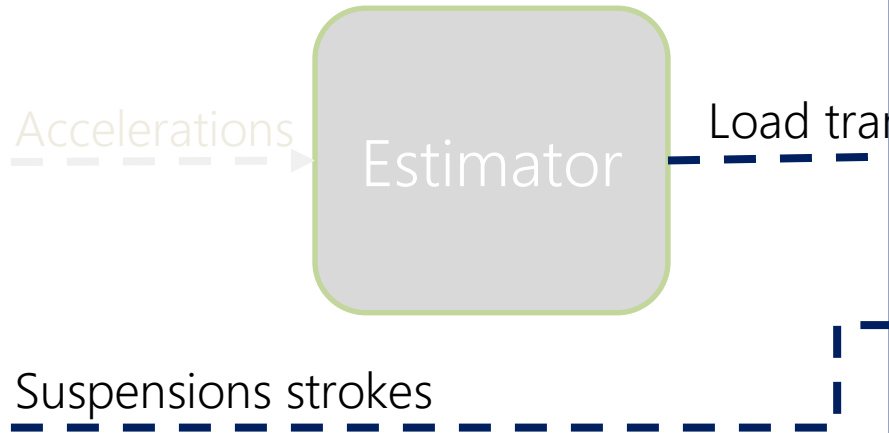
-
- It recognizes and manages mixed maneuvers
 - It predicts suspension behavior
 - Unique input for each corner

Semi-Active Stiffness Control



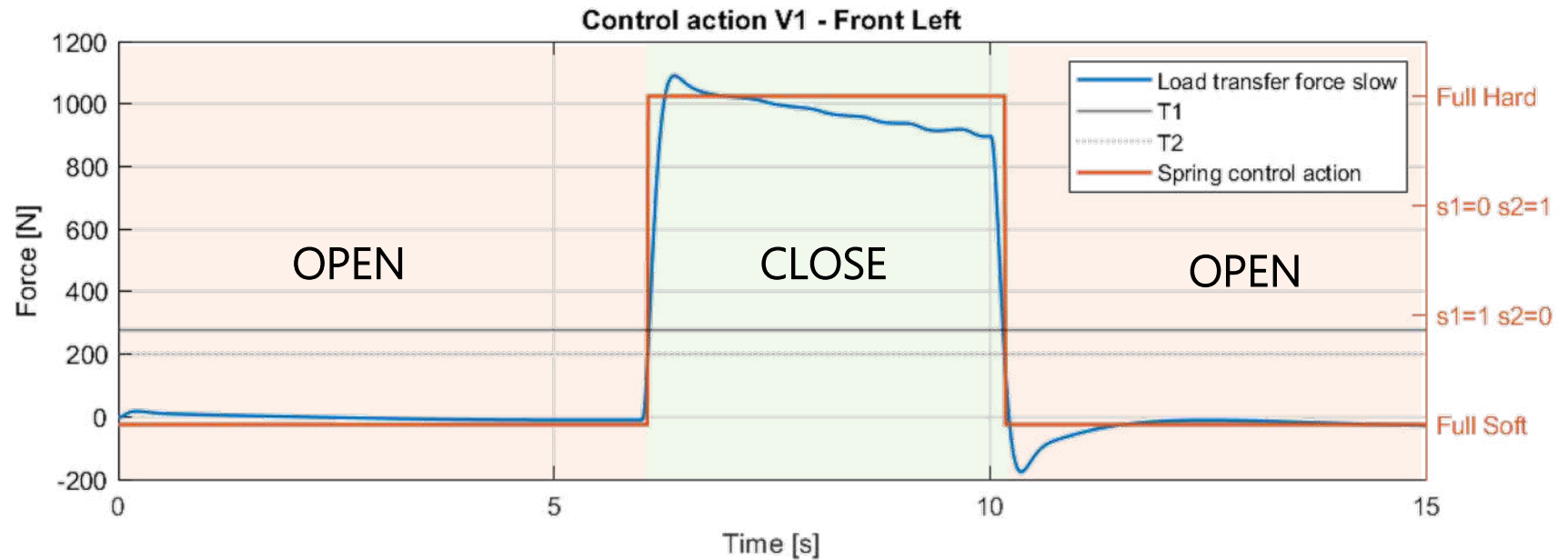
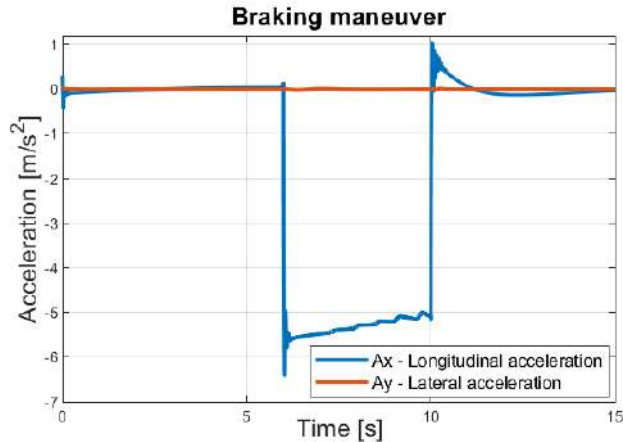
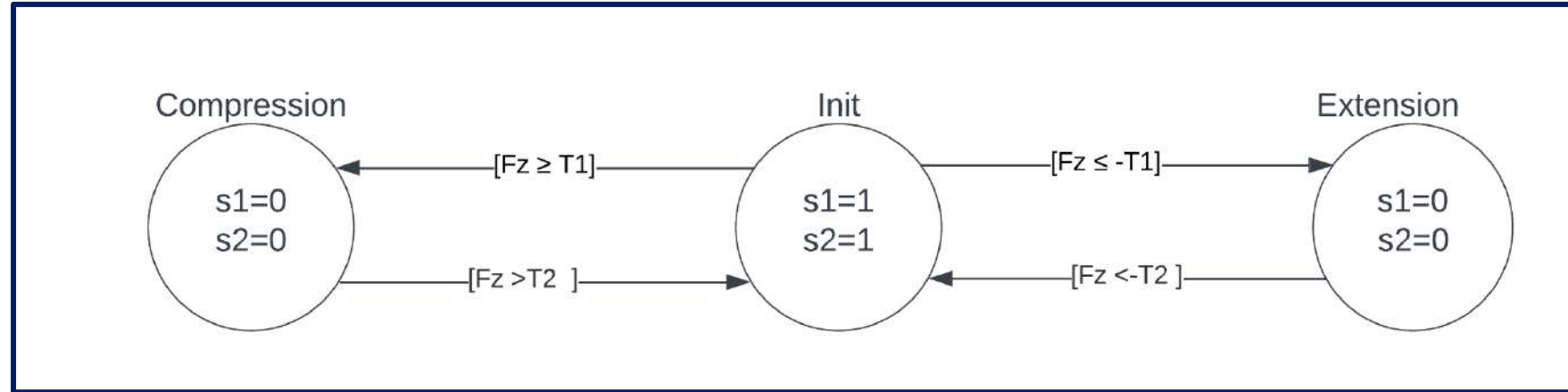
The control logic is made of **four identical finite state machine**, one for each car corner. The inputs are the **estimated load transfer** and the **suspension stroke** and the outputs are the **valves commands**.

Semi-Active Stiffness Control



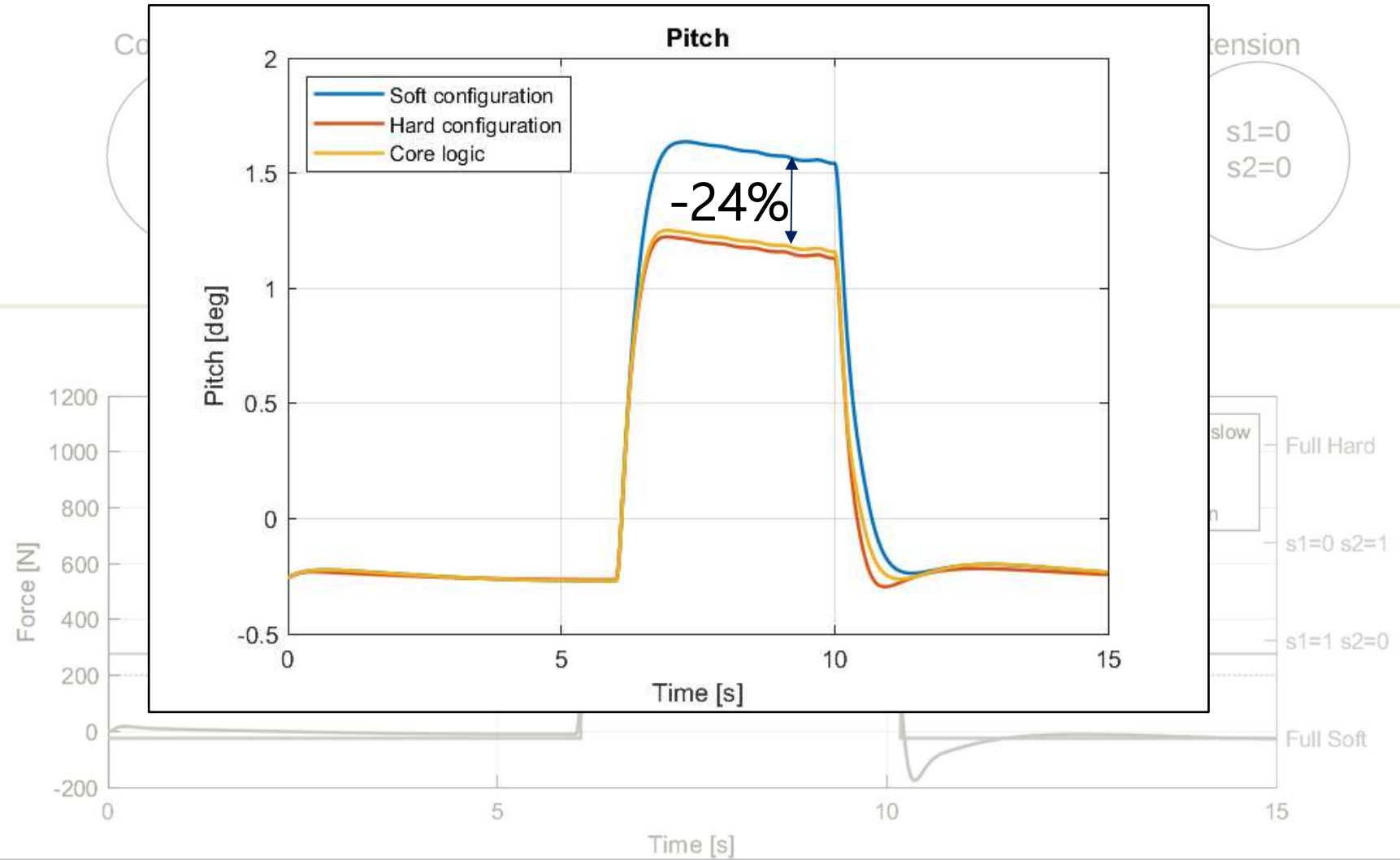
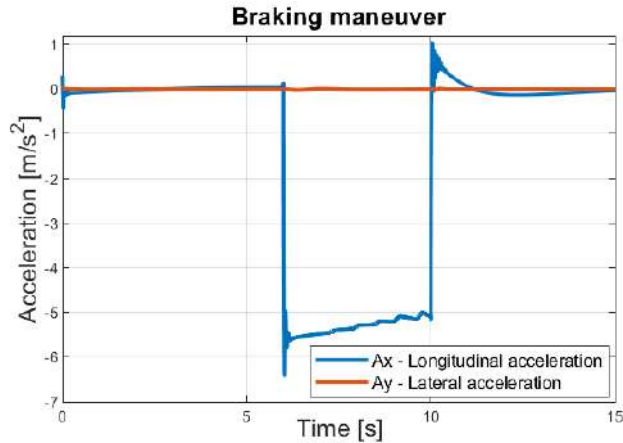
Semi-Active Stiffness Control

As soon as the estimated load transfer force is greater than $T1$, valves get closed. Then if the force is lower than $T2$ valves get opened again.



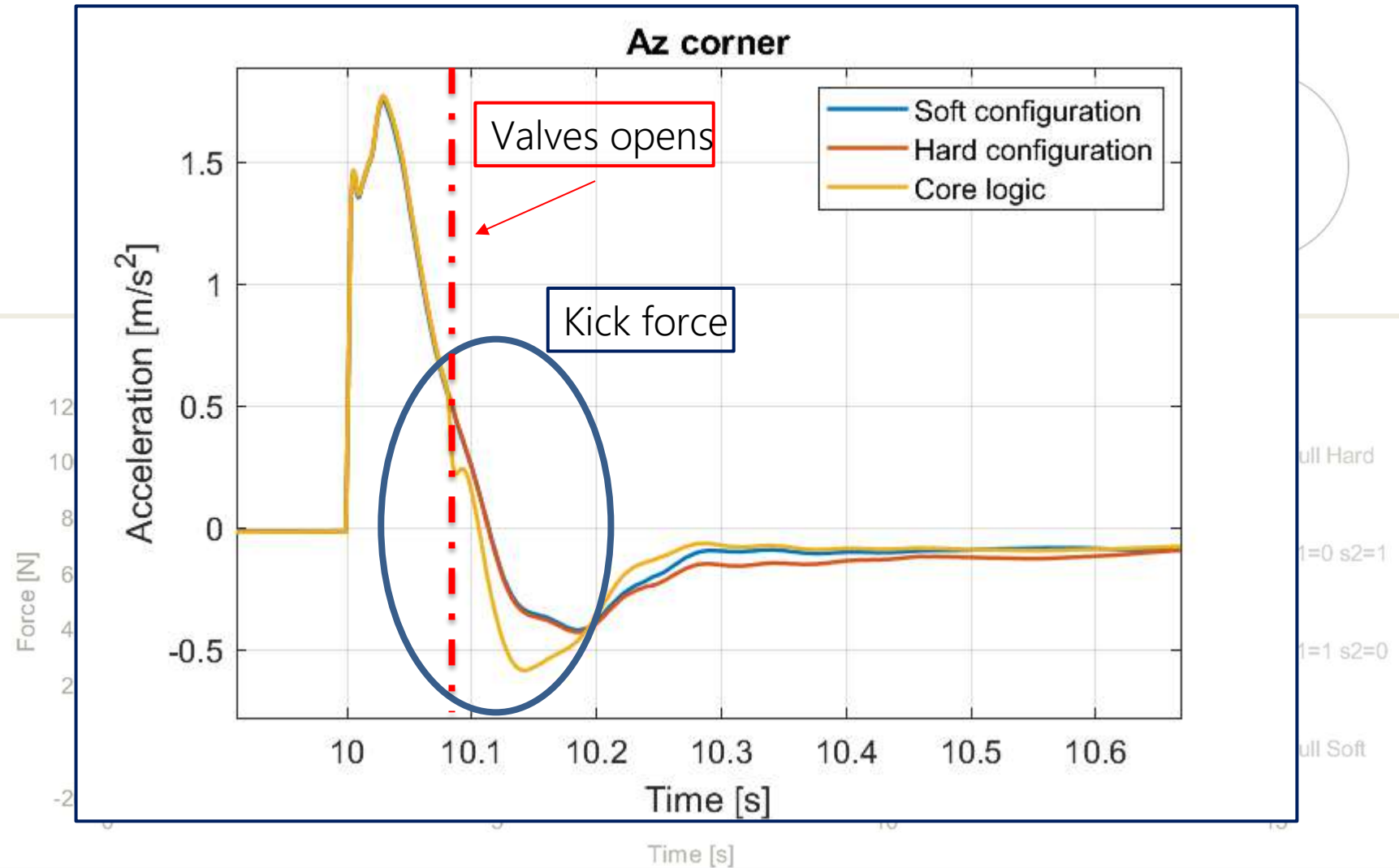
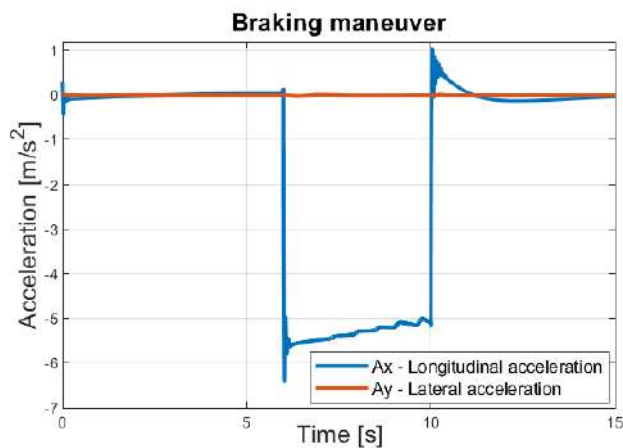
Semi-Active Stiffness Control

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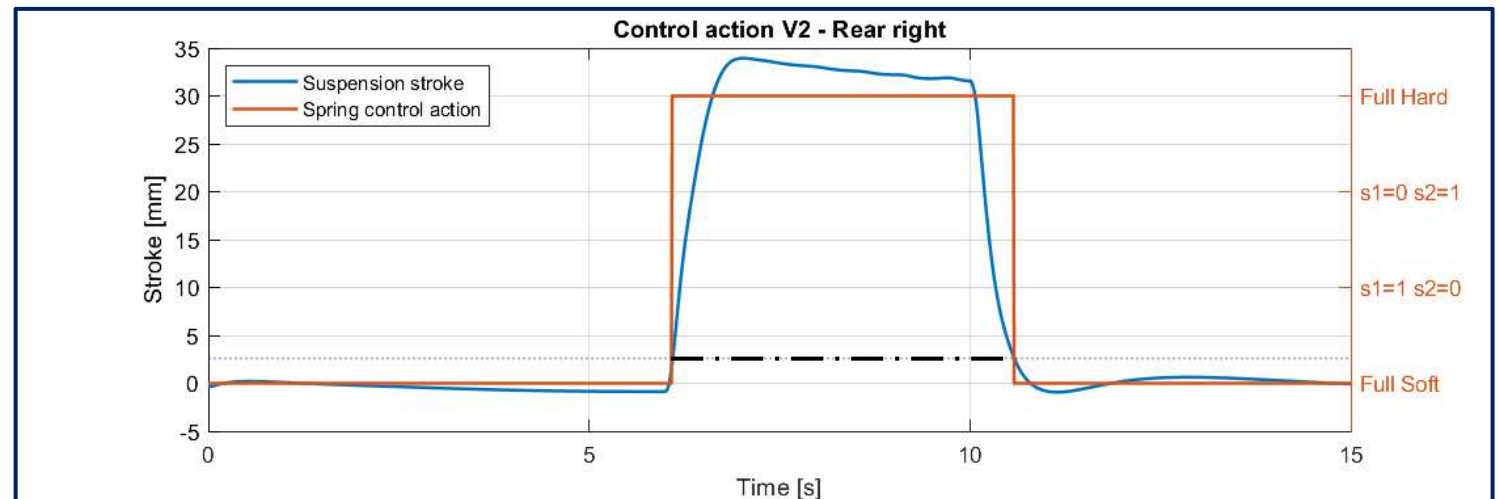
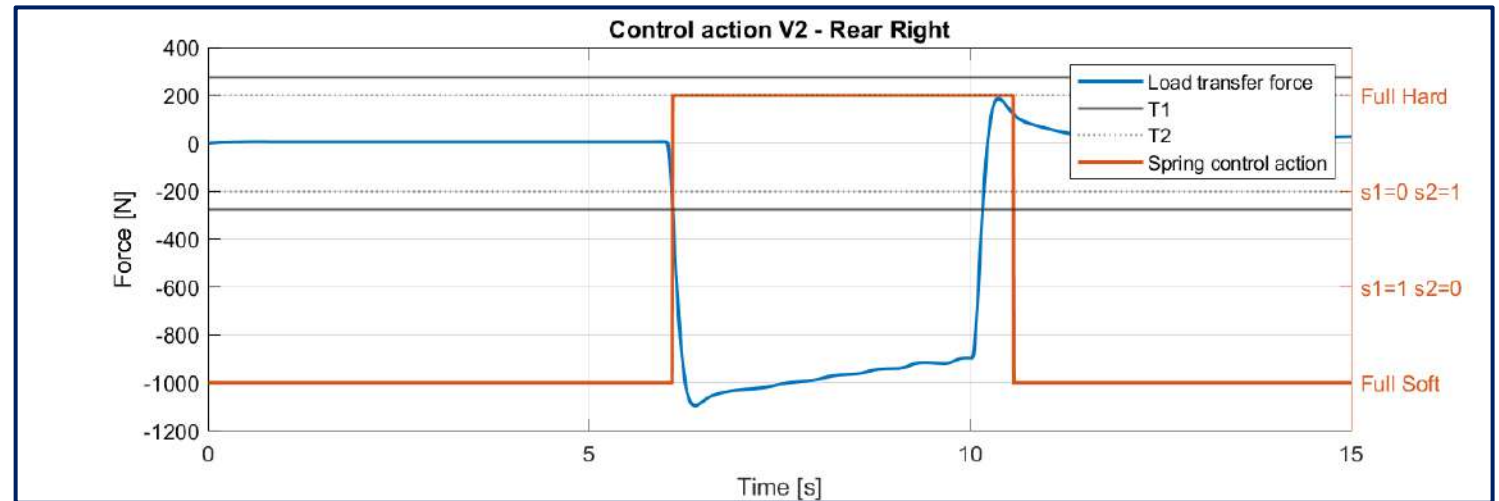
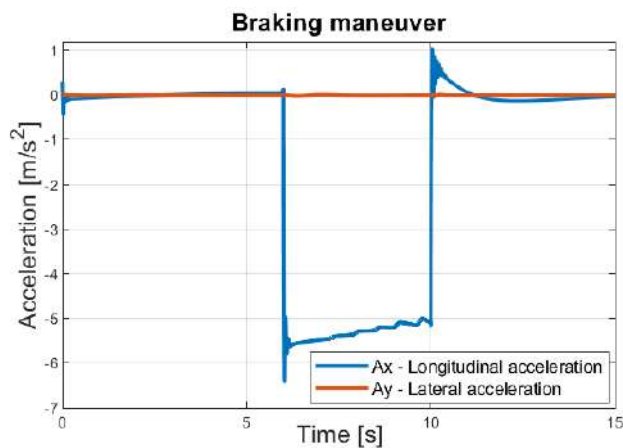
Semi-Active Stiffness Control

Kick force occurs if the valves are opened when the pressure of the **auxiliary** chambers is **different** with respect to the pressure of the **main** chamber. This phenomenon worsens the **peak** of **vertical** acceleration by 38%.



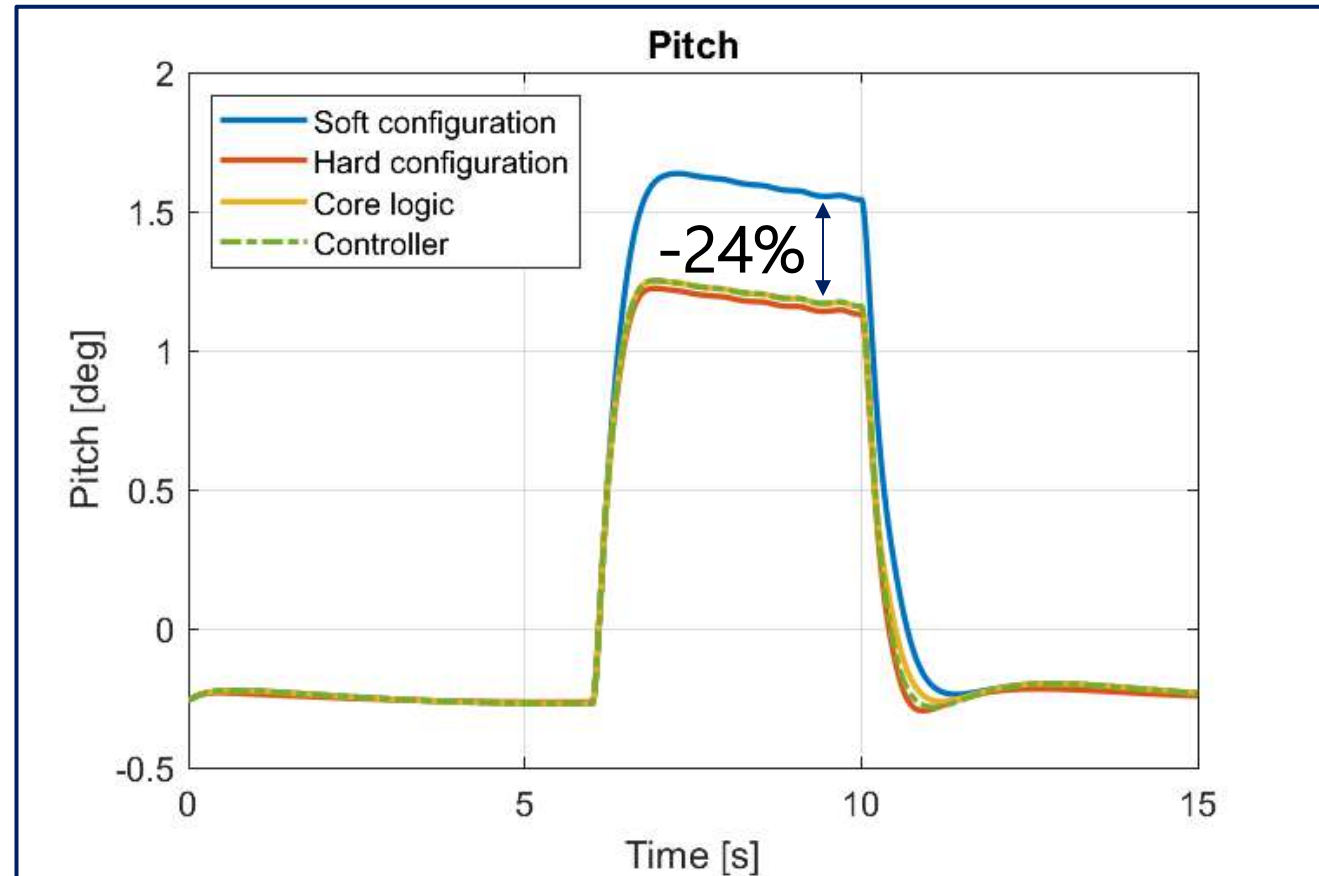
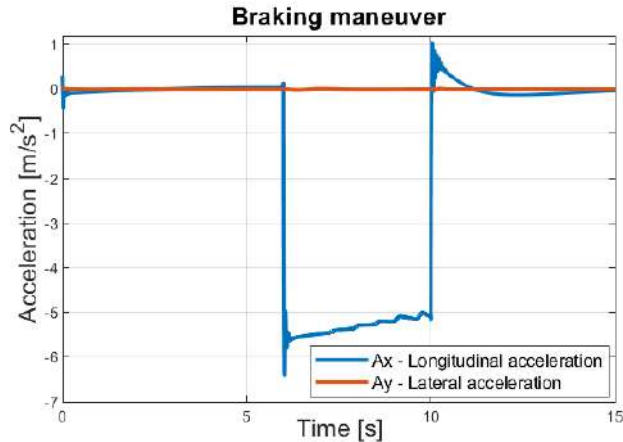
Semi-Active Stiffness Control

Valves get opened if the load transfer force is lower than the threshold $T2$ and the stroke is equal to the closing one.



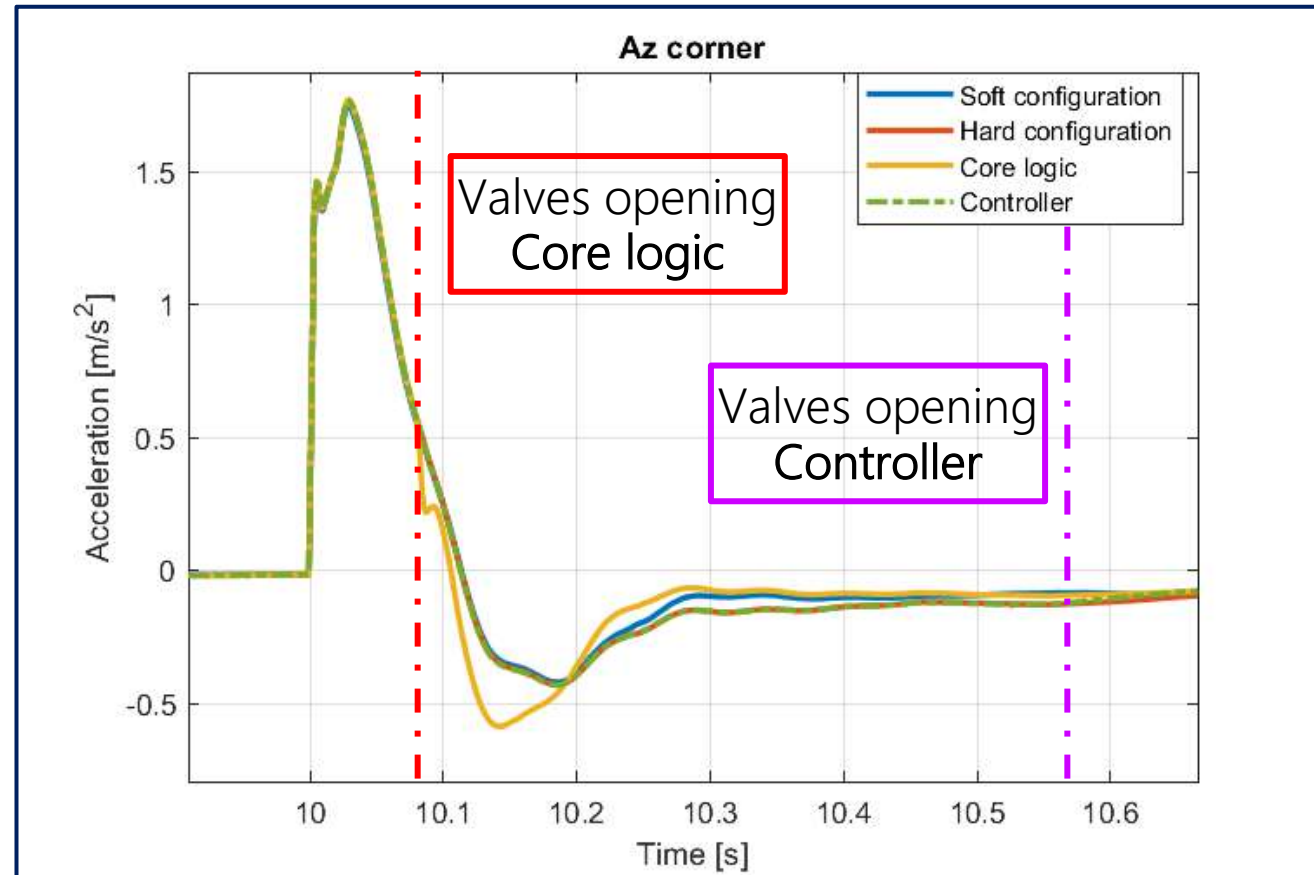
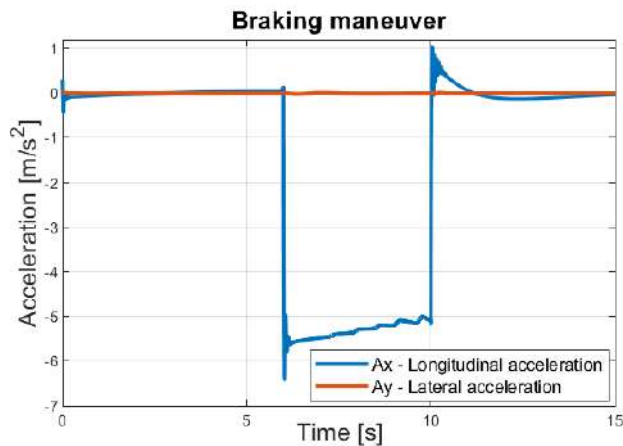
Semi-Active Stiffness Control

The **core logic** and the **controller** bring to the same improvement because the closing strategy is the same.



Semi-Active Stiffness Control

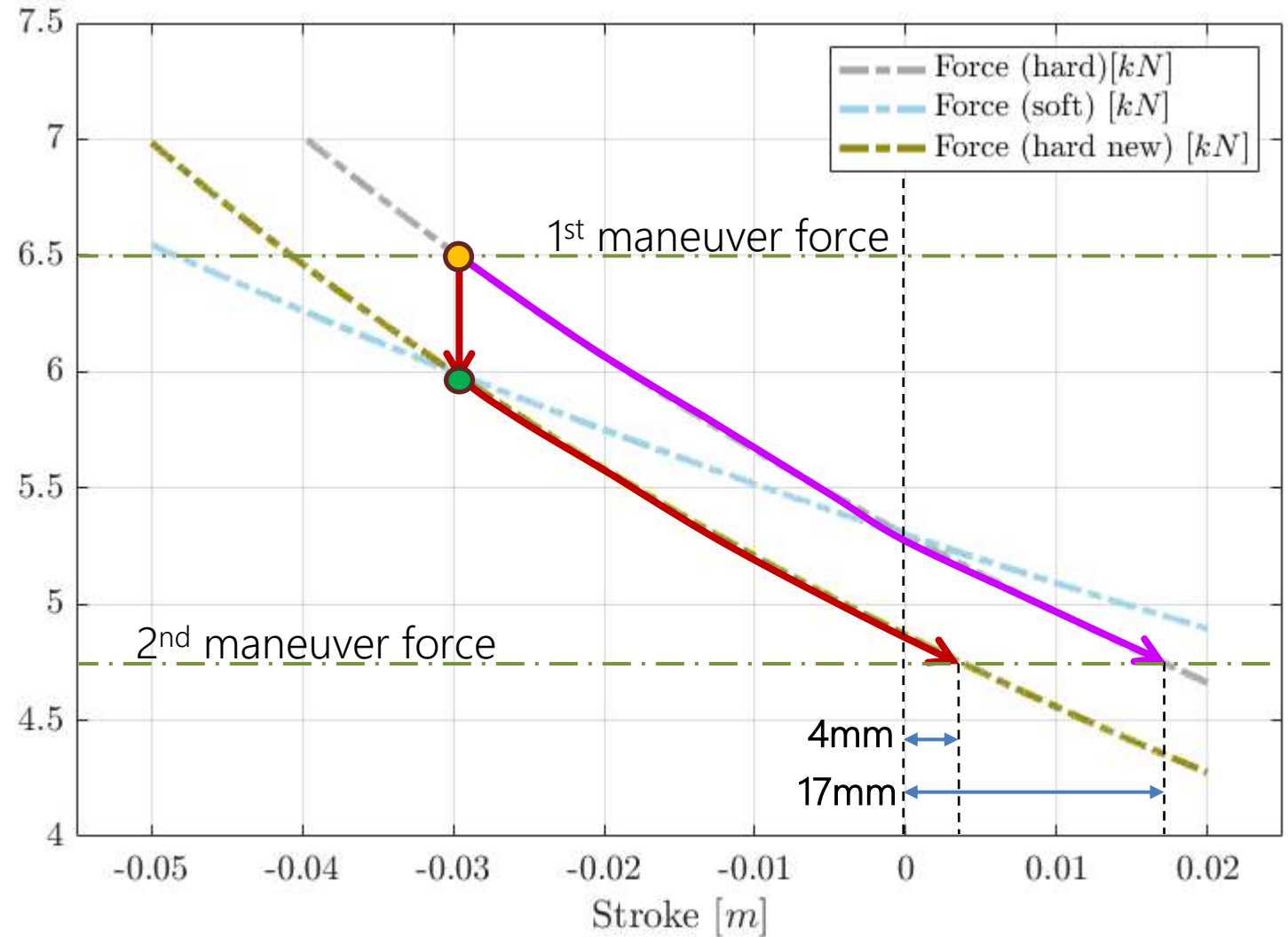
The new condition leads to a **delay** in the opening that solves the kick-force problem.



Semi-Active Stiffness Control

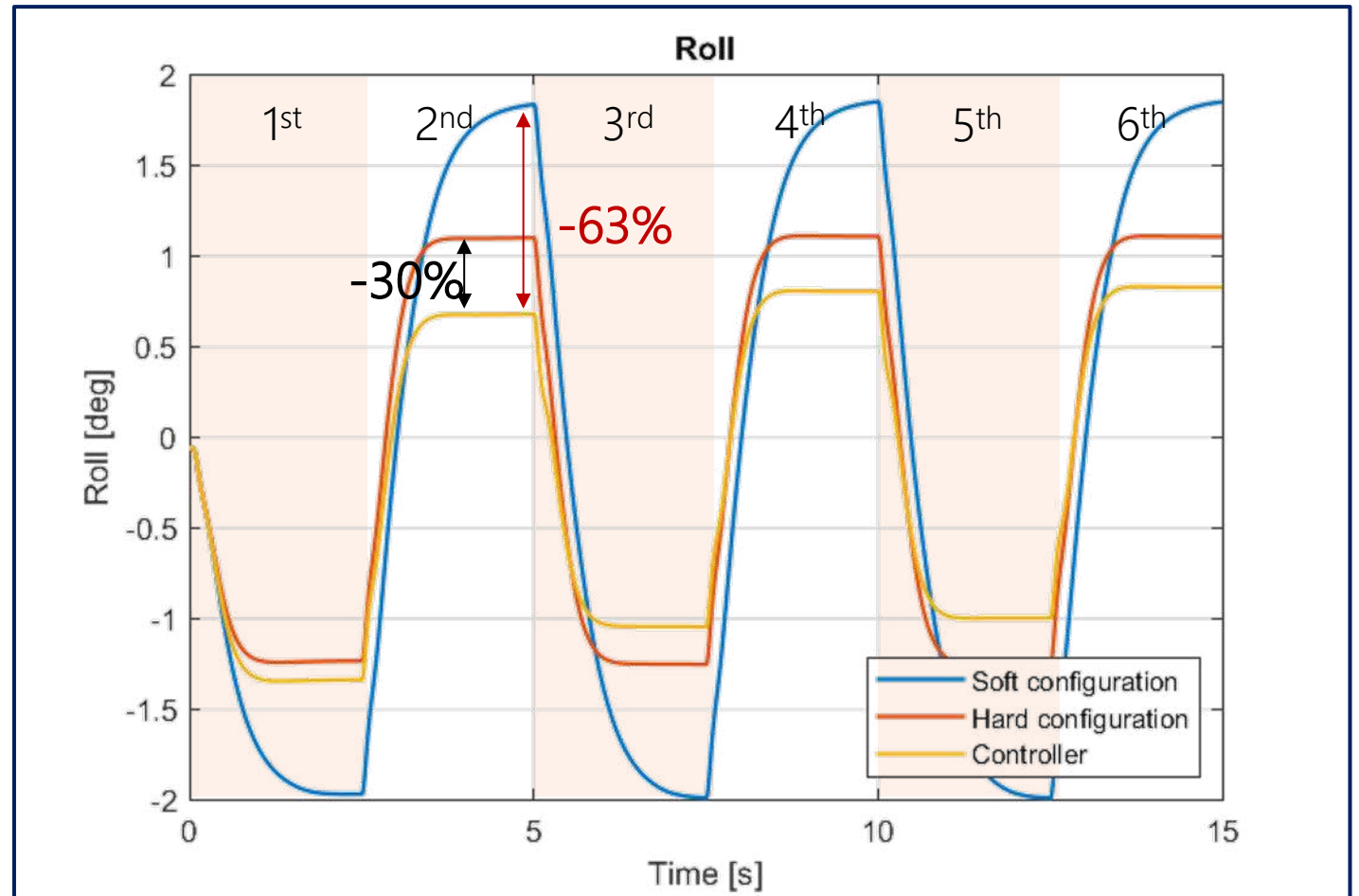
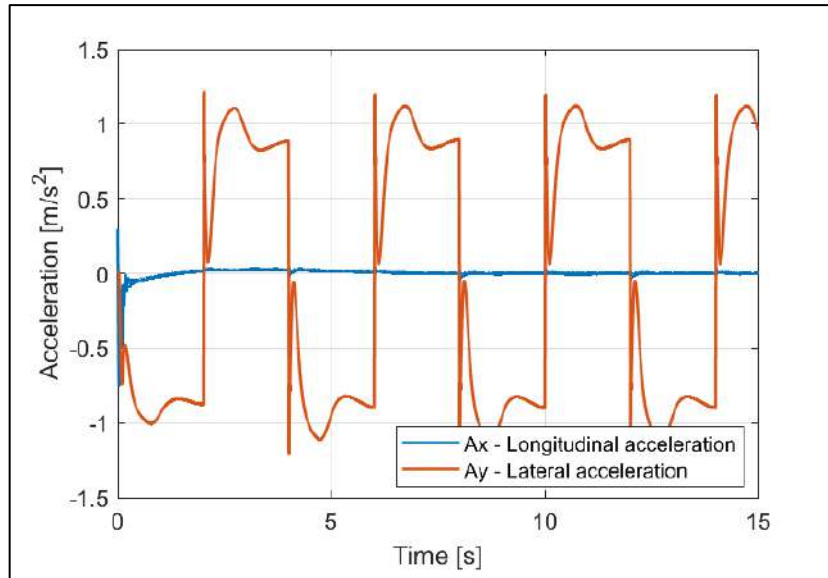
When maneuver inversion is detected a rapid **opening and closing sequence** is actuated in order to **change the working curve**, selecting the one that **minimize the stroke** for the second maneuver force.

- Open Loop
- Controller
- Opening
- Closing



Semi-Active Stiffness Control

All the maneuvers except for the first one benefits from the equilibrium change, achieving improvements of up to **63%**



Steering to the left Steering to the right

Is genuine semi-active stiffness control beneficial?

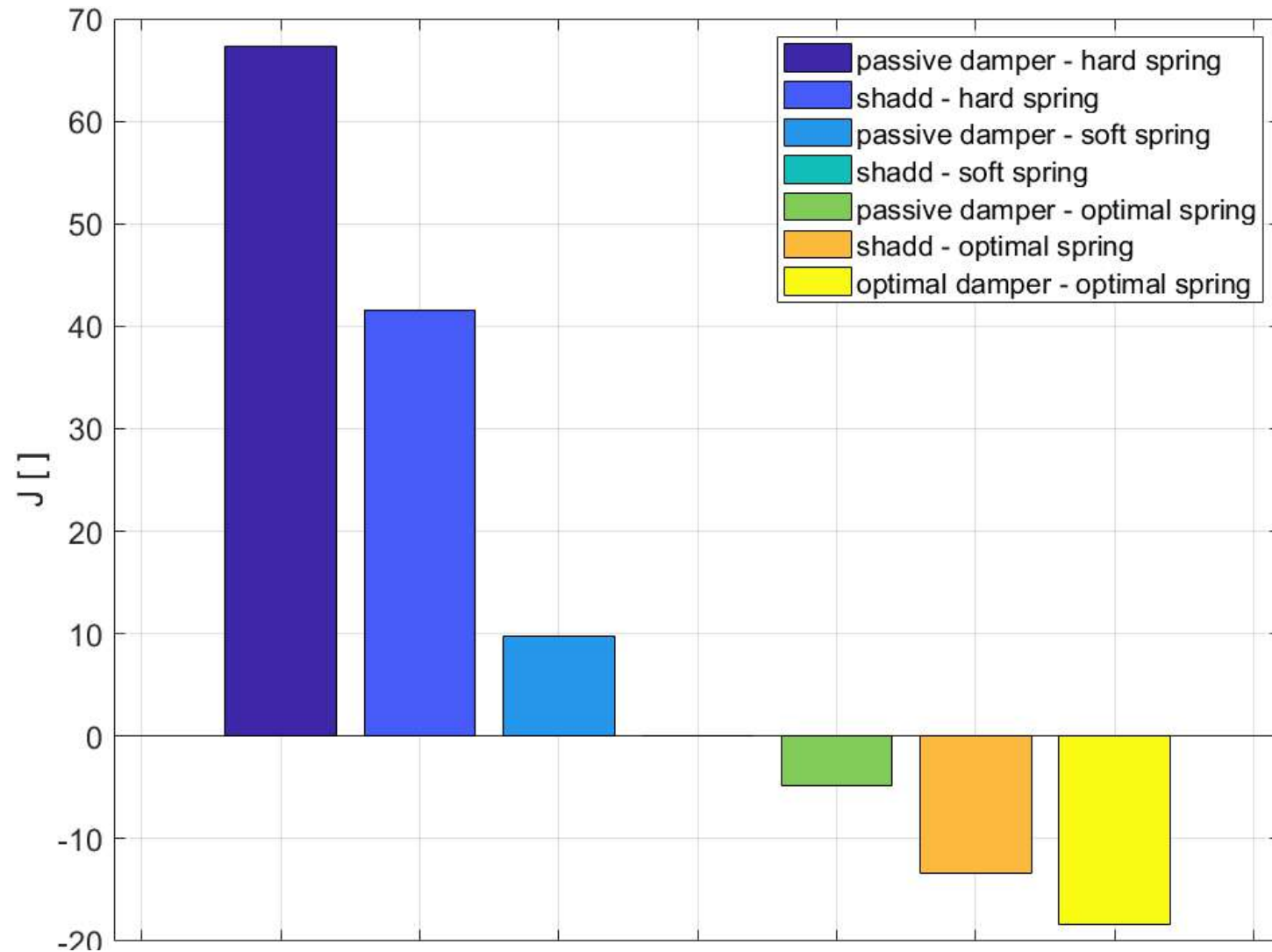
Is genuine semi-active stiffness control beneficial?



- *Offline optimization*: perfect road profile preview
- Find the sequence of openings/closings of the valve minimizing

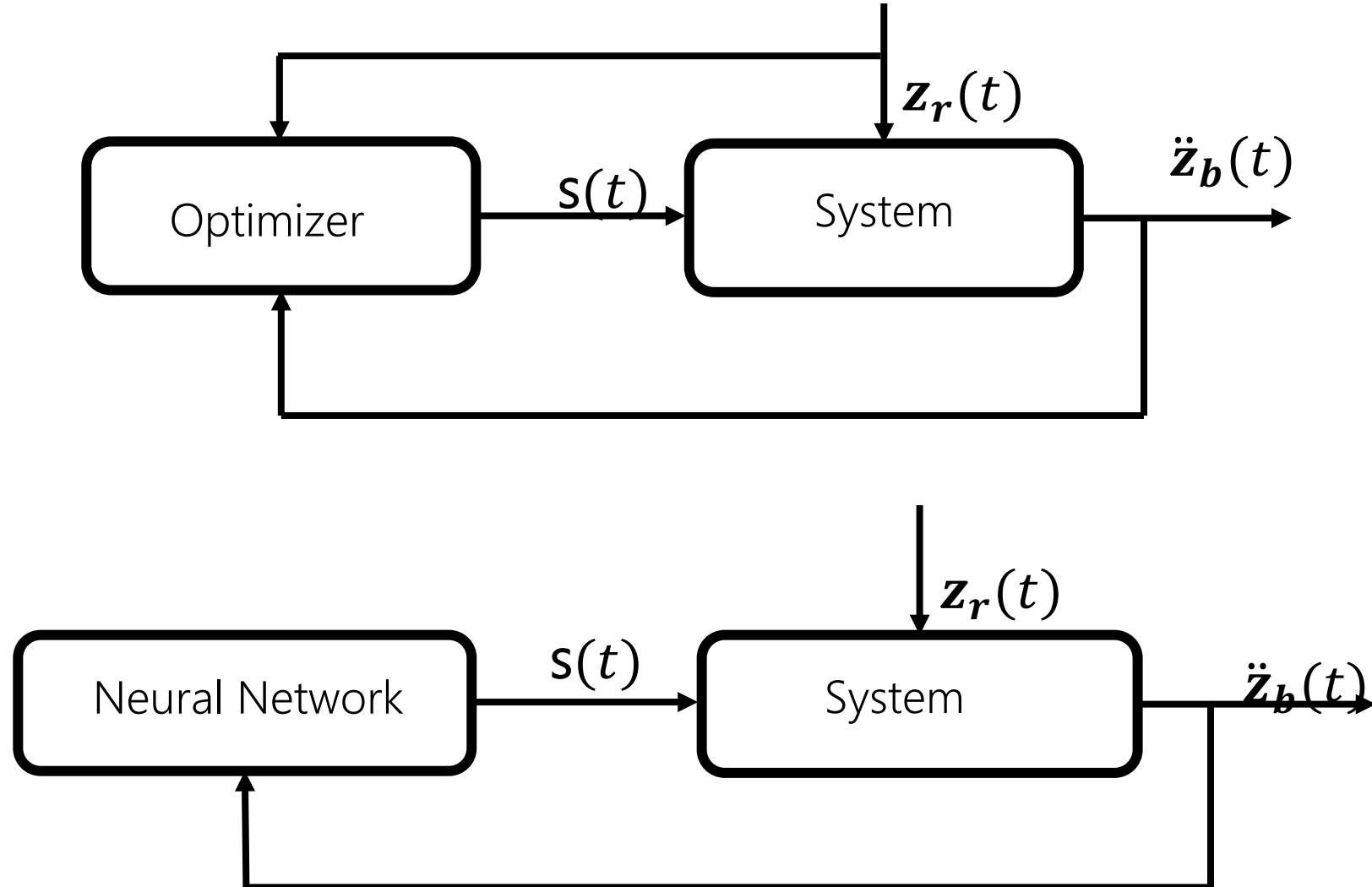
$$J = \frac{\int_0^T \delta \ddot{z}_b^2(t) dt}{\int_0^T \delta z_r^2(t) dt}$$

Semi-Active Stiffness Control



Semi-Active Stiffness Control

Causal Control – Neural Network Based



Collected features:

- Body position
- Body velocity
- Body acceleration
- Tire position
- Tire velocity
- Main chamber pressure
- Auxiliary chamber pressure
- Absolute value of the pressure difference
- Opening signal
- Closing signal
- Current Valve State

} Vehicle Body Features

Collected features:

- Body position
- Body velocity
- Body acceleration
- **Tire position**
- **Tire velocity**
- Main chamber pressure
- Auxiliary chamber pressure
- Absolute value of the pressure difference
- Opening signal
- Closing signal
- Current Valve State

} **Vehicle Tire Features**

Collected features:

- Body position
- Body velocity
- Body acceleration
- Tire position
- Tire velocity
- **Main chamber pressure**
- **Auxiliary chamber pressure**
- **Absolute value of the pressure difference**
- Opening signal
- Closing signal
- Current Valve State



Multi-chamber Pressure Variables

Collected features:

- Body position
- Body velocity
- Body acceleration
- Tire position
- Tire velocity
- Main chamber pressure
- Auxiliary chamber pressure
- Absolute value of the pressure difference
- **Opening signal**
- **Closing signal**
- **Current Valve State**

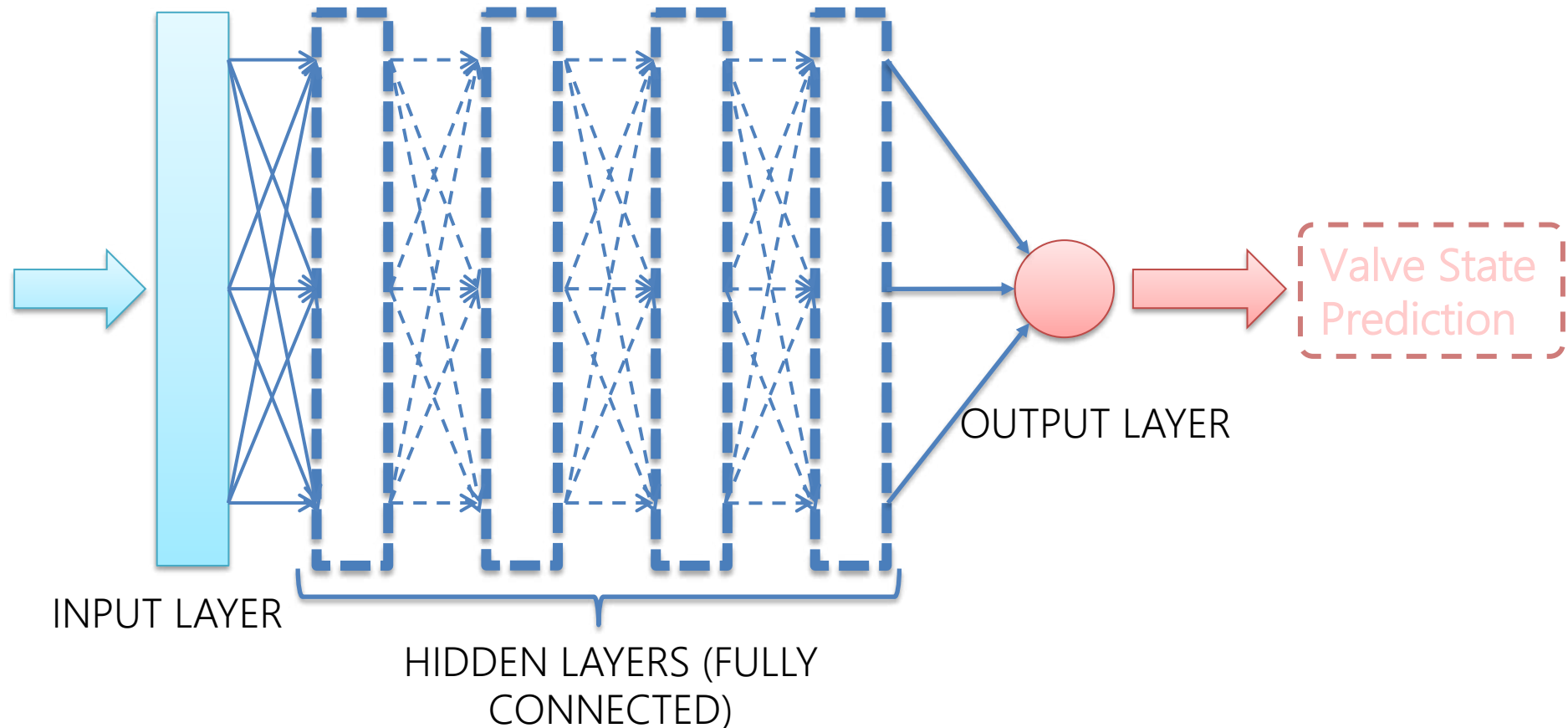
} **Multi-chamber Valve Variables**

Semi-Active Stiffness Control

Causal Control – Neural Network Based

INPUT DATA DIVISION:

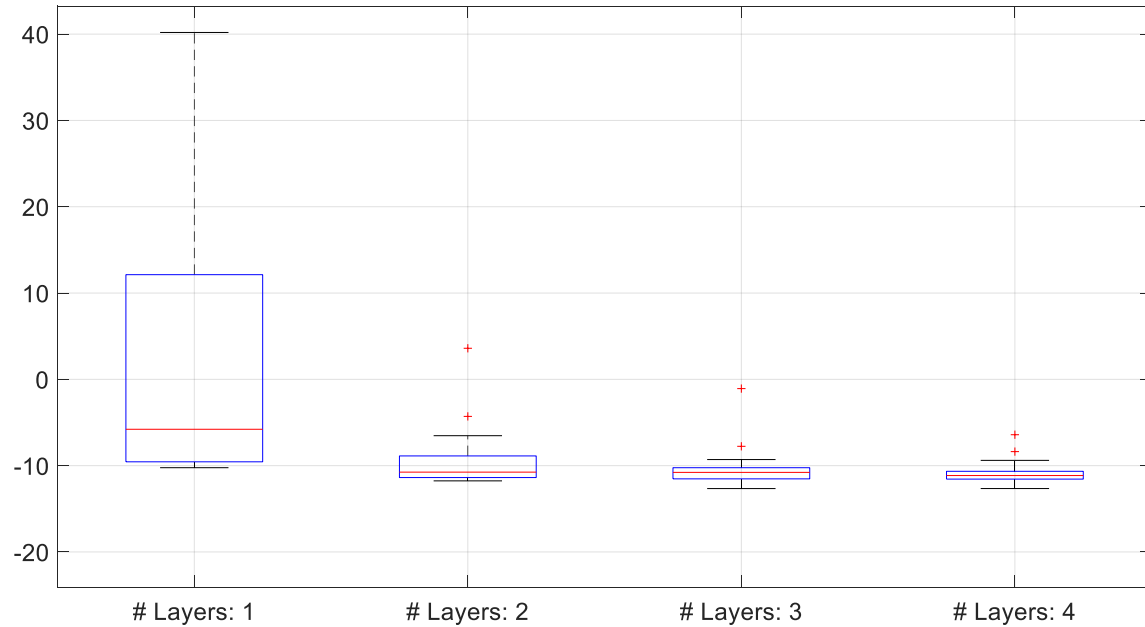
- 70% of the reduced dataset used as **TRAINING SET**.
- 15% used as **VALIDATION SET**
- 15% used as **TEST SET**



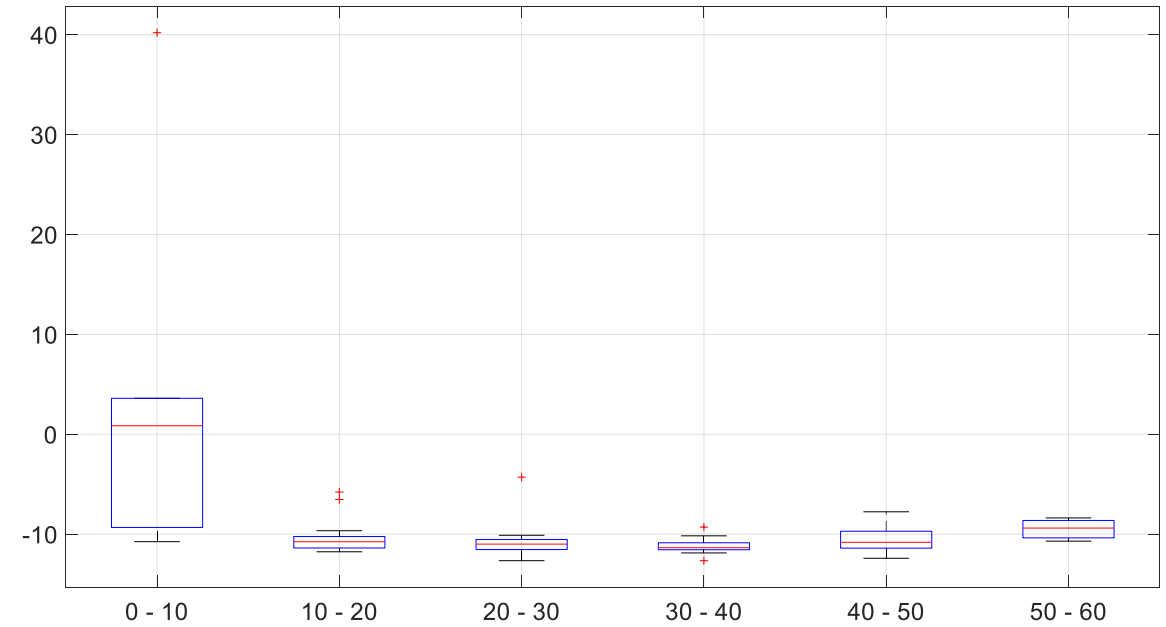
Semi-Active Stiffness Control

Causal Control – Neural Network Based

Performance mean at different number of layers



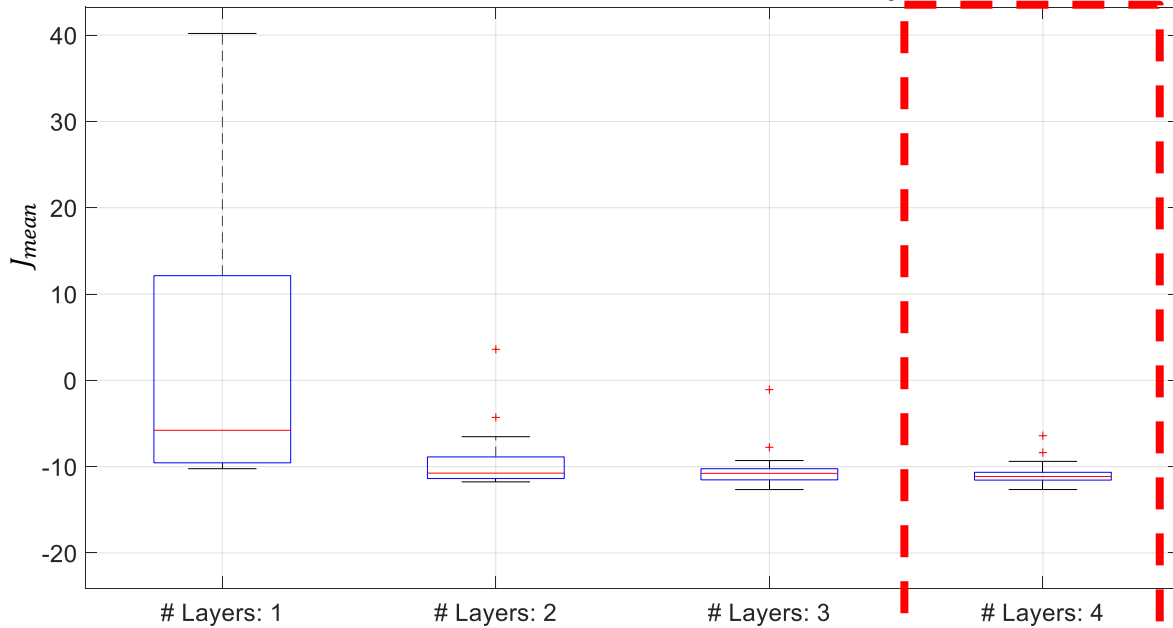
Performance mean at different number of neurons



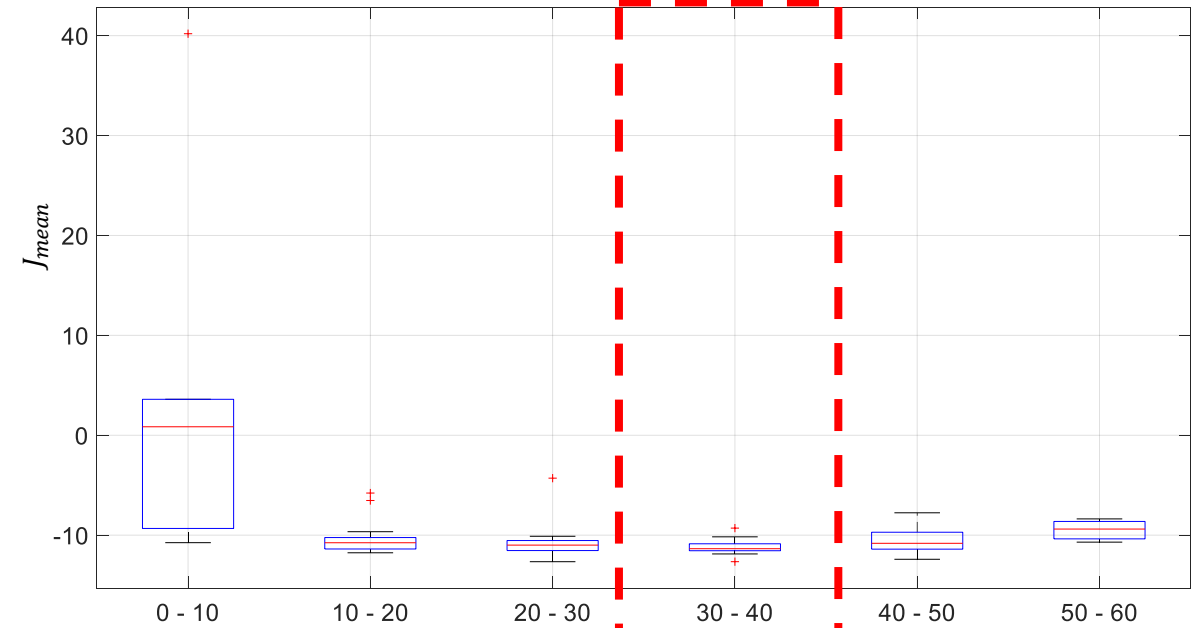
Semi-Active Stiffness Control

Causal Control – Neural Network Based

Performance mean at different number of layers



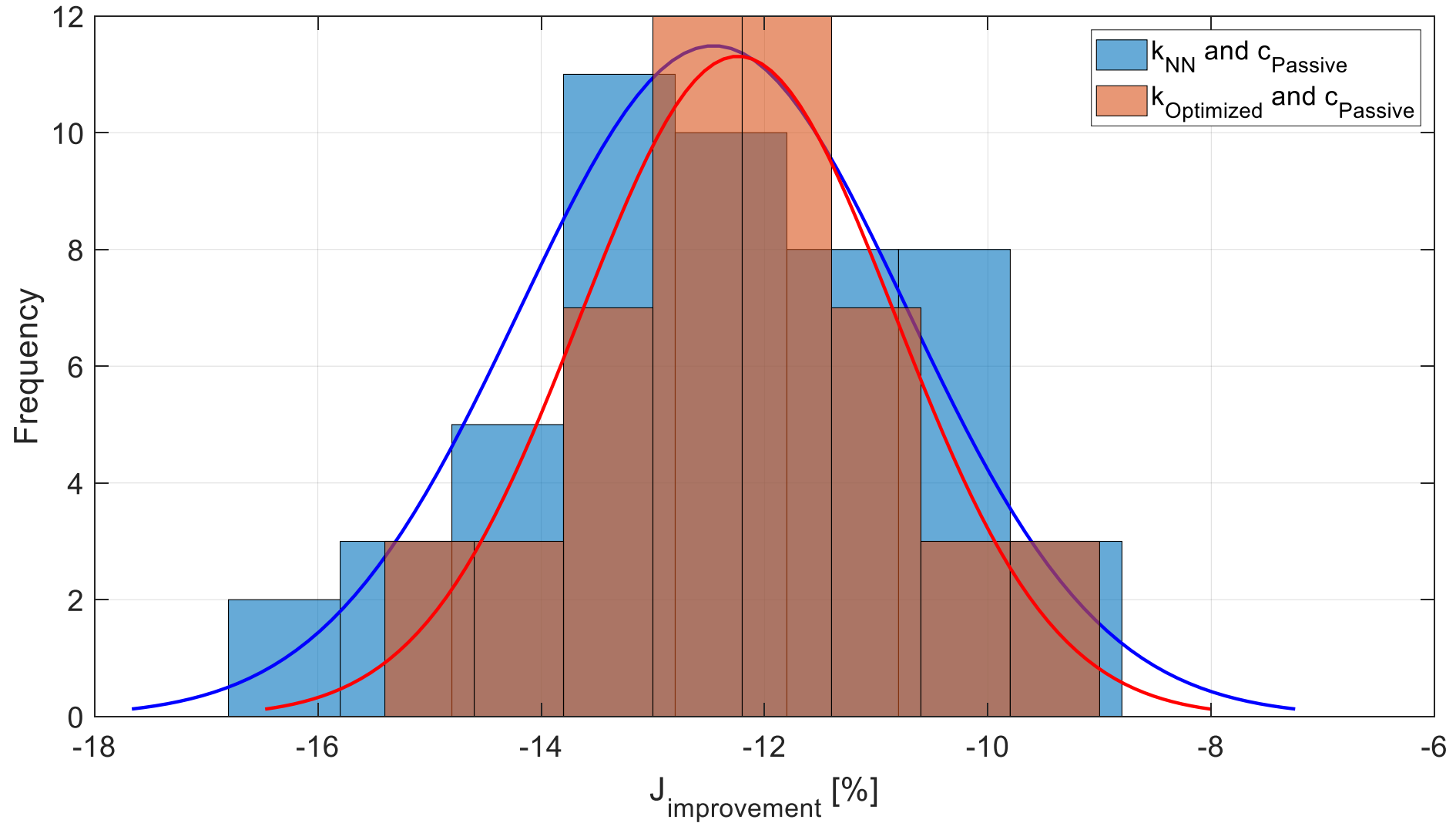
Performance mean at different number of neurons



Best Structure Configuration

Semi-Active Stiffness Control

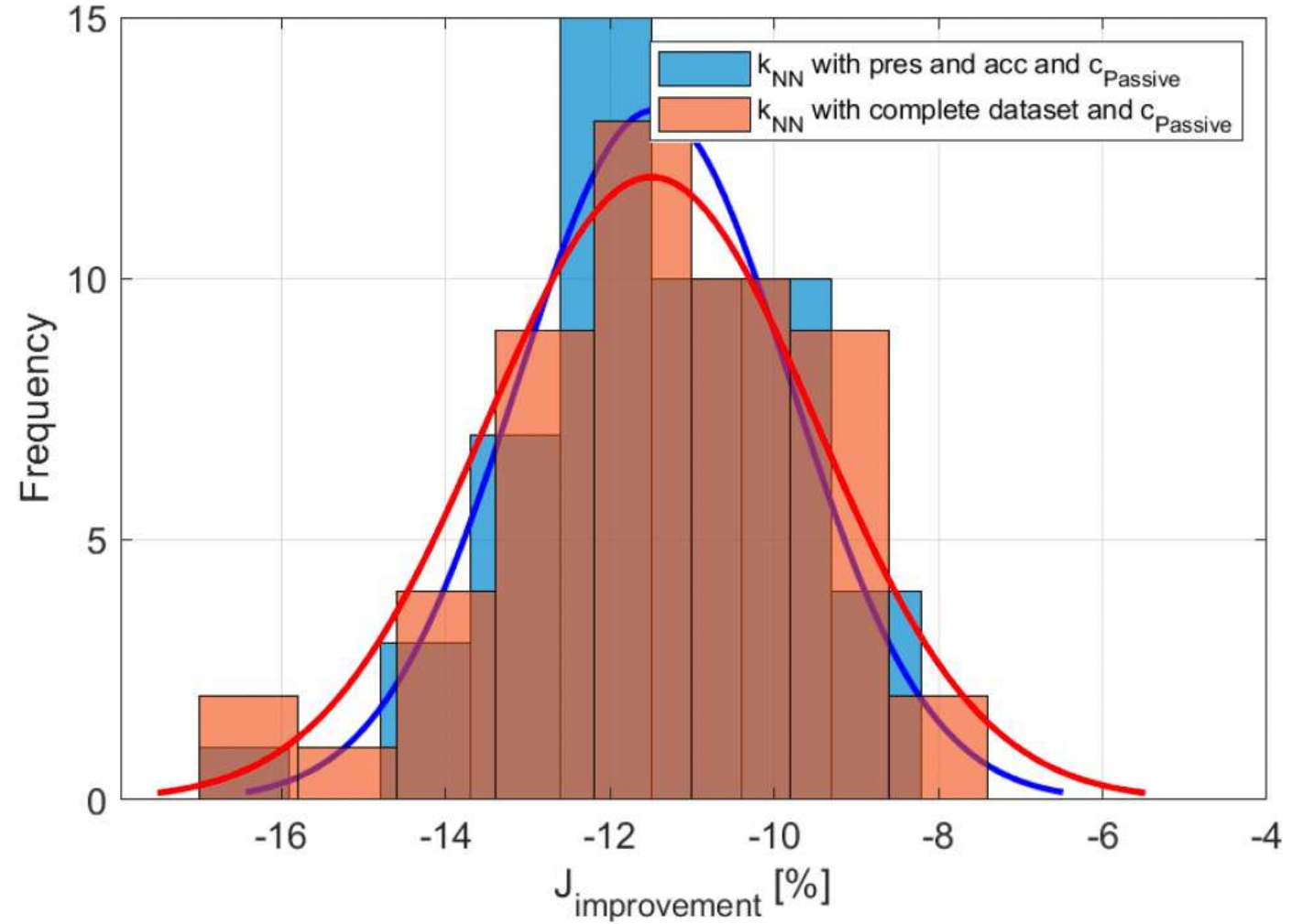
Causal Control – Neural Network Based



Semi-Active Stiffness Control

Causal Control – Neural Network Based

Feature Reduction Analysis



Semi-Active Stiffness Control

Causal Control

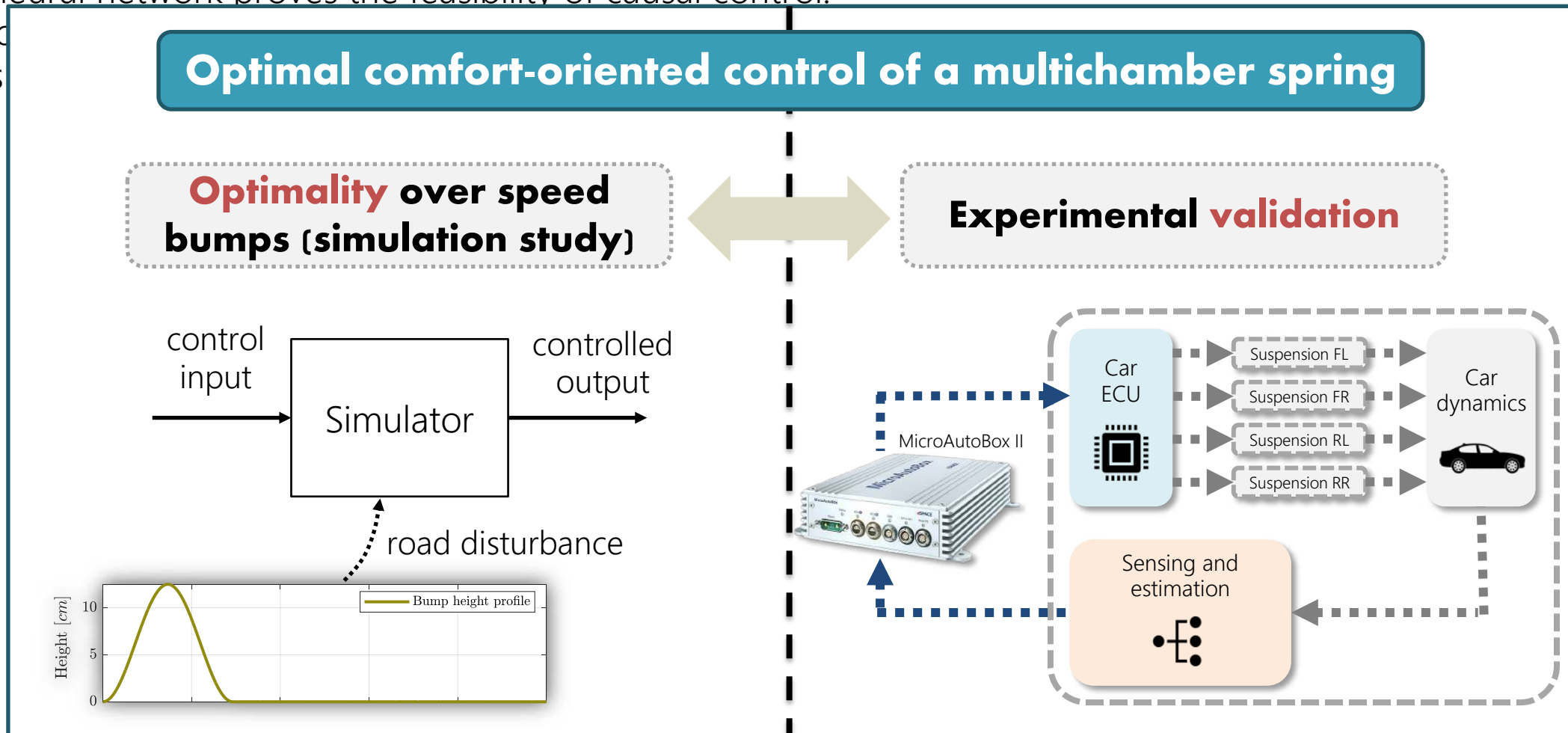
The neural network proves the feasibility of causal control.
Too complex for actual implementation
Does not provide an interpretation

Semi-Active Stiffness Control

Causal Control

The neural network proves the feasibility of causal control.

Too d
Does



Road preview



Comfort-oriented optimization

A Finite Horizon Optimal Control Problem is solved over an optimization horizon T_w in order to find a globally optimal input.

$$\min_{s_\tau, \tau=1, \dots, f_c T_w} \sqrt{\frac{1}{T_w} \int_{t_0}^{t_0+T_w} \ddot{z}_b(t)^2 dt}$$

Cost function

subject to:

$$x(t+i+1) = f(x(t+i), u(t+i))$$

Discretized model equations

$$x(t_0) = \tilde{x}(t_0)$$

Initial state

$$s_\tau \in \{0,1\}, \forall \tau = 1, \dots, f_c T_w$$

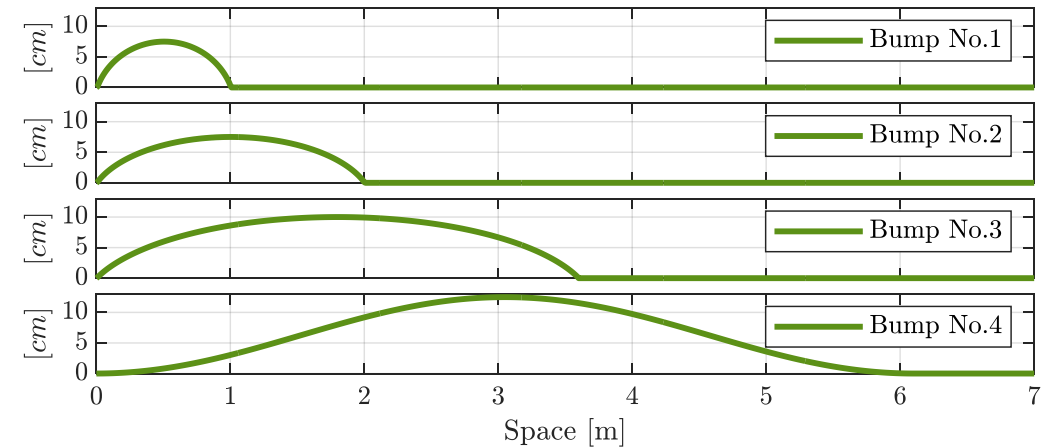
Input boundaries

$$z_r(t) = \tilde{z}(t), t \in [t_0, t_0 + T_w)$$

Road preview

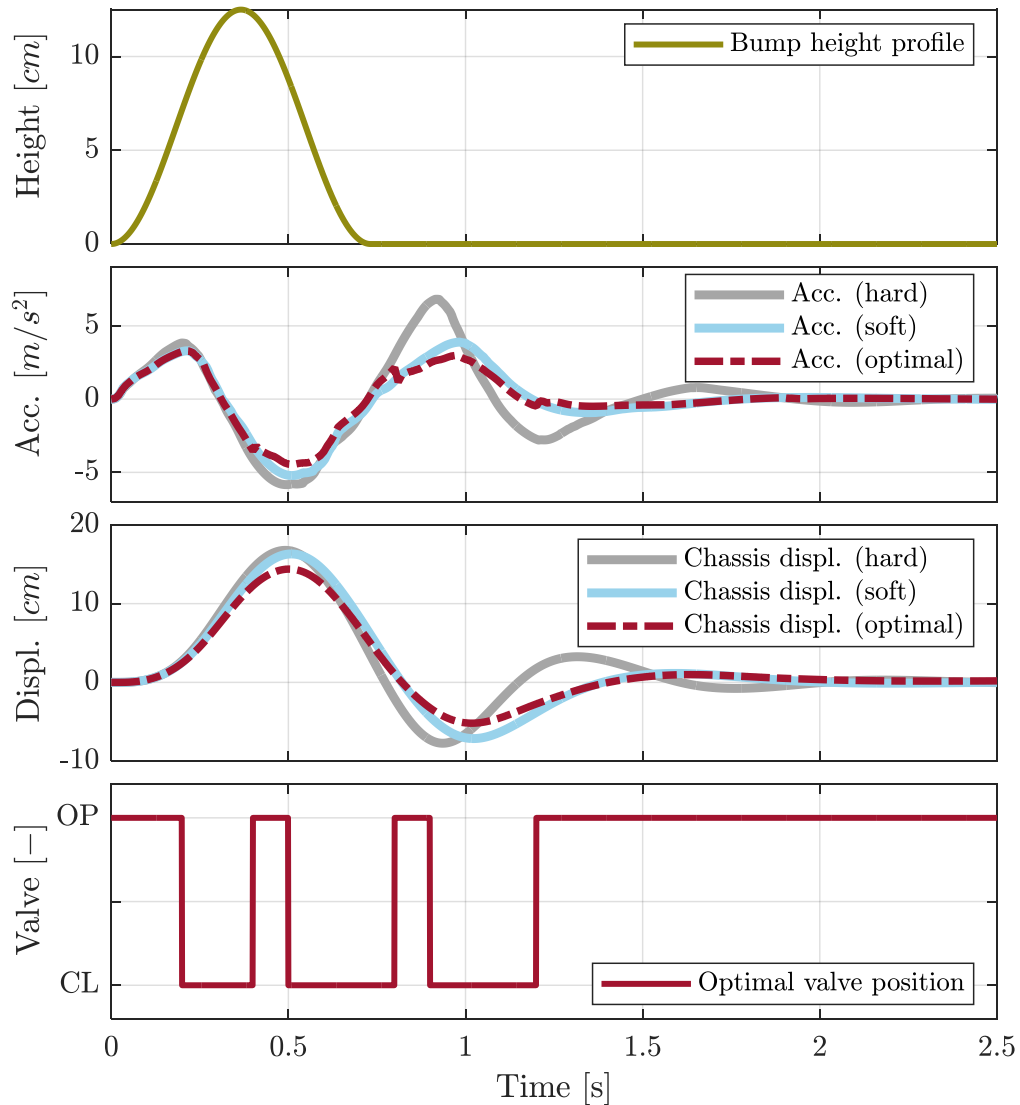
Assumption: road profile

Road preview is assumed. Four different bump types are considered.



Type	Height [cm]	Length [cm]
No. 1	7.5	100
No. 2	7.5	200
No. 3	10	360
No. 4	12.5	610

Optimization results



Optimal results

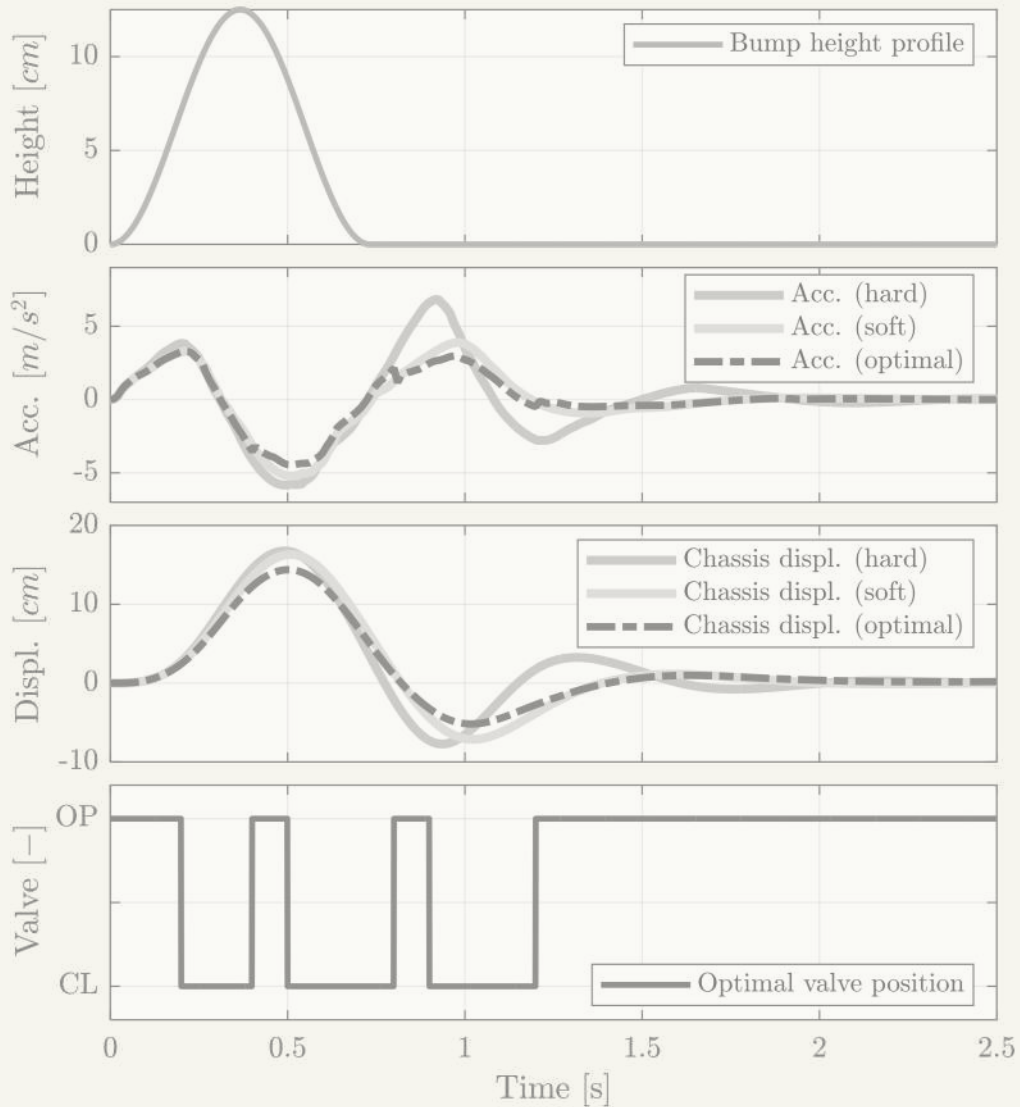
Vertical acceleration is reduced thanks to valve switching.

A bump is a single-event type of perturbation which particularly excites the **body resonance** ($\approx 1.2 \text{ Hz}$, most important chassis vertical movement).

Soft spring performs better than hard spring at the body resonance frequency and ensures a natural motion during settling.

The **controlled spring outperforms the passive configurations**, especially in the release phase of the bump, while keeping the motion natural.

Improvement indexes over bump types

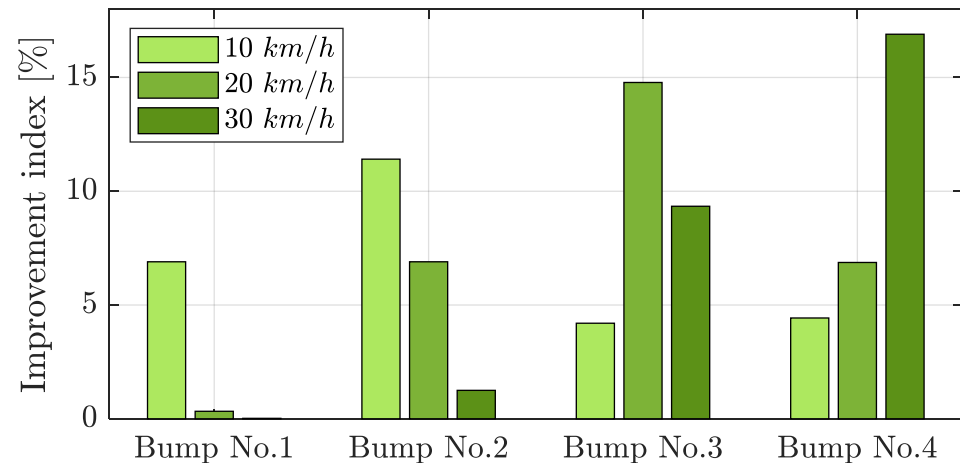


Take-home messages

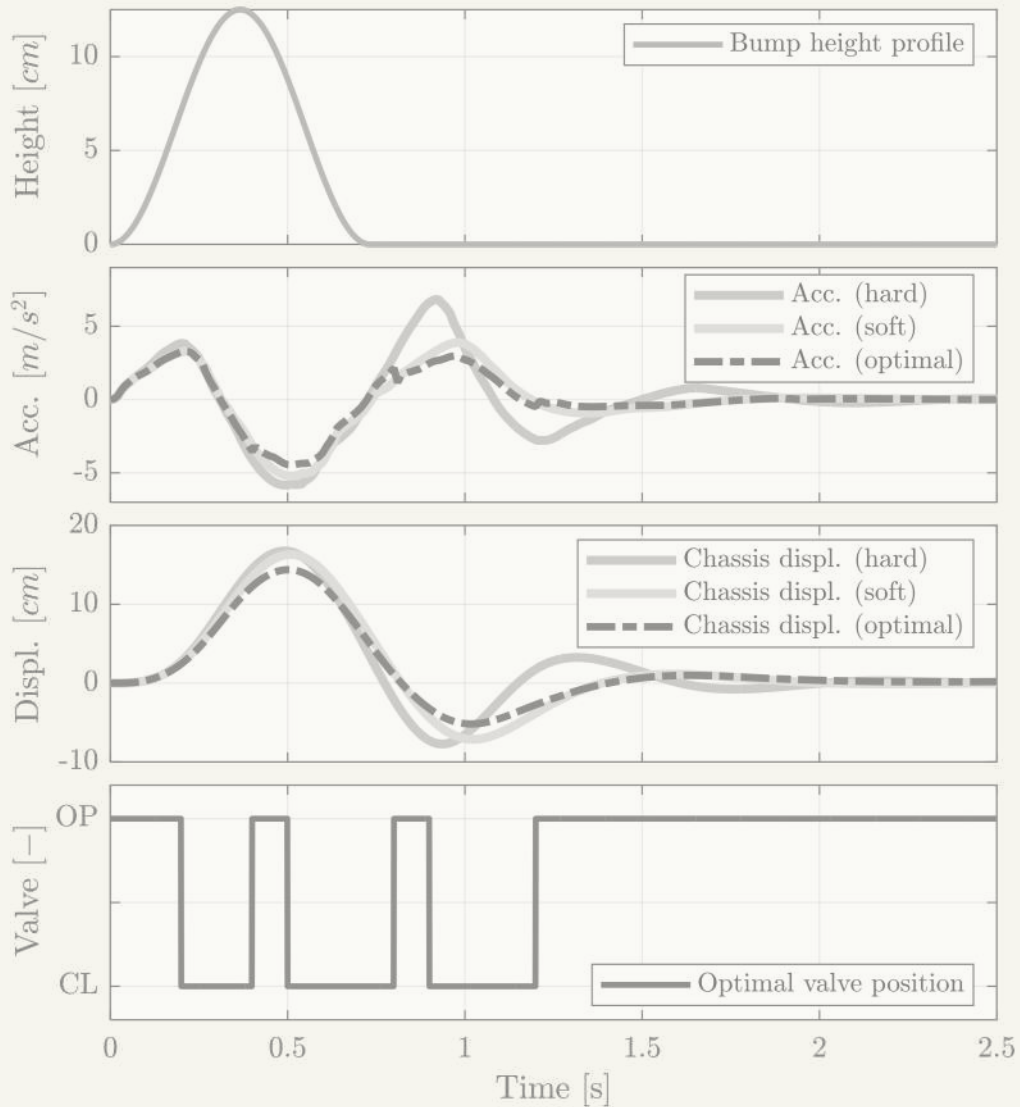
- Improvement indexes:

$$J_{impr} = \frac{J - J_{soft}}{J_{soft}} \times 100$$

Improvements are up to 17%, depending on the velocity. This result is consistent with the previous work.



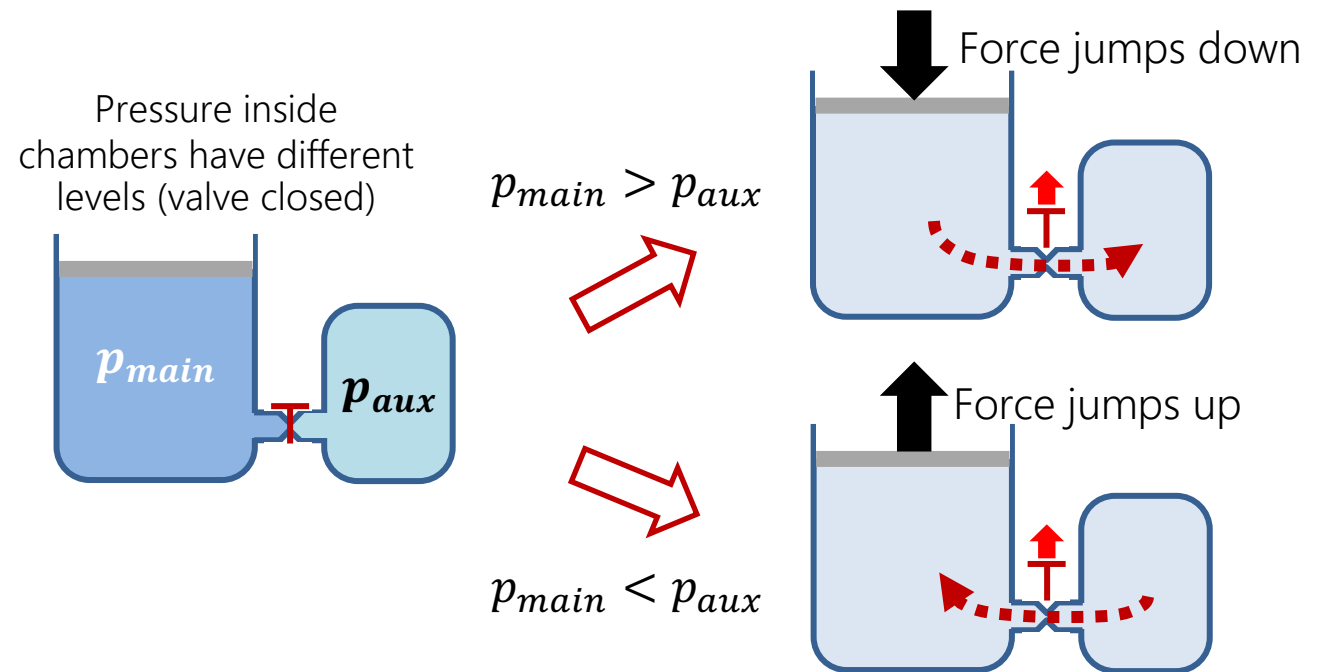
Energy release principle



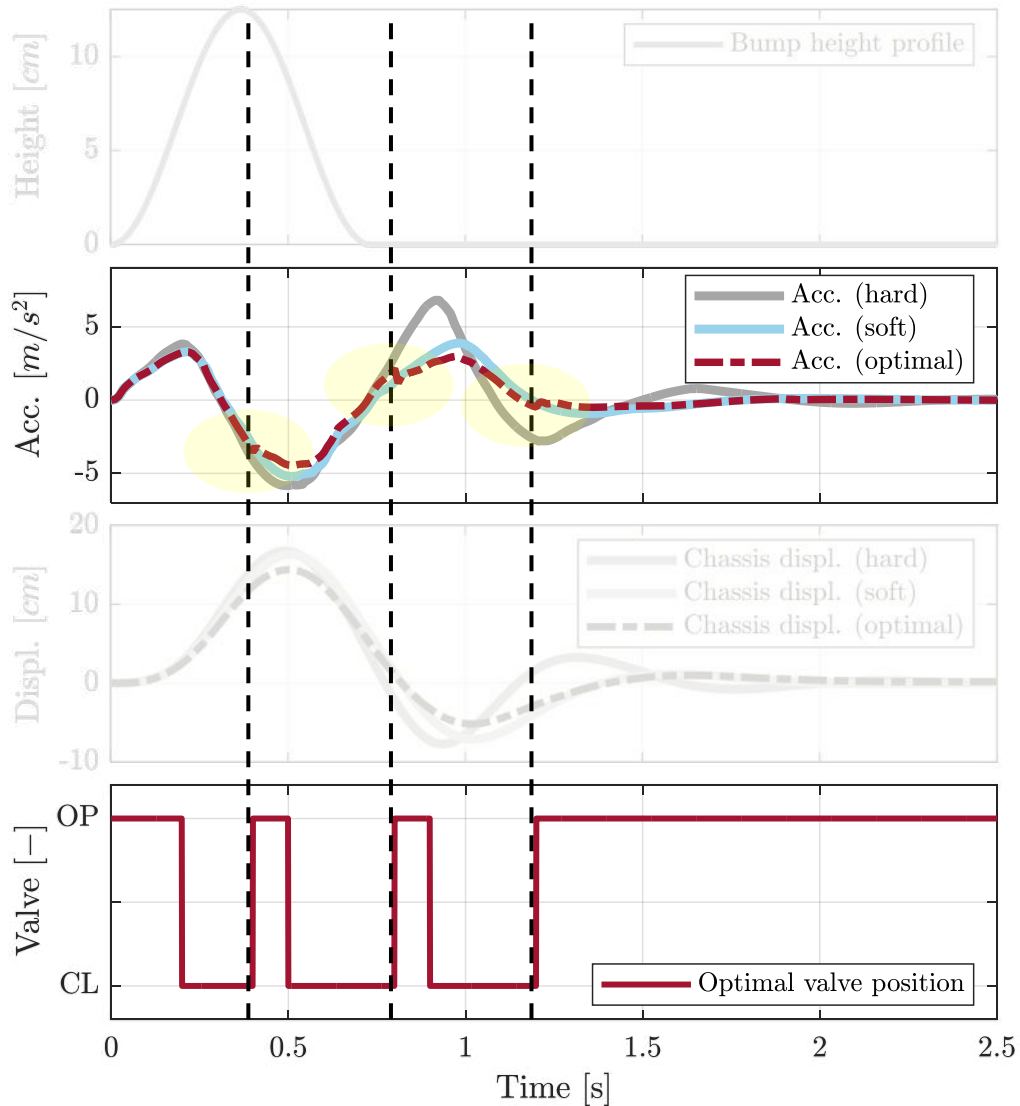
Take-home messages

☐ (controlled) energy release principle

It is a physical way to insert active energy into the system, by storing and releasing pressurized air by valve switching.



Energy release principle



(controlled) energy release principle

The valve is **optimally closed** so to create unequally pressurized chambers (energy storage phase).

Air is released by opening at an instant where the kick force is beneficial for the vertical acceleration.

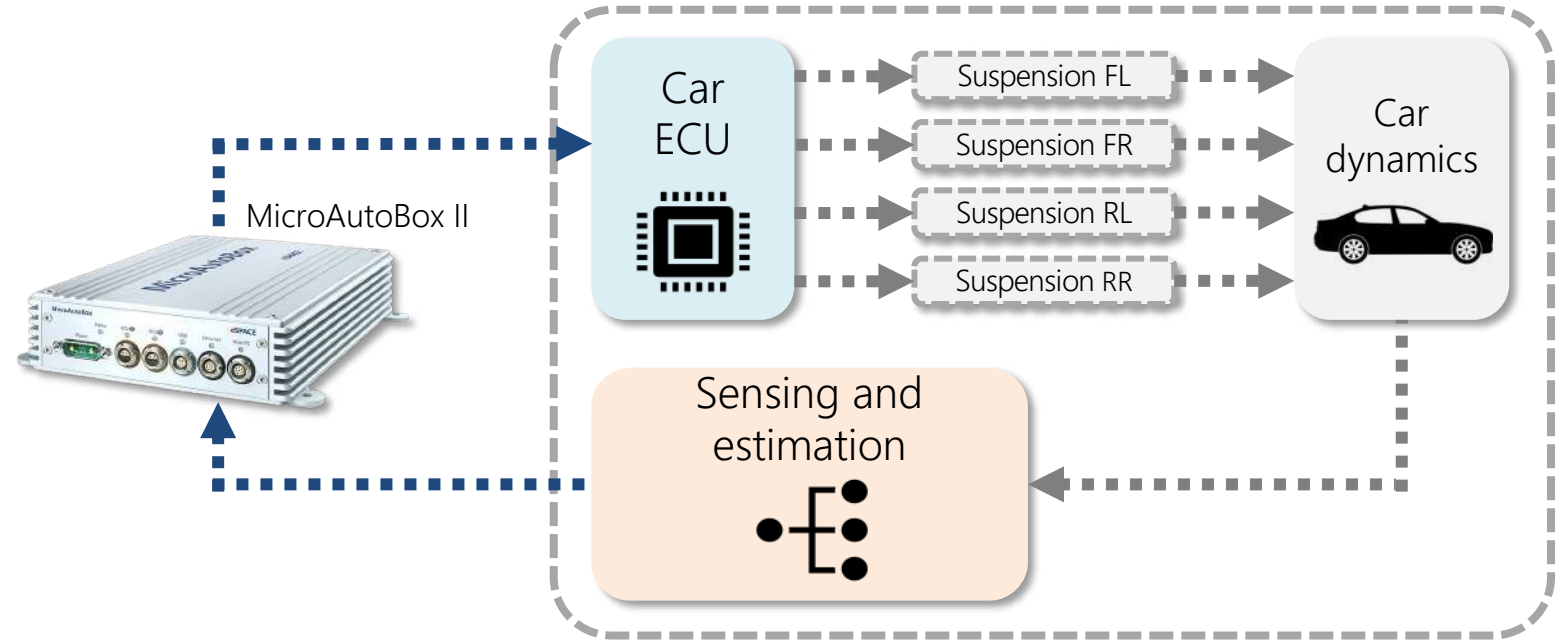
Optimal opening happen in proximity of the maxima (and minima) of the vertical acceleration, so to cut the wave peaks.

Experimental setup

□ Availability of 4 multichamber air springs.

The control strategy is computed by an external rapid prototyping ECU and is applied independently to the four suspensions.

- **Delay (estimated)** due to transmission and actuation: 30 ms
- **Control sampling time:** 100 ms



□ Comfort indexes:

- Single corner vertical accelerations (given by single-axis accelerometers)
- Vehicle pitch rate (given by a central 6-DOF IMU)



Openloop strategy with activation threshold

How to make optimal control «online»

Closed-loop global strategy

The ECU should at each iteration:

1. preview in advance the road profile;
2. solve an optimization problem.

Impossible to tackle in practice with current available computational power.

Openloop strategy with activation threshold

How to make optimal control «online»

Closed-loop global strategy

The ECU should at each iteration:

1. preview in advance the road profile;
2. solve an optimization problem.

Impossible to tackle in practice with current available computational power.

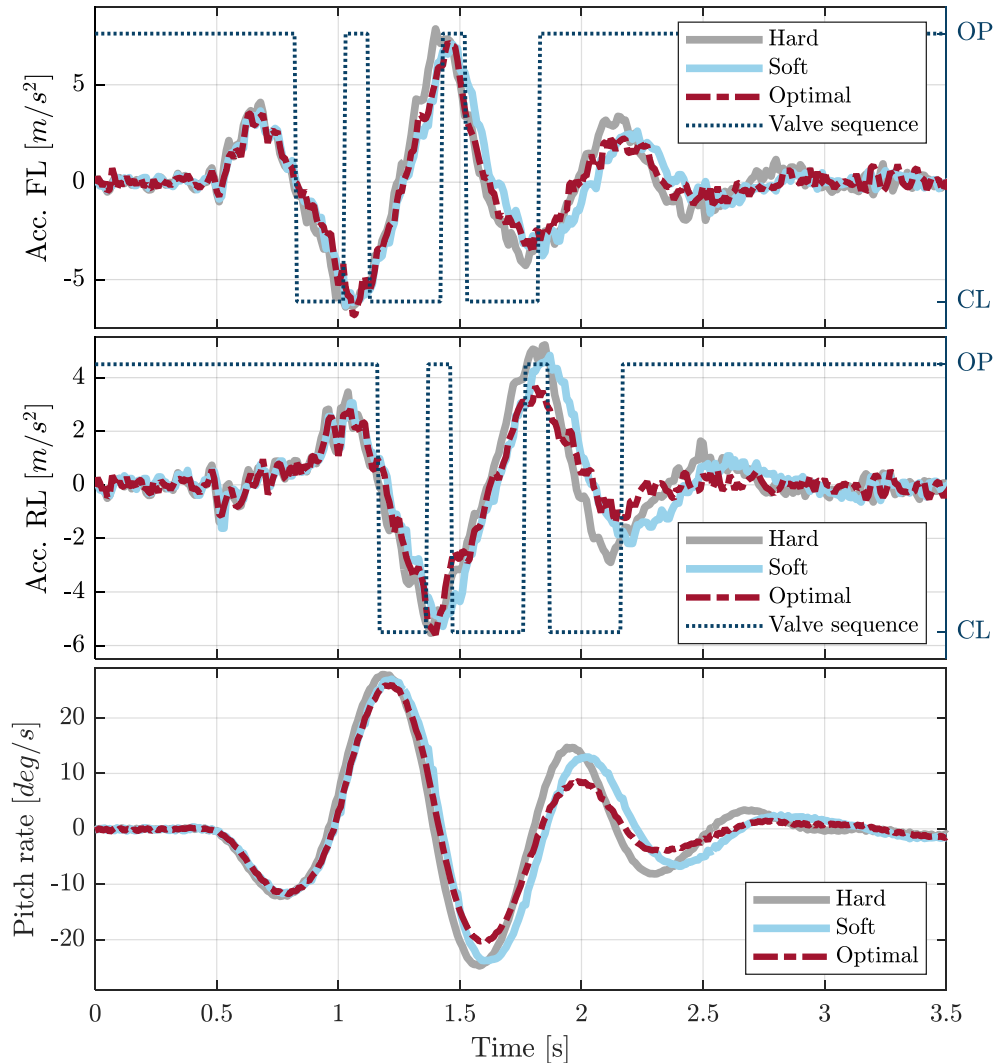
Open-loop strategy with activation threshold

The ECU at each iteration:

1. Takes values of acceleration;
2. **Apply in open loop** the global optimal valve sequence (found offline using same system parameters) when a threshold in acceleration is exceeded.

Activation threshold [2 m/s^2] is chosen robustly to noise and disturbances.

Experimental results



Experimental results

FL corner, RL corner and pitch rate as signals of interest.

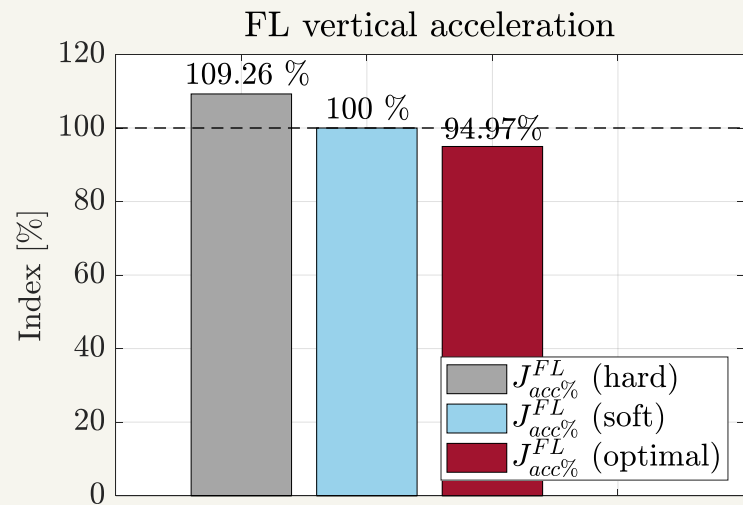
Dynamic valve switching **outperforms** the passive benchmark in all corners. Performance are higher in the bump release (in line with expectations).

Inequalities in the front/rear acceleration corners are given by a **different suspension sizing**. Also, performance can be enhanced by lowering delays.

The **pitch rate is positively affected** by suspension control, even though only acceleration minimization is enforced in the control problem.

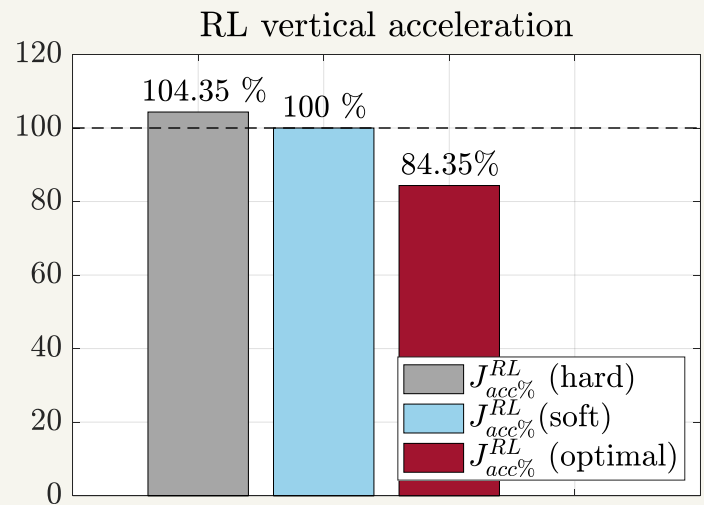
Experimentally measured performance indexes

□ Experimental indexes (normalized with respect to soft passive configuration)



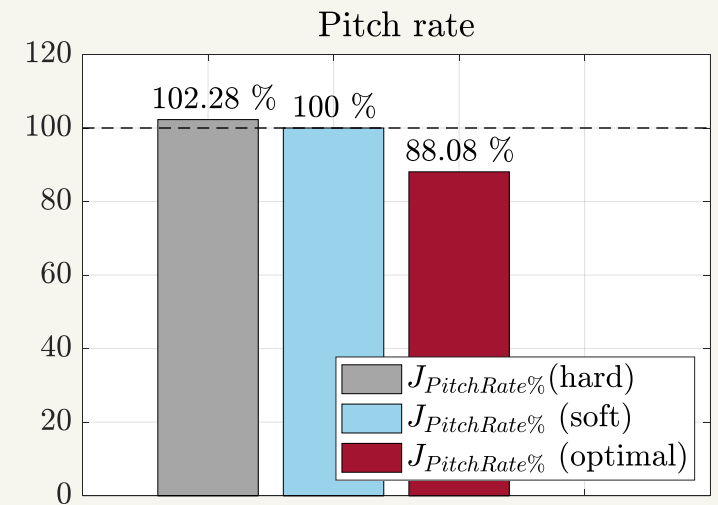
5%

improvement on front acceleration



16%

improvement on rear acceleration



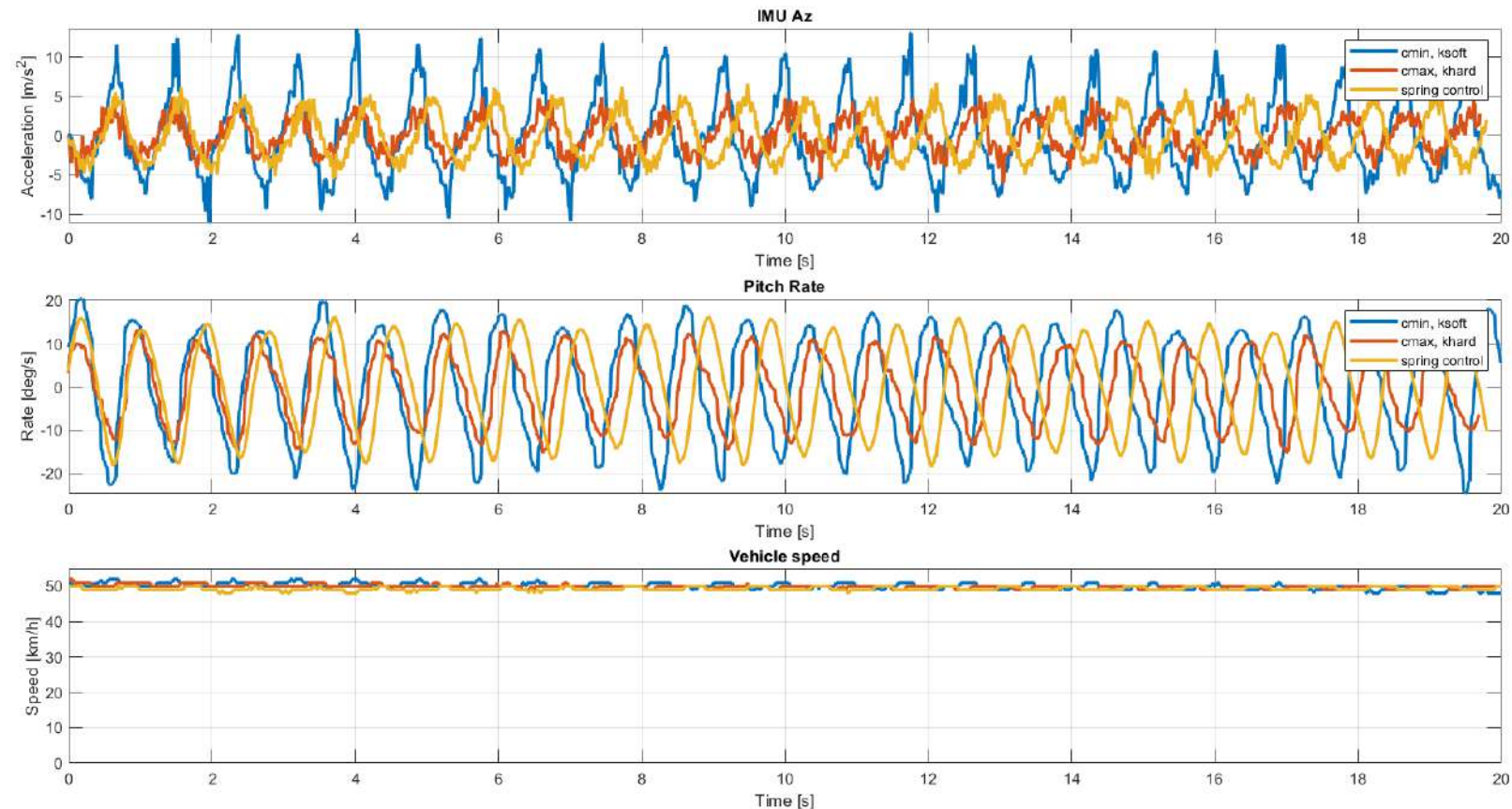
12%

improvement on pitch rate

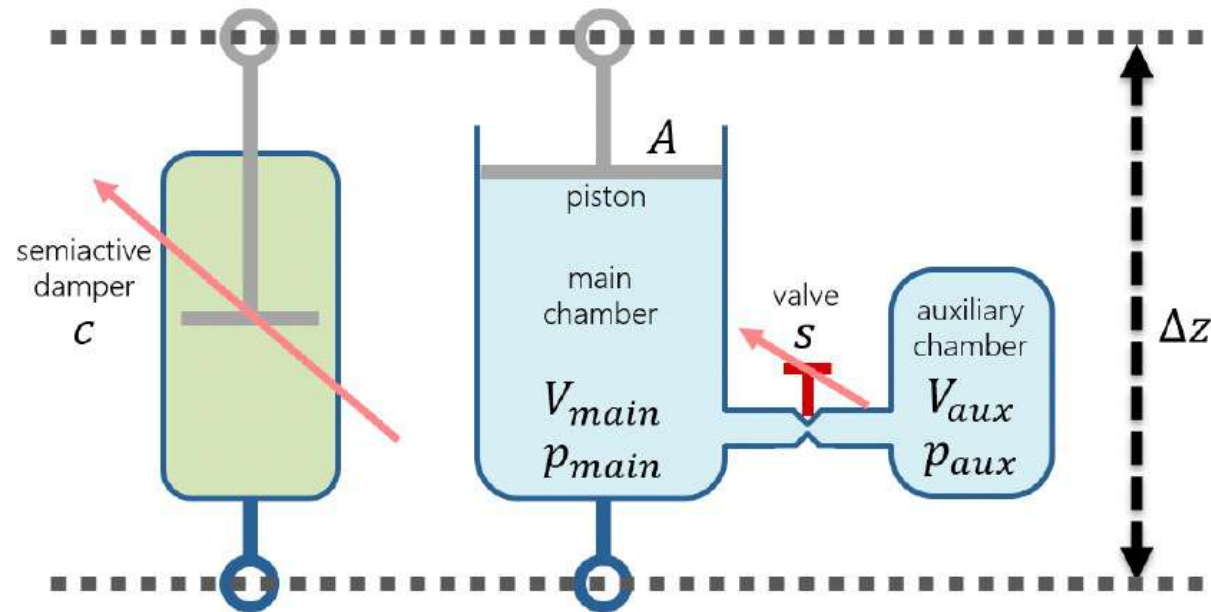
First experimental evidence of benefits induced by stiffness modulation

Experimentally measured performance indexes

The Energy release principle can be used to derive a SH-like causal control law for semi-active stiffness control.

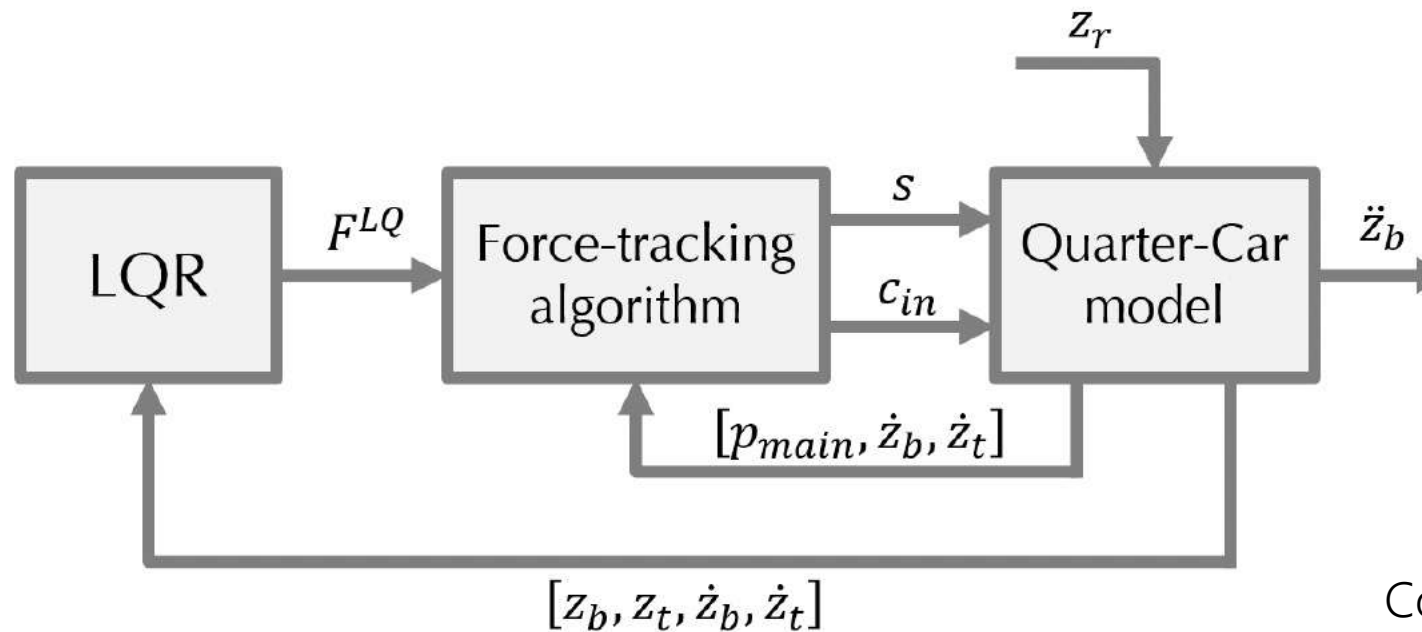


Coordinated Stiffness and Damping Control



$$F_{susp} = F_c + F_k$$

Coordinated Stiffness and Damping Control with a hierarchical control system



$$\dot{\mathbf{x}} = \mathbf{A}\mathbf{x} + \mathbf{B}F^{LQ}$$

$$F^{LQ} = -\mathbf{K}\mathbf{x}$$

$$J^{LQ} = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T [\ddot{z}_b^2 + \rho \Delta z^2] dt$$

Comfort oriented control

Avoid end of stroke

Stiffness and Damping Control

Force tracking algorithm

The force tracking algorithm tries to minimize $e_F = F_{act} - F^{LQ}$

where $F_{act} = -c\Delta\dot{z} + (p_{main} - p_{atm})A - Mg$

Daisy chain algorithms:

Semi-Active

$$1) \quad c_{in} = \text{sat}_{[c_{min}, c_{max}]} \frac{(p_{main} - p_{atm})A - Mg - F^{LQ}}{\Delta\dot{z}}$$

Priority goes to the damper because of smoothness

2) The ideal chamber pressure is:

$$p_{main}^* = p_{atm} + \frac{1}{A} [c_{in} \Delta \dot{z} + Mg + F^{LQ}]$$

the main chamber pressure is not a directly controllable variable, a pressure tracking logic is needed

Semi-Active

$$\dot{p}_{main} = \frac{-p_{main} \gamma A}{V_{main,0} + A \Delta z + s \cdot V_{aux}} \cdot \Delta \dot{z}$$

the valve position s does not change the sign of the pressure derivative, (that depends on the stroke speed only), but affects its absolute value, which increases with closed valve and decreases vice-versa.

Stiffness and Damping Control

When $(p_{main} - p_{main}^*)\Delta\dot{z} > 0$

We have two options

$$(p_{main} - p_{main}^*) > 0 \text{ and } \Delta\dot{z} > 0$$

P_{main} is greater than desired one

P_{main} will decrease

Speed up the increase \rightarrow close the valve

Stiffness and Damping Control

When $(p_{main} - p_{main}^*)\Delta\dot{z} > 0$

We have two options

$$(p_{main} - p_{main}^*) < 0 \quad \text{and} \quad \Delta\dot{z} < 0$$

P_{main} is smaller than desired one

P_{main} will increase

Speed up the increase \rightarrow close the valve

Stiffness and Damping Control

```
while  $t \leq t_{end}$  do  
  if  $(p_{main} - p_{main}^*)\Delta\dot{z} > 0$  then  
     $s_t = 0$   
  end if  
  if  $(p_{main} - p_{main}^*)\Delta\dot{z} < 0$  OR  $\Delta\dot{z} = 0$  then  
    if  $|p_{eq} - p_{main}^*| < |p_{main} - p_{main}^*|$  then  
       $s_t = 1$   
    else  
       $s_t = s_{t-1}$   
    end if  
  end if  
  if  $p_{main} - p_{main}^* = 0$  then  
     $s_t = s_{t-1}$   
  end if  
   $t \leftarrow t + 1$   
end while
```

Equilibrium pressure.

Wait until you are close to the equilibrium pressure to open the valve

Stiffness and Damping Control

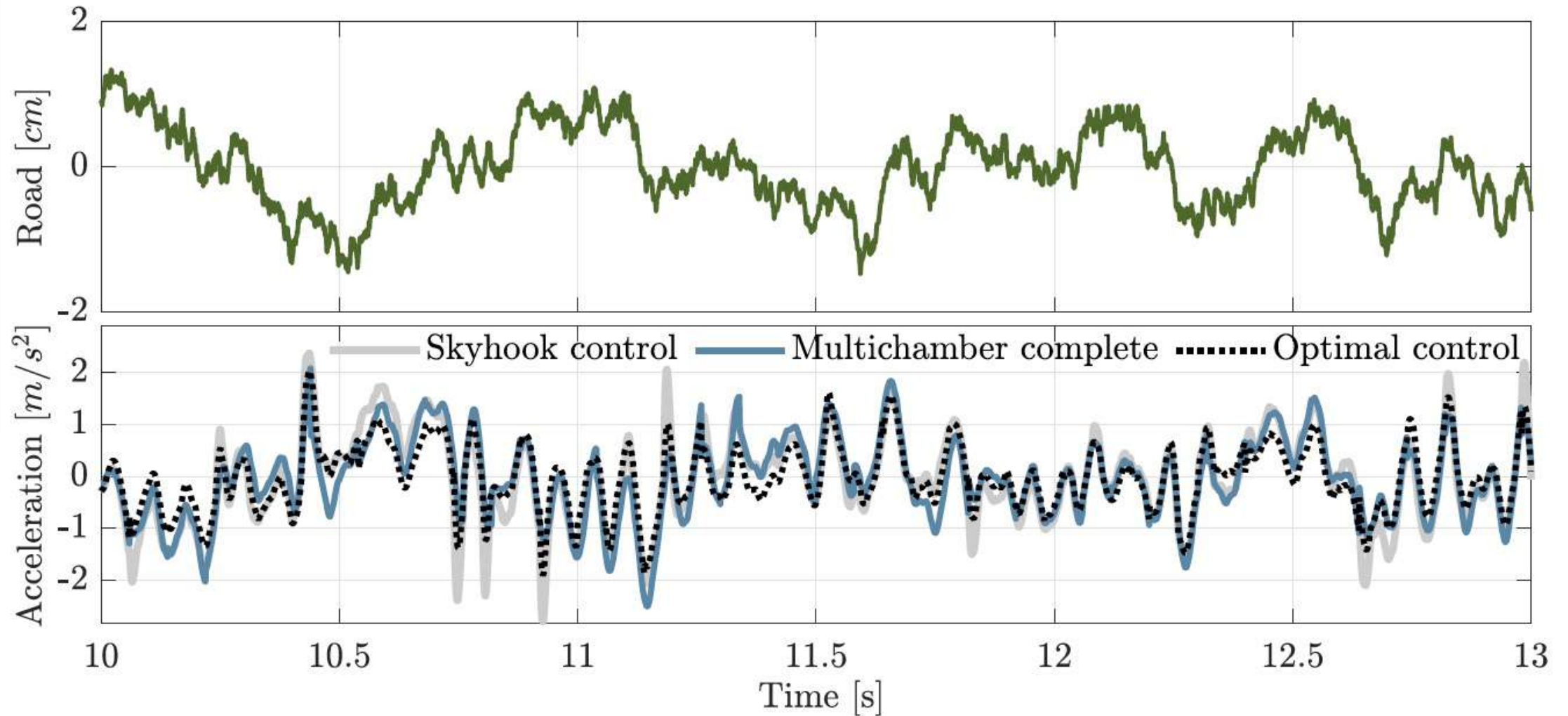
```
while  $t \leq t_{end}$  do  
  if  $(p_{main} - p_{main}^*)\Delta\dot{z} > 0$  then  
     $s_t = 0$   
  end if  
  if  $(p_{main} - p_{main}^*)\Delta\dot{z} < 0$  OR  $\Delta\dot{z} = 0$  then  
    if  $|p_{eq} - p_{main}^*| < |p_{main} - p_{main}^*|$  then  
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    else  
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    end if  
  end if  
  if  $p_{main} - p_{main}^* = 0$  then  
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  end if  
   $t \leftarrow t + 1$   
end while
```

Equilibrium pressure.

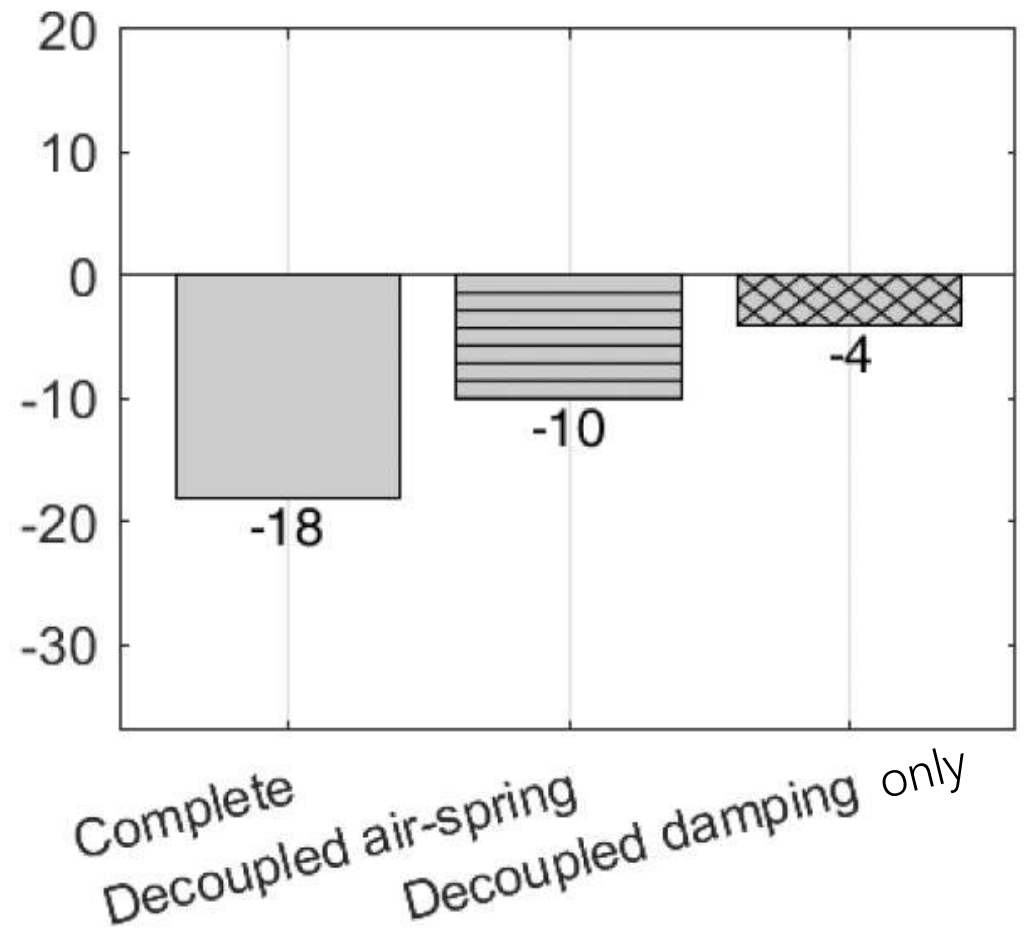
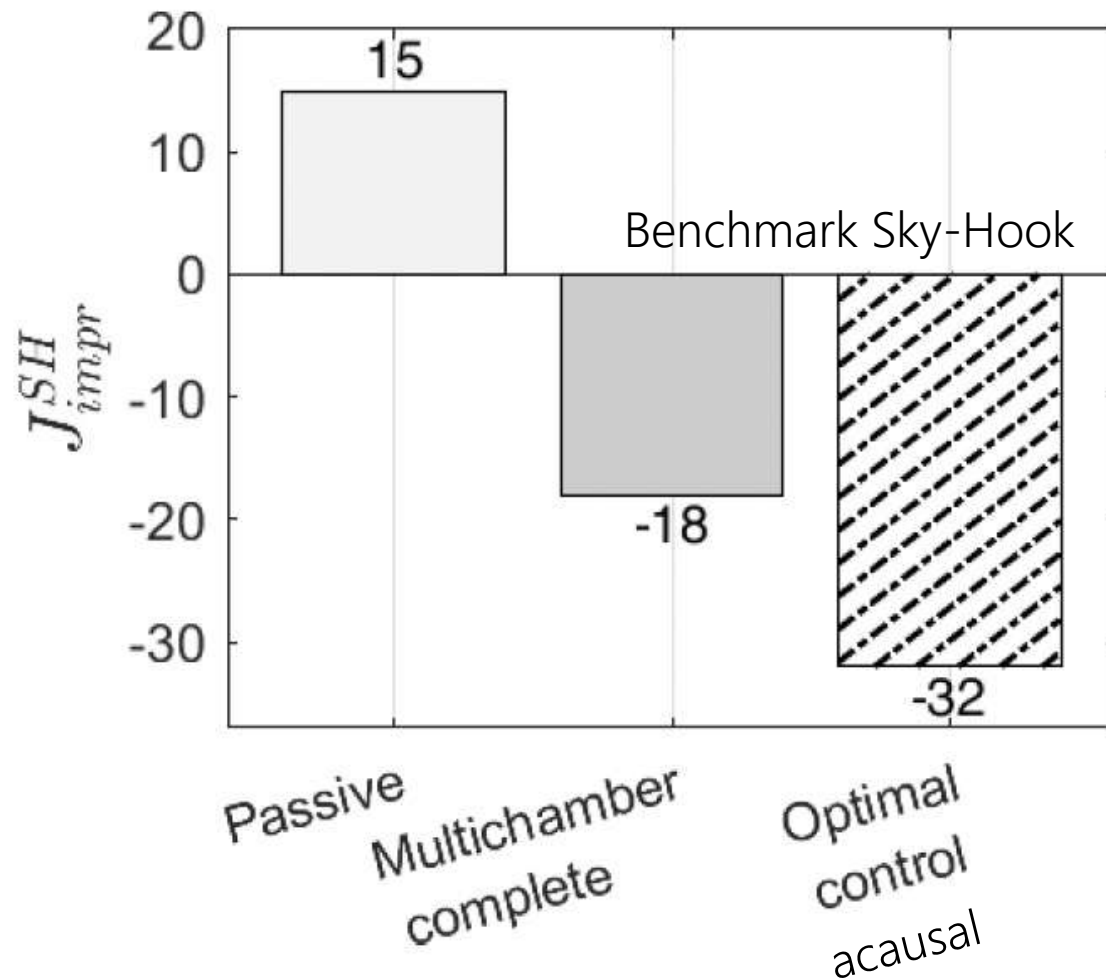
Wait until you are close to the equilibrium pressure to open the valve

It is a discrete time algorithm

Stiffness and Damping Control

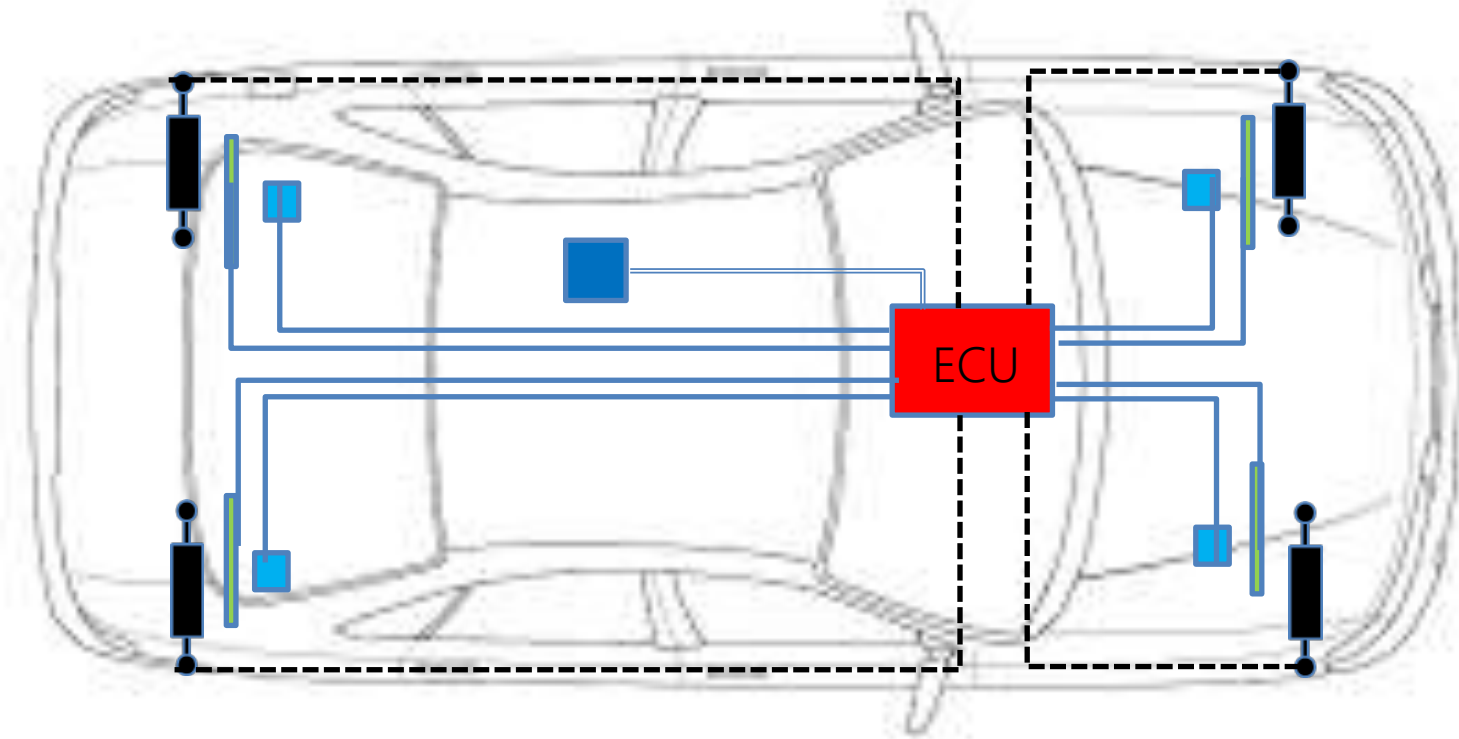


Stiffness and Damping Control



- Introduction
- Semi-Active Damping Control
 - Actuators
 - Models
 - Benchmark
 - Causal Control
- Semi-Active Stiffness Control
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- **Sensing Preliminaries**
- A look at the future
- Conclusions

Sensing Preliminaries



Semi-active damper



Elongation (stroke) sensor



Vertical accelerometer (Az)
sensor (body-side)



*CoG IMU (3 accelerations
and 3 gyros) - Optional*



Electronic Control Unit

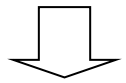
Sensing Preliminaries

Physical sensors (signal + noise):

- Body-accelerometer $\ddot{z} + d_a$
- Stroke sensor $(z - z_t) + d_e$

Body speed estimation

$$V(s) = A(s) \frac{1}{s} + D(s) \frac{1}{s}$$



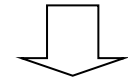
$$V(s) = A(s) \frac{1}{s + \varepsilon} + D(s) \frac{1}{s + \varepsilon}$$

$$\varepsilon = 2\pi \cdot 0.1$$

(OK beyond 0.1Hz)

Stroke speed estimation

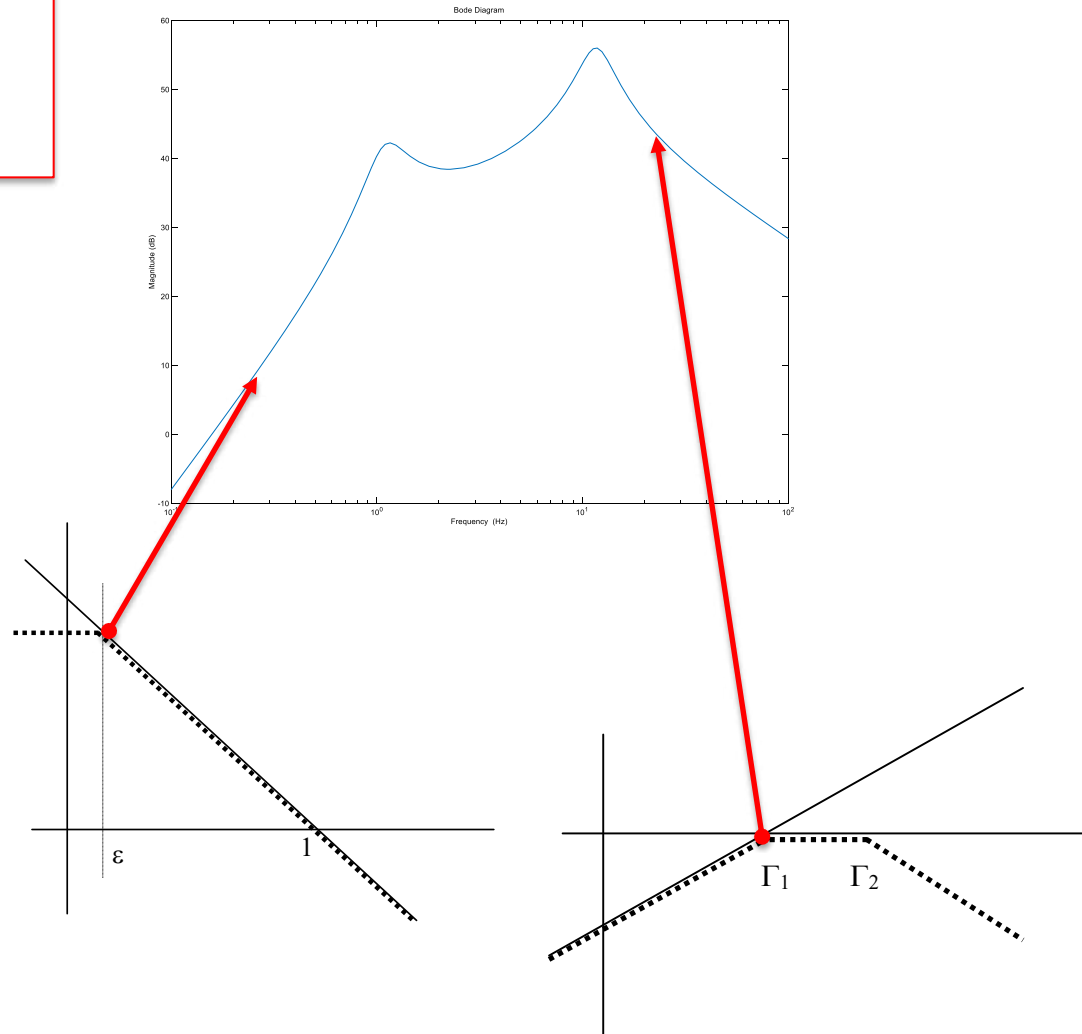
$$V(s) = sZ(s) + sD(s)$$



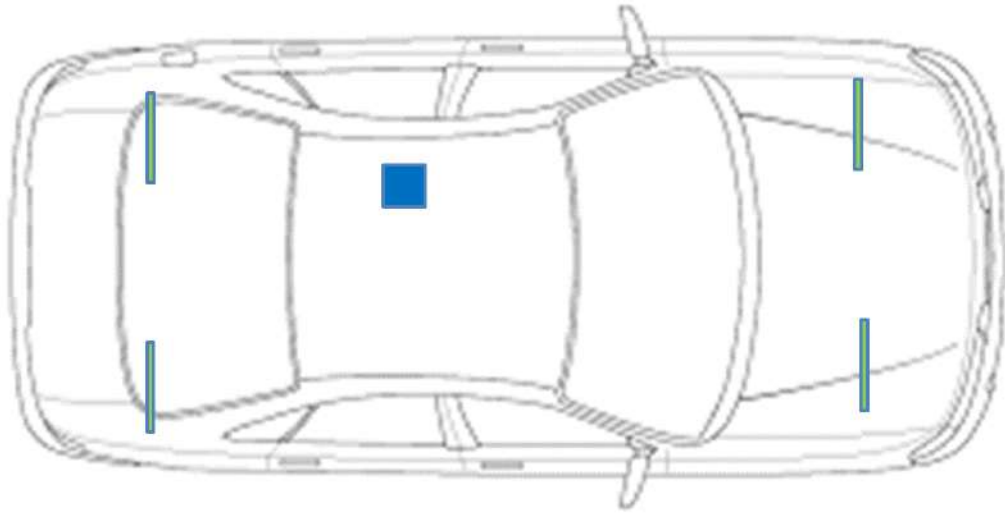
$$V(s) = (Z(s) + D(s))s \frac{\Gamma_1}{s + \Gamma_1} \frac{\Gamma_2}{s + \Gamma_2}$$

$$\Gamma_1 = 2\pi \cdot 20, \Gamma_1 < \Gamma_2$$

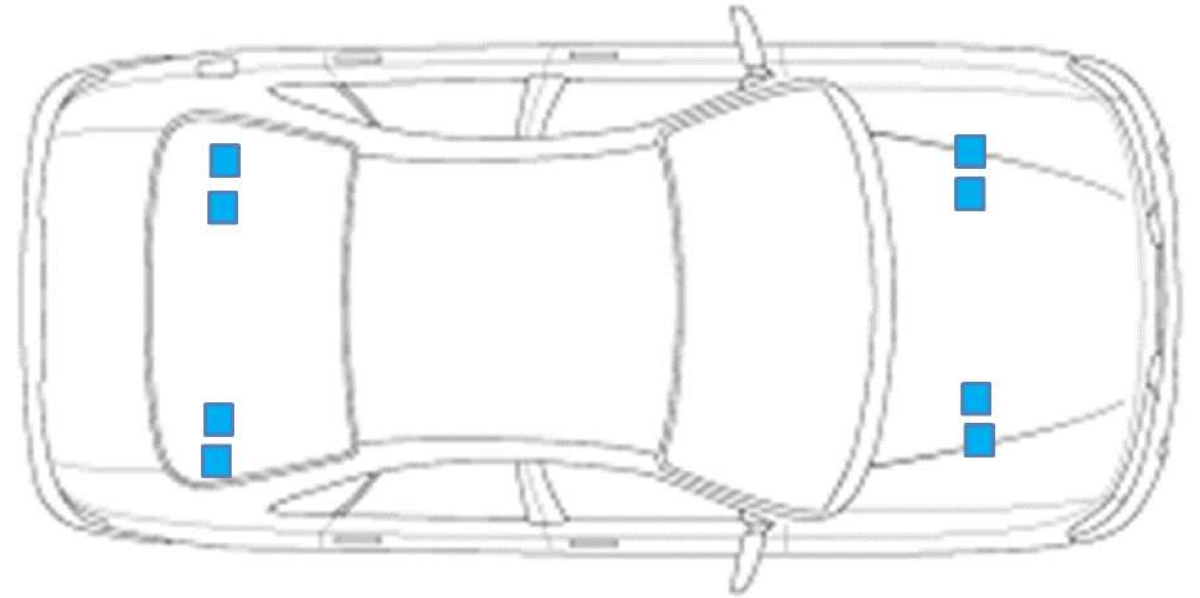
(OK below 20Hz)



Sensing Preliminaries

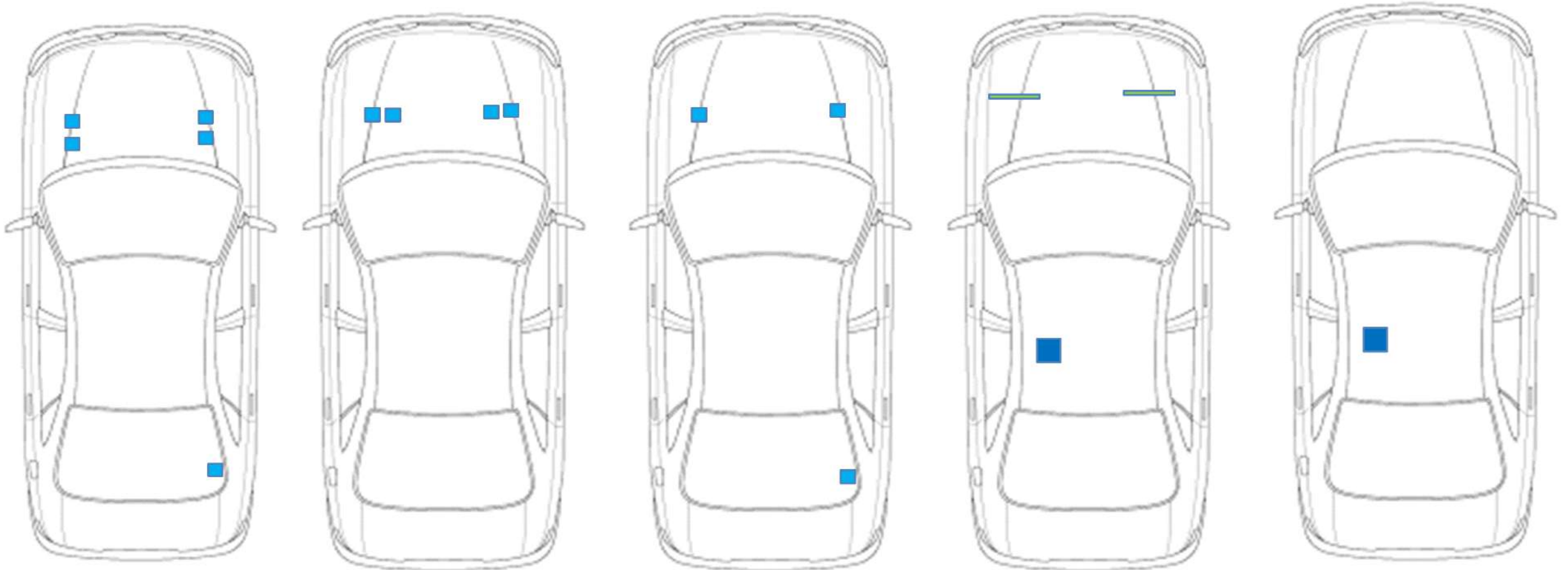


4 elongation sensors only + IMU



4 «twins» of accelerometers

Sensing Preliminaries

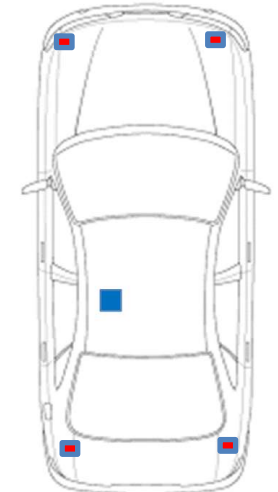
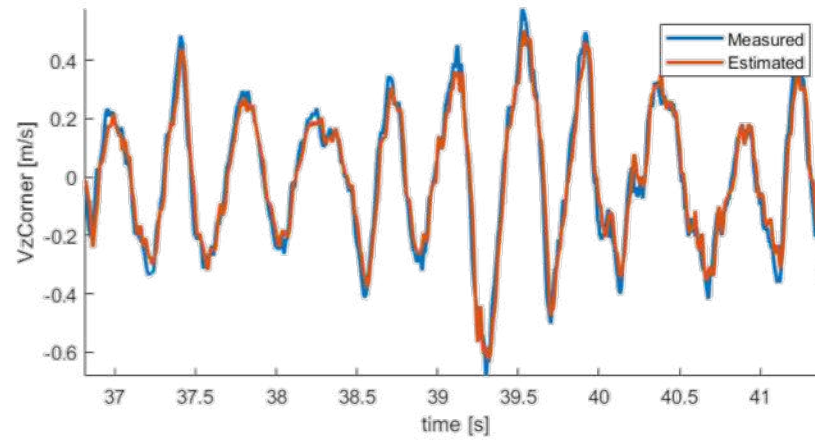
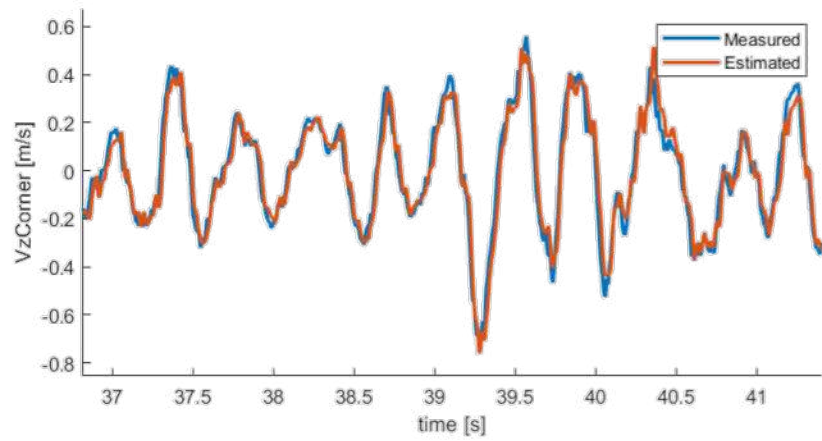
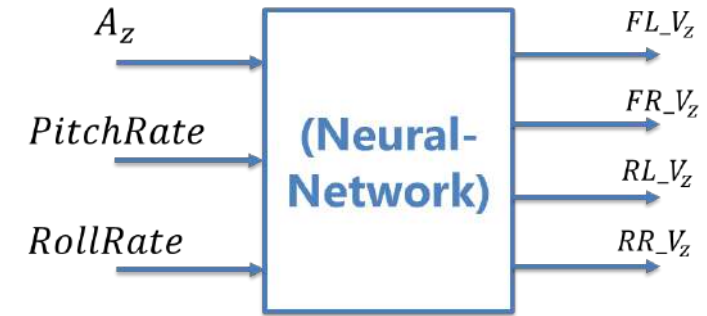
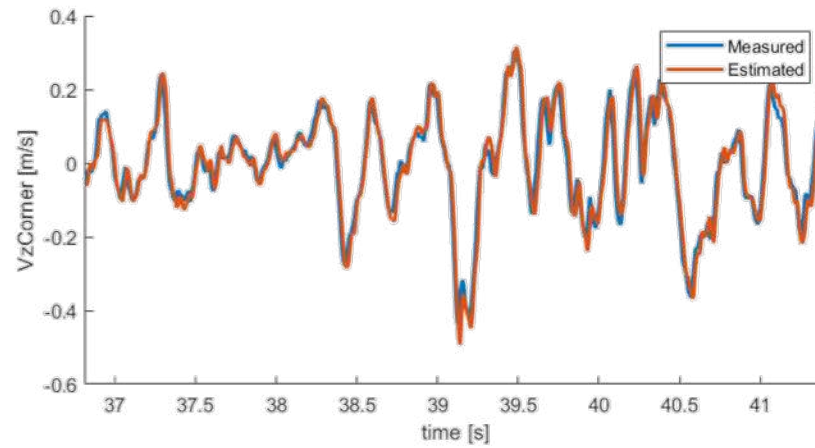
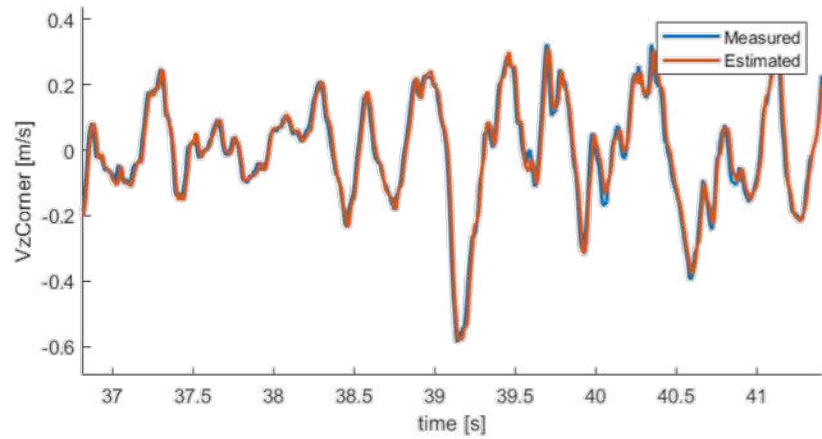


Cost and HW-complexity reduction;
reduction

SW-sensing complexity increase;

performance

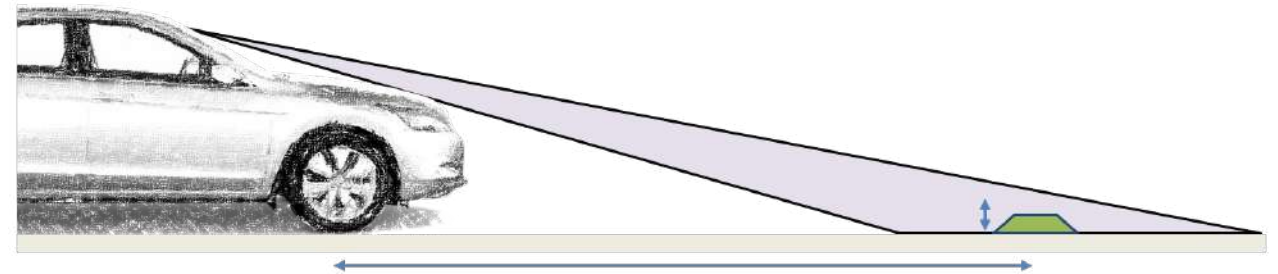
Sensing Preliminaries



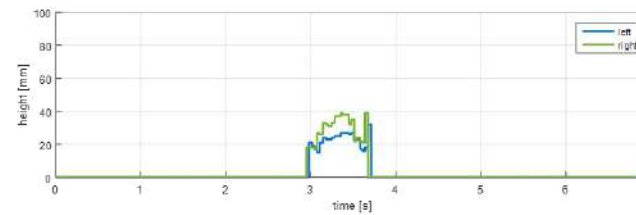
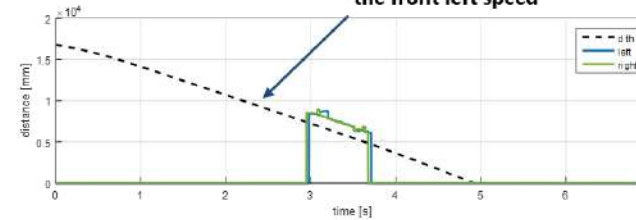
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Future Development

Road Preview



Theoretical distance from bump obtained integrating the front left speed



Low speed (< 15 km/h)

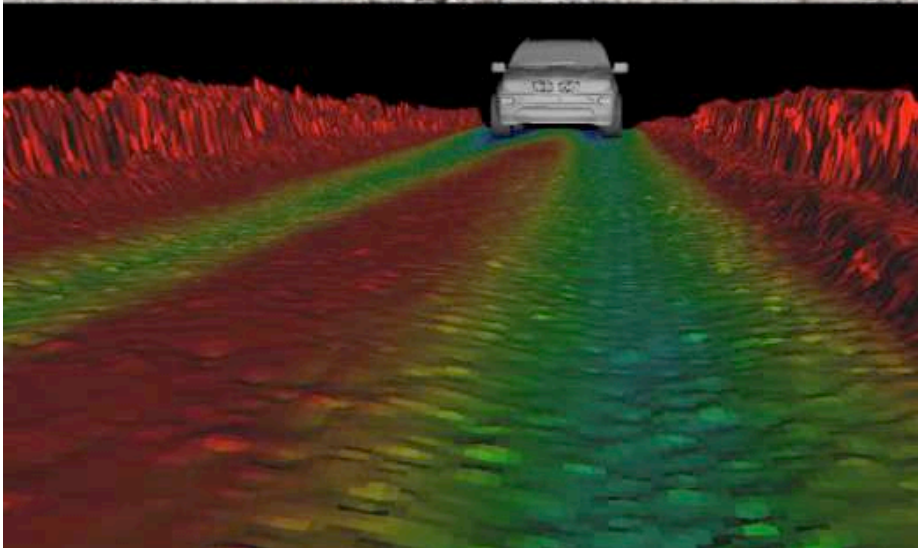
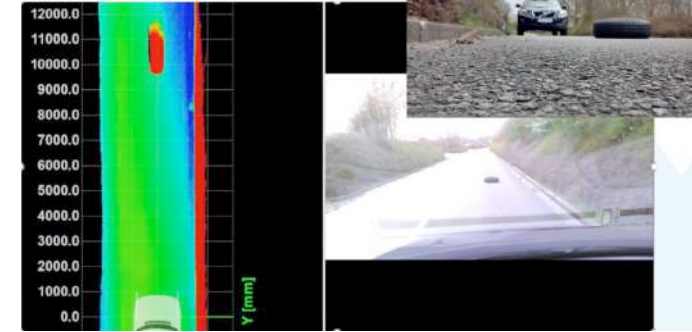


Future Development

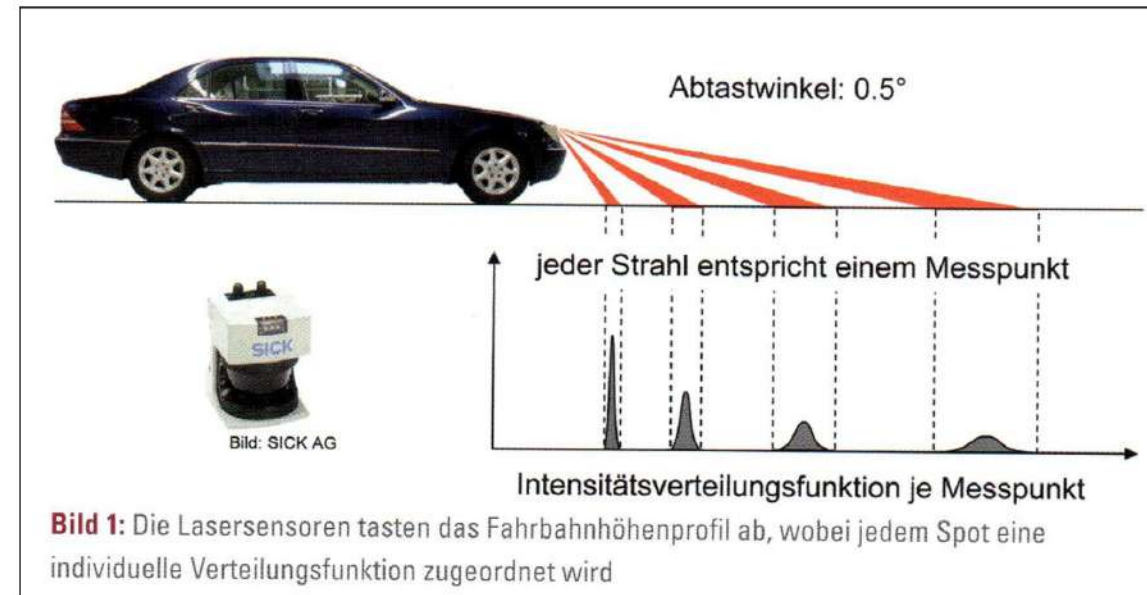
Road Preview



XenoWare applications

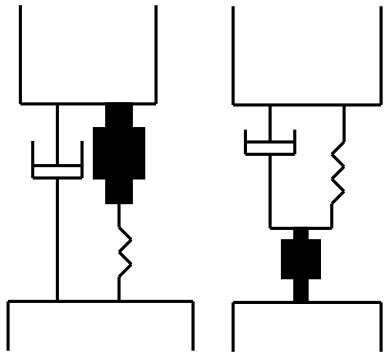


Challenge:
integrate
navigation
AND road-
scanning
LIDARS?



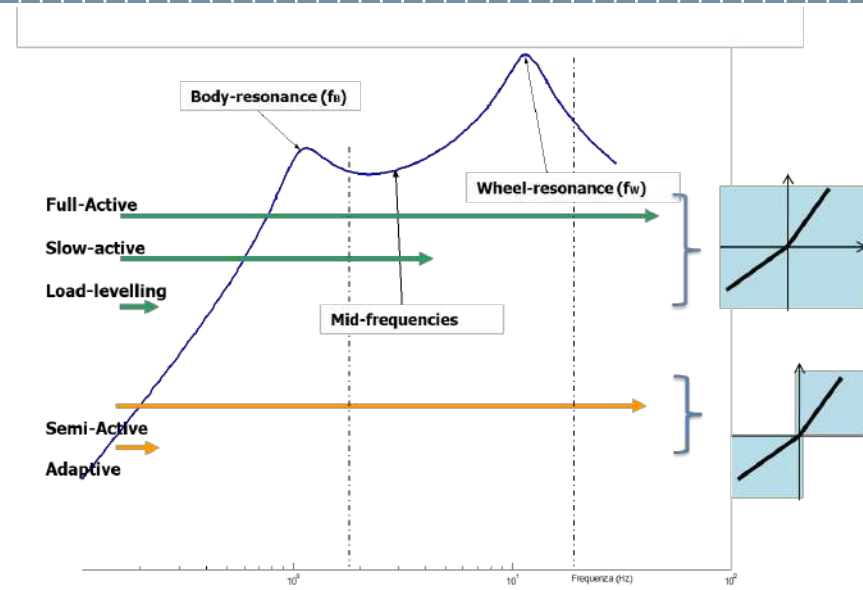
Future Development

Active Suspensions

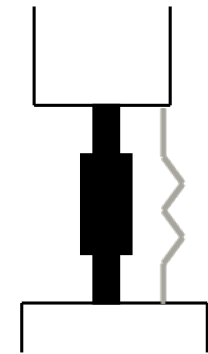


«Slow-active»

Body-bandwidth
(control cut-off around 3-5 Hz)



Actuator: can be electro-hydraulic or electro-mechanic



«Full-active»

Full-bandwidth
(control cutoff around 20-30 Hz)

Future Development

Active Suspensions



Future Development

Active Suspensions



Federico Favalli · 1st
Automation and control engineer
7h · Edited · 🌐

Ferrari Active Suspension Technology!
It is a great challenge and an honor to contribute to the development of the software in Maranello, which controls Multimatic Inc.'s TASV (true active spool valve) system, an innovative and unique component on the market.



Just launched (13/9/22) Ferrari Purosangue
Completely new full-active architecture (by multimatic)

4-quadrants e-motor + ballscrew
EH semi-active (no oil-free)
Full-active (by Multimatic)

Future Development

Active Suspensions

- Easier than semi-active suspensions
- System is LINEAR
- Classical linear control design tools (optimal control, Hinf, etc..) can be used
- Multi-variables and multi-objective control systems can be (easily) designed

Example: LQR regulator assuming the state vector is measurable (or estimated).

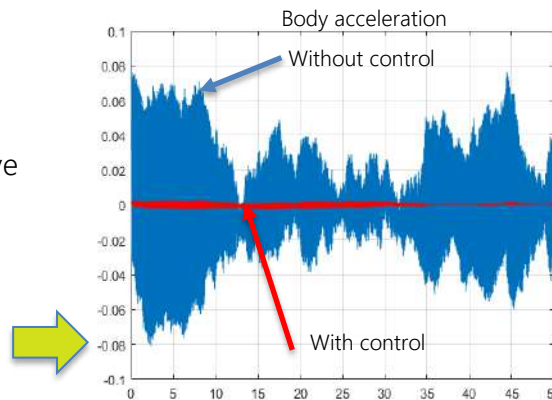
$$J = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T [\ddot{z}^2 + \rho_1 (z - z_t)^2 + \rho_2 (z_t - z_r)^2] dt$$

Comfort objective

Elongation objective

Contact objective

With ρ_1 and ρ_2 very small (all emphasis on comfort)



$$J = \lim_{T \rightarrow \infty} \frac{1}{T} \int_0^T (x' Q x + u' R u + 2x' N u) dt$$

$$Q = \begin{bmatrix} \rho_1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & \rho_2 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}, R = \gamma^2 I, N = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$x = [z - z_t, \dot{z}, z_t - z_r, \dot{z}_t]', u = F$$

$$F^{opt}(t) = -K^{opt} x(t)$$

$0 = A_n' P + P A_n + Q_n - P B R^{-1} B' P, P > 0,$
symmetric and unique solution

$$K^{opt} = R^{-1} (B' P + N')$$

$$A_n = A - B R^{-1} N'$$

$$Q_n = Q - N R^{-1} N'$$

- Introduction
- Semi-Active Damping Control
 - Actuators
 - Models
 - Benchmark
 - Causal Control
- Semi-Active Stiffness Control
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 - Benchmark
 - Causal Control
- Sensing Preliminaries
- A look at the future
- Conclusions

- Control Engineering Look at Suspension Control
- Objectives
- Control Oriented Models
- Technology
- Algorithms with an practical engineering perspective
- Tuning and Calibration

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